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# GAUTENG DEPARTMENT OF EDUCATION



## JOHANNESBURG NORTH DISTRICT

### 2021 GRADE 12 CONTROL TEST

### MATHEMATICS TERM1

**MARKS : 100**  
**TIME : 2 hours**

This question paper consist of 17 pages

## INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

1. This question paper consists of **9** questions.
2. Answer **ALL** the questions.
3. Clearly show **ALL** calculations, diagrams, graphs, etc. which was used in determining the answers.
4. Answers only will not necessarily be awarded full marks.
5. Use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
6. Where necessary, answers should be rounded off to **TWO** decimal places, unless stated otherwise.
7. Diagrams are **NOT** necessarily drawn to scale.
- 8. ANSWER Question 7 on Annexure 7.1 - 7.2.2**
- 9. ANSWER Question 8 on Annexure 8.1 - 8.1.3**
- 10. ANSWER Question 9 on Annexure 9.1 - 9.2**
- 11. Tear off page 12 till page 17 . AND SUBMIT theses pages with your answer scripts .**
12. An **information sheet** is on page 11 of the question paper.
13. Number the questions correctly according to the numbering used in the question paper.
14. Write neatly and legibly.

## QUESTION 1

1.1 Solve for  $x$ :

1.1.1  $(x - 5)(x + 1) = 0$  (2)

1.1.2  $2x^2 - 11x + 7 = 0$  (correct to two decimal places) (3)

1.1.3  $x - 5x^{\frac{1}{2}} = -6$  (4)

1.2 Calculate  $a$  and  $b$  if  $\sqrt{\frac{5^{2014} - 5^{2012}}{6}} = a(5^b)$  and  $a$  is not a multiple of 5. (4)

1.3 Solve for  $x$  and  $y$ :

$1 = 3y - x$  and  $y^2 + 2xy = 3x^2 - 7$  (7)

[20]

## QUESTION 2

Given the arithmetic series:  $3 + 10 + 17 + \dots + 150$ .

2.1 Write down the fourth term in the series. (1)

2.2 Determine the general term of the series. (2)

2.3 Express the series in sigma notation. (1)

[4]

## QUESTION 3

3.1 Consider the progression :  $3; \frac{1}{2}; 3; \frac{4}{10}; 3; \frac{16}{50}; \dots$

3.1.1 Write down the next TWO terms of the progression. (1)

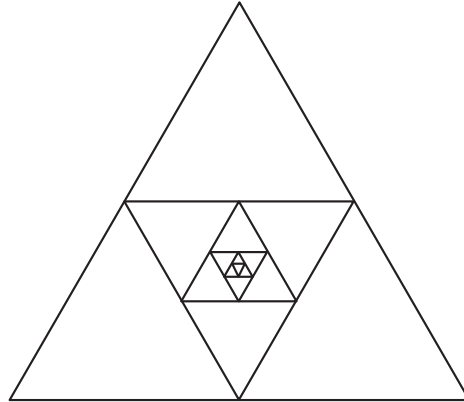
3.1.2 Calculate the sum of the first thirty-five terms of the progression. (5)

3.2 Calculate :  $\sum_{n=3}^{\infty} 5(3)^{1-n}$  (4)

[10]

#### QUESTION 4

In the diagram below, the 1<sup>st</sup> (outer) triangle is an equilateral triangle with sides of  $8\text{cm}$ . A 2<sup>nd</sup> triangle is drawn within this triangle by joining the midpoints of the sides of the 1<sup>st</sup> triangle. This process is continued without end.



4.1 What is the perimeter of the 4<sup>th</sup> triangle? (2)

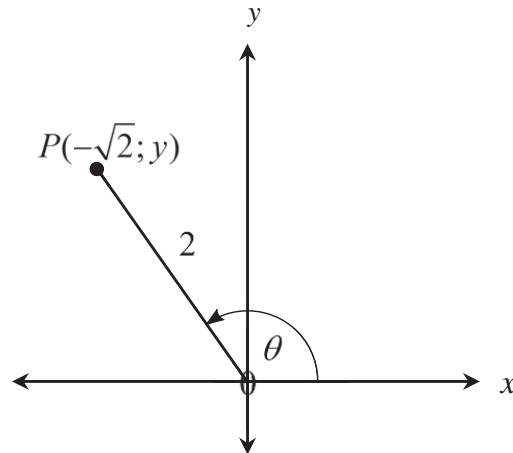
4.2 What is the perimeter of the  $n^{\text{th}}$  triangle? (3)

[5]

### QUESTION 5

5.1 In the sketch below, P is a point on the Cartesian plane, with  $P\hat{O}X = \theta$ .

Use the sketch to determine the following:



