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GRADE 12

**MATHEMATICS CONTROLLED MARKING
GUIDELINE**

TERM 1 2021

Marks: 50

This MARKING GUIDELINE consists of 5 pages including cover page

NOTE:

- If a candidate answers a question TWICE, mark the FIRST attempt ONLY.
- Consistent accuracy applies in ALL aspects of the marking guideline.
- If a candidate crossed out an attempt of a question and did not redo the question, mark the crossed-out attempt.
- The mark for substitution is awarded for substitution into the correct formula.

QUESTION 1		
1.1.1	$T_5 = 0,625$ OR $\frac{5}{8}$	✓ answer (1)
1.1.2	$T_n = 10\left(\frac{1}{2}\right)^{n-1}$ OR $20\left(\frac{1}{2}\right)^n$	✓✓ answer (2)
1.1.3	$-1 < r < 1$ $\therefore -1 < \frac{1}{2} < 1$	✓✓ answer (2)
1.2	$S_{20} = 20(20 + 1)(20 + 2) = 9240$ $S_{19} = 19(19 + 1)(19 + 2) = 7980$ $T_{20} = S_{20} - S_{19}$ $\therefore T_{20} = 1260$	✓ S_{20} ✓ S_{19} ✓ T_{20} (3)
1.3	$\sum_{k=1}^{\infty} \left(\frac{1}{3}\right)^k = \frac{1}{3} + \frac{1}{9} + \frac{1}{27} + \dots$ $S_{\infty} = \frac{\frac{1}{3}}{1 - \frac{1}{3}} = \frac{1}{2}$ $\sum_{k=2}^{40} 5 = 5 + 5 + 5 + \dots + 5$ $n = 40 - 2 + 1 = 39$ $S_{39} = 5(39) = 195$ or $S_{39} = \frac{39}{2}(5 + 5) = 195$ $S_{\infty} - S_{39}$ $= \frac{1}{2} - 195$ $= \frac{-389}{2}$ OR -194,5	✓ substitution ✓ S_{∞} ✓ S_{39} ✓ $S_{\infty} - S_{39}$ ✓ answer (5)

1.4	$1; 1+d; 1+2d; \dots$ $1; r; r^2; \dots$ $r = 1+d \dots \dots \dots (1)$ $r^2 = 1+2d \dots \dots \dots (2)$ sub.(1)in(2) $(1+d)^2 = 1+2d$ $1+2d+d^2 = 1+2d$ $d^2 = 0$ $\therefore d = 0 \text{ and } r = 1$ $\therefore 1; 1; 1; \dots$ Arithmetic sequence $1; 1; 1; \dots$ geometric sequence He is correct	✓ eqn (1) and (2) ✓ substitution ✓ comm. diff ✓ comm. ratio ✓ conclusion (5)
(18)		
QUESTION 2		
2.1.1	$\frac{QS}{PS} = \frac{3}{5}$ <i>Line // to one side of a Δ OR prop. theorem, $ST \parallel PV$</i>	✓ S ✓ R (2)
2.1.2	<p><i>length: $QS = 3a$ and $QP = 8a$</i></p> $\text{Area } \Delta PQR = \frac{1}{2} \times QP \times QR \sin \hat{Q}$ $= \frac{1}{2} \times 8a \times 11 \sin \hat{Q}$ $= 44a \sin \hat{Q}$ <p><i>Area of a quad PSTR = Area of ΔPQR - Area ΔSQT</i></p> $= 44a \sin \hat{Q} - \frac{1}{2} \times 3a \times 3 \sin \hat{Q}$ $= \frac{79a}{2} \sin \hat{Q}$ $\frac{\text{Area } \Delta PQR}{\text{Area of quad PSTR}} = \frac{44a \sin \hat{Q}}{\frac{79}{2} a \sin \hat{Q}} = \frac{88}{79}$	✓ area ΔPQR ✓ area ΔSQT ✓ area of a Quad PSTR ✓ ratio ✓ answer (5)

