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NATIONAL SENIOR CERTIFICATE

GRADE 12

SEPTEMBER 2019

MATHEMATICS P1

MARKS: 150

TIME: 3 hours



This question paper consists of 8 pages and 1 information sheet.

INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

- 1. This question paper consists of ELEVEN questions. Answer ALL the questions.
- 2. Clearly show ALL calculations, diagrams, graphs, et cetera that you have used in determining your answer.
- 3. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
- 4. Answers only will NOT necessarily be awarded full marks.
- 5. If necessary, round off answers to TWO decimal places, unless stated otherwise.
- 6. Diagrams are NOT necessarily drawn to scale.
- 7. Number the answers correctly according to the numbering system used in this question paper.
- 8. An information sheet with formulae is included at the end of the question paper.
- 9. Write neatly and legibly.

(EC/SEPTEMBER 2019)

1.1 Solve for x

$$1.1.1 \quad x^2 - 3x - 4 = 0 \tag{3}$$

1.1.2
$$2x^2 - x - 7 = 0$$
 (correct to TWO decimal places) (3)

$$1.1.3 \quad 5^{x+1} - 5^x = 2500 \tag{3}$$

$$1.1.4 \quad (x-3)(x+1) < 12 \tag{4}$$

1.2 Solve the following equations simultaneously:

$$2x = y + 1 3x^2 - xy - y^2 = 1$$
 (6)

1.3 Given that $f(x) = x^2 - 2px + 8 + 2p$ has two equal roots and p < 0, determine the coordinates of the turning point of h, if h(x) = f(x) - 3. (5) [24]

QUESTION 2

- 2.1 Given the quadratic number pattern: 3; 1; -3; -9; ...
 - 2.1.1 Write down the next 2 terms of the pattern. (1)
 - 2.1.2 Determine T_n , the n^{th} term of the pattern, in the form $T_n = an^2 + bn + c$. (4)
 - 2.1.3 Which term of the pattern has a value of -809? (3)
- 2.2 Given the arithmetic sequence: -1; 1; 3; 5; ...
 - 2.2.1 Determine T_{53} , the 53rd term of the sequence. (2)
 - 2.2.2 Determine the sum of the first 29 terms of the sequence. (2)
 - 2.2.3 Hence, write your answer in sigma notation. (2)
- 2.3 In an arithmetic sequence, $T_4 = 2x + y$ and $T_{10} = 8x 2y$. Determine the first term of the sequence in terms of x and y. (5)

Given that: $p = \sum_{k=1}^{\infty} (x-1)^k$

- 3.1 Determine the values of x for which p converges. (2)
- 3.2 Calculate the value of p when $x = \frac{2}{3}$. (4)

QUESTION 4

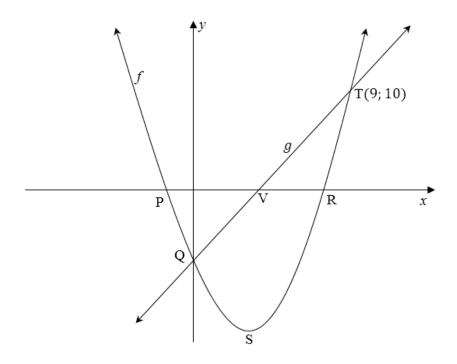
Given: $f(x) = 1 + \frac{2}{x+3}$

- 4.1 Write down the equations of the asymptotes of f. (2)
- 4.2 Calculate the x and y intercepts of f. (3)
- 4.3 Draw a neat sketch of f, clearly indicating all intercepts with the axes and any asymptotes. (4)
- 4.4 Given that *h* is a reflection of *f* in the *x*-axis, determine the equation of the axis of symmetry of *h* having a positive gradient. (4) [13]

<u>5</u>

QUESTION 5

The diagram below shows the graphs of $f(x) = x^2 - 7x - 8$ and g(x) = mx + c. P and R are x-intercepts of f, and V is the x-intercept of g. S is the turning point of f. f and g intersect on the y-axis at Q and also at T(9; 10).



- 5.1 Write down the coordinates of Q. (1)
- 5.2 Determine the equation of g. (3)
- 5.3 Write down the equation of f in the form $y = a(x + p)^2 + q$. (2)
- 5.4 Hence, or otherwise, determine the coordinates of S, the turning point of f. (2)
- Determine the coordinates of a point W, on f, such that the average gradient between T and W is 1. (5)
- 5.6 Determine the values of x for which f(x). g(x) < 0. (4) [17]

Given: $f(x) = \log_m x$

- 6.1 Determine the value of m, if the point (64;3) lies on f. (2)
- 6.2 Determine the equation of f^{-1} in the form y = ... (2)
- Draw a neat sketch of f^{-1} , showing all intercepts with the axes. Indicate at least one other point on your graph. (2)
- 6.4 Write down the range of *h* if: $h(x) = f^{-1}(x) 2$ (1)

QUESTION 7

- 7.1 Kamva bought a motorbike valued at R40 000. After 5 years the value of the motorbike had depreciated to R26 700, at a rate of r % p.a. on the reducing balance method, compounded annually. Calculate r, the rate of depreciation. (3)
- A bank granted Nathan a loan for R1 200 000 to buy a house. He agreed to repay the loan over a period of 15 years at an interest rate of 11,5% p.a. compounded monthly. He made his first payment at the end of the first month after the loan was granted.
 - 7.2.1 Calculate Nathan's monthly instalment. (3)
 - 7.2.2 Due to unforeseen circumstances, Nathan could not pay his 76th, 77th, 78th, 79th and 80th instalments. He resumed his payments at the end of the 81st month.
 - (a) Calculate the outstanding balance at the end of the 80th month. (5)
 - (b) If Nathan continues paying the same monthly instalment, how many months will it take him to pay the balance outstanding at the end of the 80th month?