5.1.1 The value of  $y$ . (2)

5.1.2 The value of  $\frac{2\sin\theta\cos\theta}{\cos^2\theta - 1}$  (5)

5.2 Simplify the following, WITHOUT USING A CALCULATOR:

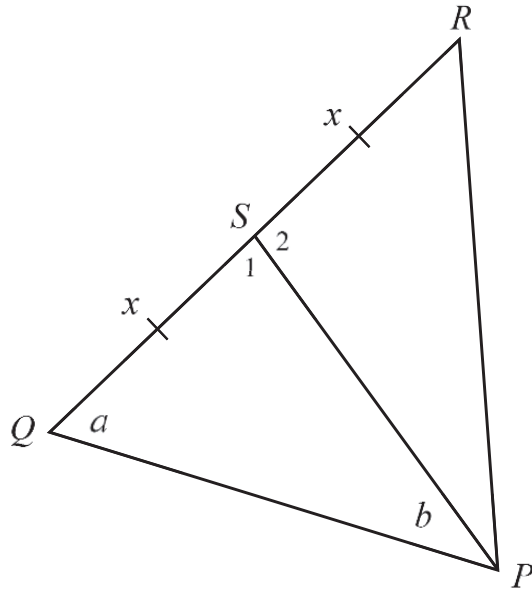
$$\frac{\cos(180^\circ + \theta) \cdot \tan(720^\circ - \theta) \cdot \sin^2(90^\circ - \theta)}{\sin(180^\circ - \theta)} + \sin^2\theta \quad (7)$$

5.3 If  $6\sin^2\theta - 4\cos^2\theta = -5\sin\theta \cdot \cos\theta$ , determine the general solution for  $\theta$ . (8)

[22]

## QUESTION 6

In the sketch below, PS is the median of  $\triangle PQR$ , and thus  $QS = SR = x$ .  $\hat{Q} = a$  and  $\hat{QPS} = b$ .



6.1 Show that  $PS = \frac{x \sin a}{\sin b}$  (2)

6.2 Express the size of  $S_2$ , in terms of  $a$  and  $b$ , without reasons. (1)

6.3 Hence, show that: Area of  $\triangle PSR = \frac{x^2 \sin a \times \sin(a + b)}{2 \sin b}$  (3)

6.4 Determine the area of  $\triangle PSR$ , rounded to two decimal places, if  $x = 14,2 \text{ cm}$ ,  $a = 34^\circ$  and  $b = 41^\circ$ . (3)

[9]

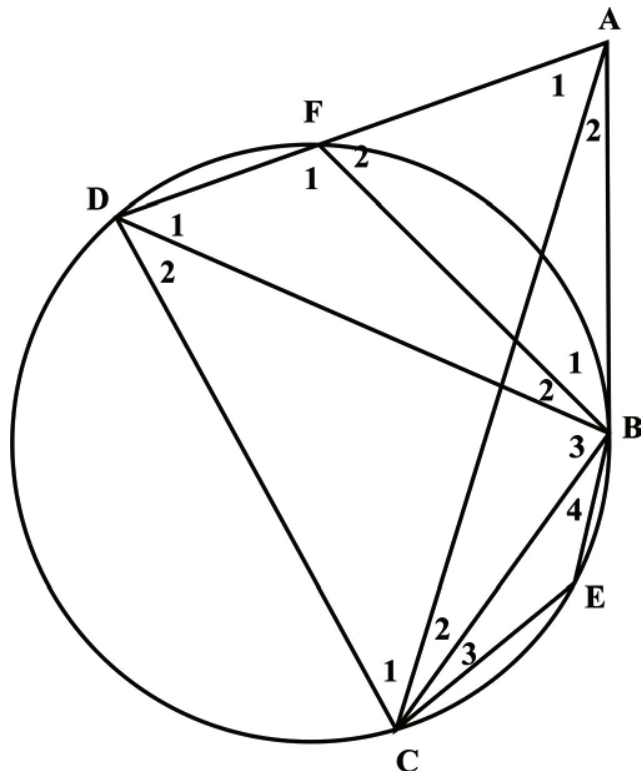
Give reasons for your statements and calculations in QUESTIONS 7, 8 and 9

Use the Annexure's provided to answer QUESTIONS 7, 8 and 9

### QUESTION 7

7.1 In the diagram below, AB is a tangent to the circle passing through B, E, C and D

AD cuts the circle at F. AC is drawn.