<p>2.2.1</p>	$\hat{D}_1 = \hat{A}_1 = x \quad \text{tan chord theorem}$ $\hat{D}_3 = \hat{A}_1 = x \quad \text{Alt. } < \text{'s}; AB // ED$ $\hat{D}_3 = \hat{D}_2 = x \quad = \text{ chords } = < \text{'s OR}$ $< \text{'s subtended by } = \text{ chords}$	<p>✓ S & R</p> <p>✓ S & R</p> <p>✓ S & R (3)</p>
<p>2.2.2</p>	$\hat{AED} = \hat{B}_2 \quad \text{Ext. } < \text{ of a } \odot \text{ quad}$ $\hat{D}_3 = \hat{D}_1 \quad \text{proven in 2.2.1}$ $\hat{A}_1 = \hat{C}_1 \quad \text{sum of } < \text{'s in a } \Delta$ $\therefore \triangle DEA \parallel \triangle DBC \quad \text{AAA}$	<p>✓ S & R</p> <p>✓ S & R</p> <p>(2)</p>
<p>2.2.3 (a)</p>	<p>In $\triangle DBC$ and $\triangle ADC$</p> $\hat{D}_1 = \hat{A}_2 \quad \text{tan chord theorem}$ $\hat{C} = \hat{C} \quad \text{common } <$ $\hat{B}_2 = \hat{ADC} \quad \text{sum of } < \text{'s in a } \Delta$ $\therefore \triangle DBC \parallel \triangle ADC \quad \text{AAA}$ $\frac{DB}{AD} = \frac{BC}{DC} \quad \parallel \Delta \text{'s}$ $\therefore DC = \frac{BC \times AD}{DB}$	<p>✓ S & R</p> <p>✓ $\triangle DBC \parallel \triangle ADC$</p> <p>✓ prop theorem (3)</p>
<p>2.2.3 (b)</p>	<p>$DB = AE$ chords subt. by $= < \text{'s}$</p> <p>But $\triangle ADC \parallel \triangle DBC$ proved in 2.2.3 (a)</p> <p>and</p> <p>$\triangle DEA \parallel \triangle DBC$ proved in 2.2.2</p> $\therefore \triangle ADC \parallel \triangle DEA \quad \text{both } \parallel \triangle DBC$ $\frac{AD}{DE} = \frac{DC}{EA} \quad \parallel \Delta \text{'s}$ $EA = \frac{DC \times DE}{AD}$	<p>✓ S & R</p> <p>✓ $\triangle ADC \parallel \triangle DEA$</p> <p>✓ prop theorem (3)</p>

2.2.4	$EA = \left(\frac{BC \times AD}{DB}\right) \left(\frac{DE}{AD}\right)$ $EA = \frac{BC \times DE}{EA} \quad \text{since } DB = EA$ $EA^2 = BC \times DE$	✓ substitution ✓ EA (2)
		(20)
QUESTION 3		
3.1.1	$r = 13$ $\cos \alpha = \frac{-5}{13}$	✓ answer (1)
3.1.2	$\tan(180^\circ - \alpha)$ $= -\tan \alpha$ $= -\left(\frac{-12}{-5}\right)$ $= -\frac{12}{5}$	✓ $-\tan \alpha$ ✓ answer (2)
3.2	$\frac{\sin(x - 180^\circ) \cdot \cos(x - 90^\circ)}{\cos(-x - 360^\circ) \sin(90^\circ + x)}$ $= \frac{-\sin x \cdot \sin x}{\cos x \cdot \cos x}$ $= -\frac{\sin^2 x}{\cos^2 x}$ $= -\tan^2 x$	✓ $-\sin x$ ✓ $\sin x$ ✓ $\cos x$ ✓ $\cos x$ ✓ $-\frac{\sin^2 x}{\cos^2 x}$ ✓ $-\tan^2 x$ (6)
3.3	$\sin(A + B) = \cos(90^\circ - (A + B))$ $= \cos((90^\circ - A) - B)$ $= \cos(90^\circ - A)\cos(B) + \sin(90^\circ - A)\sin(B)$ $= \sin A \cos B + \cos A \sin B$	✓ correct co-function ✓ regrouping ✓ simplification (3)
		(12)
	TOTAL	[50]