(4)

8.1 Determine
$$f'(x)$$
 from first principles if $f(x) = 3 - 2x^2$ (5)

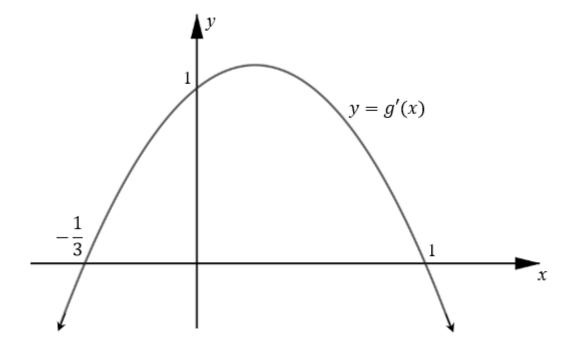
8.2 Determine:

$$8.2.1 D_x \left[x \left(x - 2 \right)^2 \right] \tag{4}$$

8.2.2
$$\frac{dy}{dx}$$
 if $y = ax^{\frac{3}{7}} - \frac{2x}{\sqrt{x}} + 3$ (3)

QUESTION 9

The diagram below shows the graph of y = g'(x) where $g(x) = ax^3 + bx^2 + cx + d$. The graph g'(x) cuts the y-axis at (0; 1) and the x-axis at $(-\frac{1}{3}; 0)$ and (1; 0).



- 9.1 Write down the *x*-coordinate(s) of the stationary point(s) of g. (2)
- 9.2 Determine the x-coordinate of the point of inflection of g. (2)
- 9.3 Determine the values of x for which g is an increasing function. (2)
- 9.4 Determine the equation of g'(x) in the form: $g'(x) = px^2 + qx + r$. (4)
- 9.5 Given that:
 - g(x) + 1 passes through (0;0) and
 - $g'(x) = -3x^2 + 2x + 1$

Show that for
$$g(x)$$
, $a = -1$, $b = 1$, $c = 1$ and $d = -1$. (5)

[15]

Two numbers are such that their sum is 18. One of the numbers is multiplied by the square of the other. Calculate the numbers that make this product a maximum.

[7]

QUESTION 11

- 11.1 A school has 530 learners. Each learner is expected to choose his/her summer extra-curricular activity from the following:
 - Athletics
 - Cricket
 - Tennis

The choices for 2019 were recorded in the following partially completed table:

	Athletics	Cricket	Tennis	Total
Girls	120	а	57	288
Boys	b	108	28	242
Total	226	219	85	530

- 11.1.1 Determine the values of a and b. (2)
- 11.1.2 A learner is chosen at random. Determine the probability that:
 - (a) It is a boy who plays cricket (2)
 - (b) It is a girl or **not** a tennis player (3)
- 11.2 Consider the letters of the word: NUMERATOR.
 - 11.2.1 How many 9 letter word-arrangements can be formed, if repetition of letters is allowed? (1)
 - How many 9 letter word-arrangements can be formed, if all 4 vowels are never together and repetition of letters is not allowed? (3)
 - 11.2.3 An 8 letter word-arrangement is made from the word NUMERATOR.
 All the vowels must be included in this word-arrangement and repetition of letters is not allowed. What is the probability that all odd-number spaces are occupied by vowels?

 (4)

TOTAL: 150

INFORMATION SHEET: MATHEMATICS

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1+ni) \qquad A = P(1-ni) \qquad A = P(1-i)^n \qquad A = P(1+i)^n$$

$$T_n = a + (n-1)d \qquad S_n = \frac{n}{2}(2a + (n-1)d)$$

$$T_n = ar^{n-1} \qquad S_n = \frac{a(r^n - 1)}{r - 1} \quad ; \quad r \neq 1 \qquad S_{\infty} = \frac{a}{1 - r}; -1 < r < 1$$

$$F = \frac{x[(1+i)^n - 1]}{i} \qquad P = \frac{x[1 - (1+i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \qquad M\left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c \qquad y - y_1 = m(x - x_1) \qquad m = \frac{y_2 - y_1}{x_2 - x_1} \qquad m = \tan \theta$$

$$(x-a)^2 + (y-b)^2 = r^2$$

In
$$\triangle ABC$$
: $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$ $a^2 = b^2 + c^2 - 2bc \cdot \cos A$ $area \triangle ABC = \frac{1}{2}ab \cdot \sin C$
 $\sin(\alpha + \beta) = \sin \alpha \cdot \cos \beta + \cos \alpha \cdot \sin \beta$ $\sin(\alpha - \beta) = \sin \alpha \cdot \cos \beta - \cos \alpha \cdot \sin \beta$
 $\cos(\alpha + \beta) = \cos \alpha \cdot \cos \beta - \sin \alpha \cdot \sin \beta$ $\cos(\alpha - \beta) = \cos \alpha \cdot \cos \beta + \sin \alpha \cdot \sin \beta$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases} \qquad \qquad \sin 2\alpha = 2\sin \alpha . \cos \alpha$$

$$\bar{x} = \frac{\sum x}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$