Give reasons for the following statements:

(5)

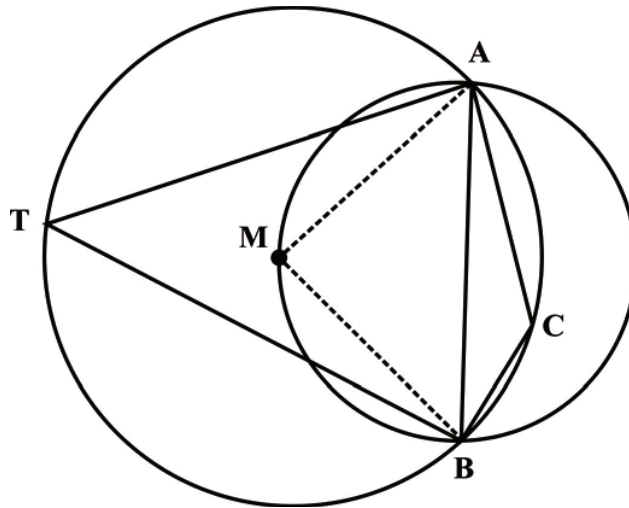
STATEMENT	REASONS
$\hat{C}_1 + \hat{C}_2 = \hat{F}_2$	
$\hat{D}_2 + \hat{E} = 180^\circ$	
$\hat{B}_1 = \hat{D}_1$	
$\hat{B}_2 + \hat{B}_3 + \hat{D}_1 + \hat{D}_2 = 180^\circ$	
$\hat{B}_2 + \hat{B}_1 = \hat{C}_1 + \hat{C}_2$	



7.2 In the diagram below, circle centre M intersects a second smaller circle at A and B.

A, C, B and T are points on circle M.

AB is the diameter of the smaller circle.



7.2.1 Determine the size of  $\hat{C}$ . (6)

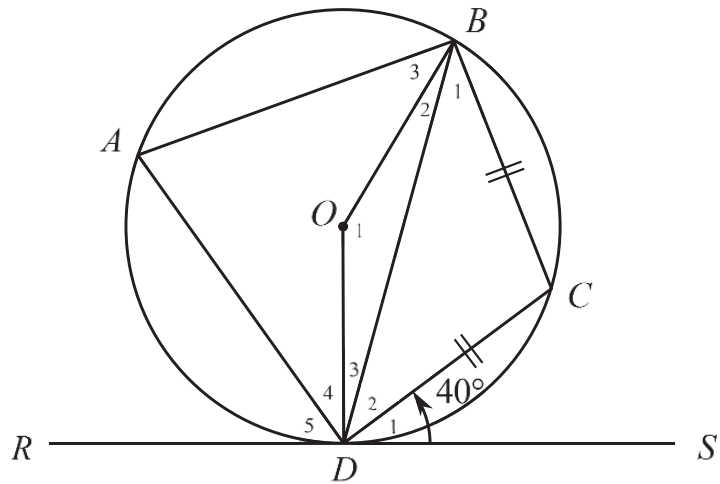
7.2.2 Explain why AMBC is not a cyclic quadrilateral. (1)

[12]

### QUESTION 8

In the figure below,  $RDS$  is a tangent to circle  $O$  at  $D$ .  $BC = DC$ , and  $\hat{CDS} = 40^\circ$ .

Thus, calculate the size of the following angles, with reasons.



8.1  $\hat{BDC}$  (2)

8.2  $\hat{C}$  (2)

8.3  $\hat{A}$  (2)

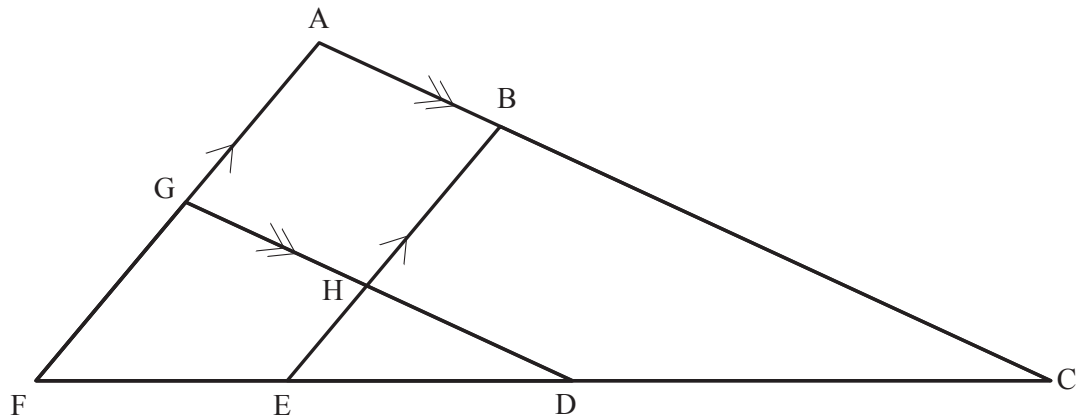
8.4  $\hat{O}_1$  (1)

[7]

## QUESTION 9

The diagram below is the top view design of a new railway system. There are eight stations being built and these are labelled with letters from A- H. You have been asked to do some calculations for the railway company. As the engineer you know that:

- $AF \parallel BE$  and  $AC \parallel GD$ .
- $\frac{AB}{BC} = \frac{4}{7}$  and  $\frac{AG}{AF} = \frac{9}{17}$ .



9.1 Calculate

9.1.1  $\frac{FE}{FC}$ . (3)

9.1.2  $\frac{CD}{DF}$ . (2)

9.2 If the straight line distance of the track from F to C is 374 kilometres and it takes 50 hours to build one kilometre of the track, determine the number of hours it will take to build the section from E to D. (6)

[11]

**TOTAL 100 MARKS**

# INFORMATION SHEET: MATHEMATICS

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni)$$

$$A = P(1 - ni)$$

$$A = P(1 - i)^n$$

$$A = P(1 + i)^n$$

$$\sum_{i=1}^n 1 = n$$

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}$$

$$T_n = a + (n-1)d$$

$$S_n = \frac{n}{2}(2a + (n-1)d)$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1} ; r \neq 1$$

$$S_{\infty} = \frac{a}{1 - r} ; -1 < r < 1$$

$$F = \frac{x[(1+i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1+i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

In  $\Delta ABC$ :

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cdot \cos A$$

$$\text{area} \Delta ABC = \frac{1}{2} ab \cdot \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cdot \cos \beta + \cos \alpha \cdot \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cdot \cos \beta - \cos \alpha \cdot \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cdot \cos \beta - \sin \alpha \cdot \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cdot \cos \beta + \sin \alpha \cdot \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2 \sin^2 \alpha \\ 2 \cos^2 \alpha - 1 \end{cases}$$

$$\sin 2\alpha = 2 \sin \alpha \cdot \cos \alpha$$

$$(x; y) \rightarrow (x \cos \theta - y \sin \theta ; y \cos \theta + x \sin \theta)$$

$$\bar{x} = \frac{\sum fx}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$

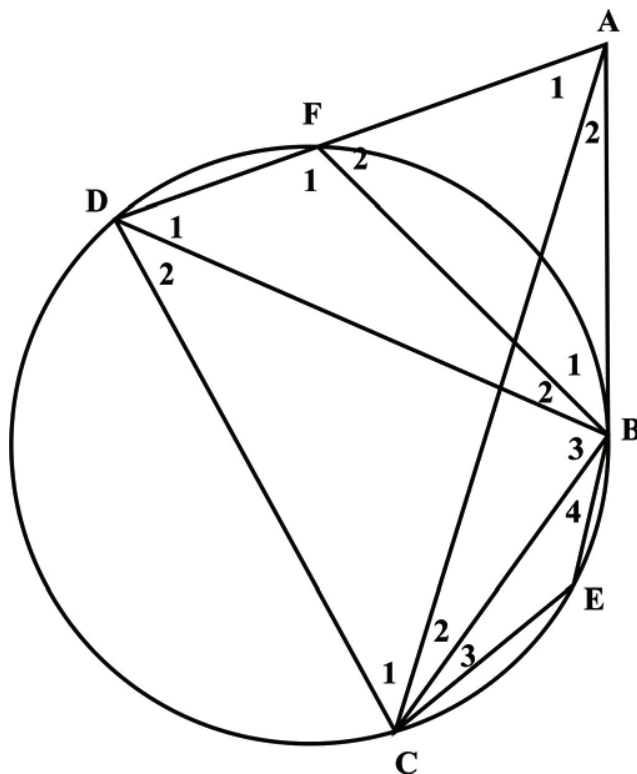
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Class: \_\_\_\_\_

## ANNEXURE 7.1 - 7.2 .2

### QUESTION 7

7.1

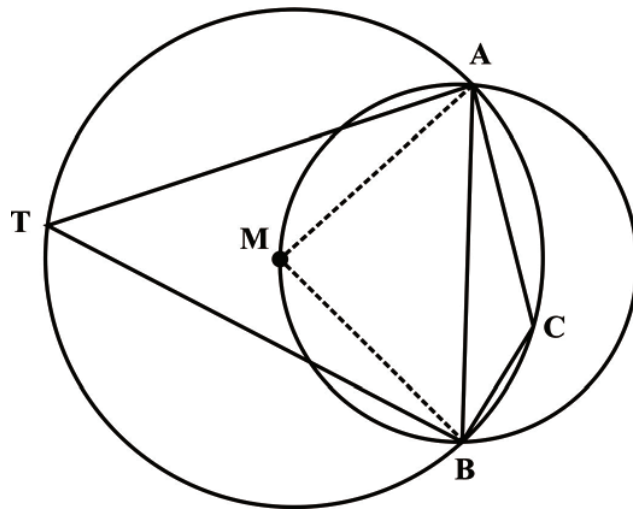


Give reasons for the following statements:

(5)

STATEMENT	REASONS
$\hat{C}_1 + \hat{C}_2 = \hat{F}_2$	
$\hat{D}_2 + \hat{E} = 180^\circ$	
$\hat{B}_1 = \hat{D}_1$	
$\hat{B}_2 + \hat{B}_3 + \hat{D}_1 + \hat{D}_2 = 180^\circ$	
$\hat{B}_2 + \hat{B}_1 = \hat{C}_1 + \hat{C}_2$	

7.2



7.2.1 Determine the size of  $\hat{C}$ . (6)

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7.2.2 Explain why AMBC is not a cyclic quadrilateral. (1)

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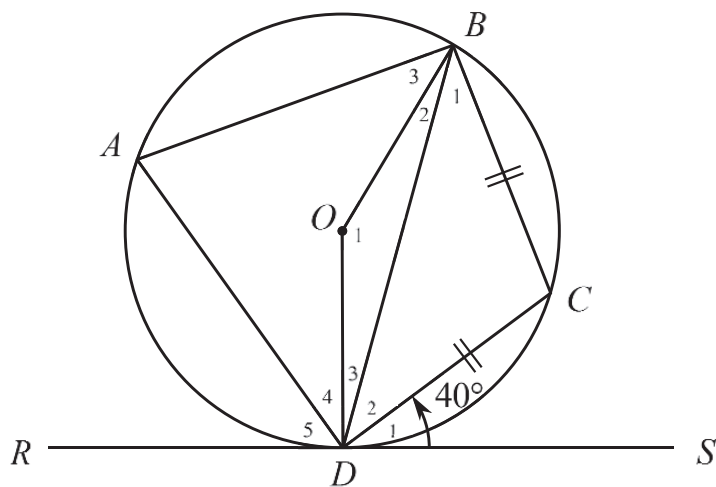
[12]

Name: \_\_\_\_\_

Class: \_\_\_\_\_

# ANNEXURE 8.1 - 8.1.3

## QUESTION 8



8.1  $\hat{BDC}$  (2)

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8.2  $\hat{C}$  (2)

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8.3  $\hat{A}$  (2)

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8.4  $\hat{O}_1$  (1)

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[7]

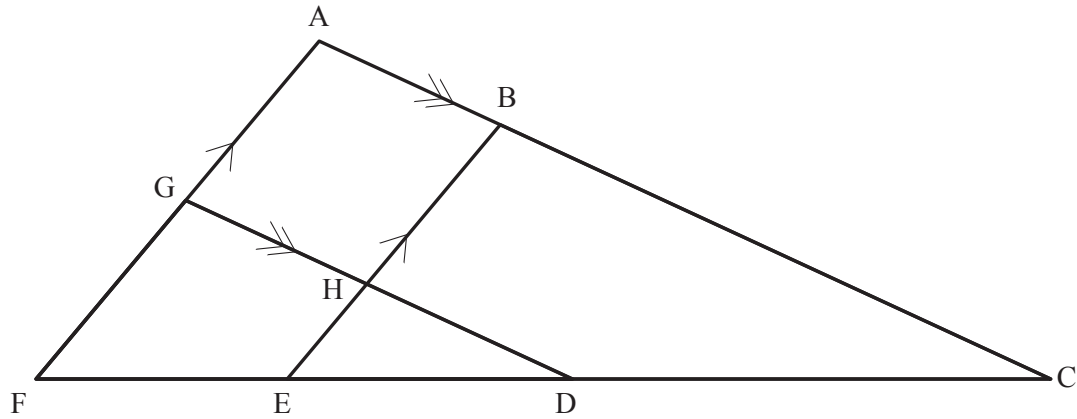


Name: \_\_\_\_\_

Class: \_\_\_\_\_

## ANNEXURE 9.1 - 9.2

### QUESTION 9



9.1 Calculate

9.1.1  $\frac{FE}{FC}$ . (3)

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9.1.2  $\frac{CD}{DF}$ . (2)

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[illegible]

[11]