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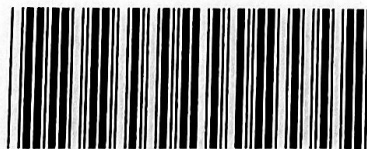
DEPARTMENT OF EDUCATION  
DEPARTEMENT VAN ONDERWYS  
LEFAPHA LA THUTO  
ISEBE LEZEMFUNDO

**PROVINCIAL PREPARATORY EXAMINATION**

**GRADE 12**

**MATHEMATICS P1**

**SEPTEMBER 2021**



CMATHP1

**MARKS: 150**

**TIME: 3 hours**

**This question paper consists of 11 pages including an information sheet.**

**QUESTION 1**1.1 Solve for  $x$ .

1.1.1  $x^2 - x - 6 = 0$  (3)

1.1.2  $x(x+6)+1=0$  (correct to TWO decimal places) (4)

1.1.3  $6x - 2x^2 \leq 0$  (3)

1.1.4  $(\sqrt{\sqrt{2}-x})(\sqrt{\sqrt{2}+x}) = x$  (5)

1.2 Solve simultaneously for  $x$  and  $y$ :

$x - y = 3$  and  $x^2 - 3y^2 = 13$  (6)

1.3 If  $x^2 = 7$  and  $x > 0$ , determine the value of  $x^5$  without using a calculator. (3)  
**[24]****QUESTION 2**

2.1 The first four terms of a quadratic number pattern are 171; 282; 387; 486 ...

2.1.1 Write down the second difference. (2)

2.1.2 Determine the  $n^{\text{th}}$  term of this pattern in the form  $T_n = an^2 + bn + c$ . (4)2.1.3 Another pattern, with general term,  $P_n = -60n + 2754$ , is given. Which term of this new pattern will be the same as that of the quadratic pattern 171; 282; 387; 486 ...? (4)2.2 Study the geometric series  $\frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \dots$ 

2.2.1 Calculate the sum of the first 16 terms. (3)

2.2.2 Calculate the value of  $n$  such that  $S_\infty - T_n = \frac{1023}{4096}$ . (5)  
**[18]**

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**QUESTION 3**

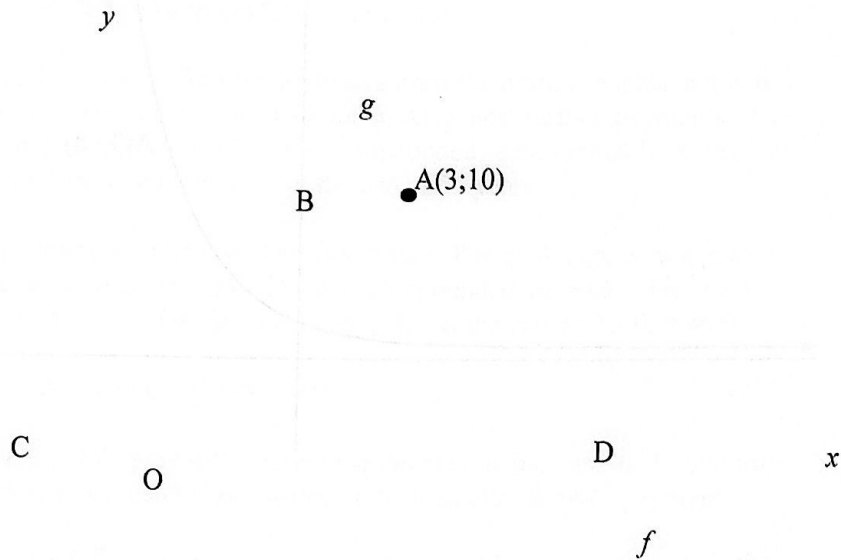
Consider:  $\sum_{k=1}^n (6k + 13)$

- 3.1 Show that  $\sum_{k=1}^n (6k + 13) = 3n^2 + 16n$ . (3)
- 3.2 Hence, calculate the difference between the sum of the first 34 terms and the sum of the first 33 terms. (2)
- 3.3 The first difference of a quadratic number pattern is given by  $T_k = 6k + 13$ . If the fifth term of the quadratic number pattern is 120, determine the value of the third term. (3)

**[8]**

## QUESTION 4

Sketched below are the graphs of  $f(x) = -x^2 + 4x + 5$  and  $g(x) = \frac{1}{x+p} + q$ . B is the turning point of  $f$ . The asymptotes of  $g$  intersect at B and the point A(3; 10) lies on  $g$ . C and D are the  $x$ -intercepts of  $f$ .

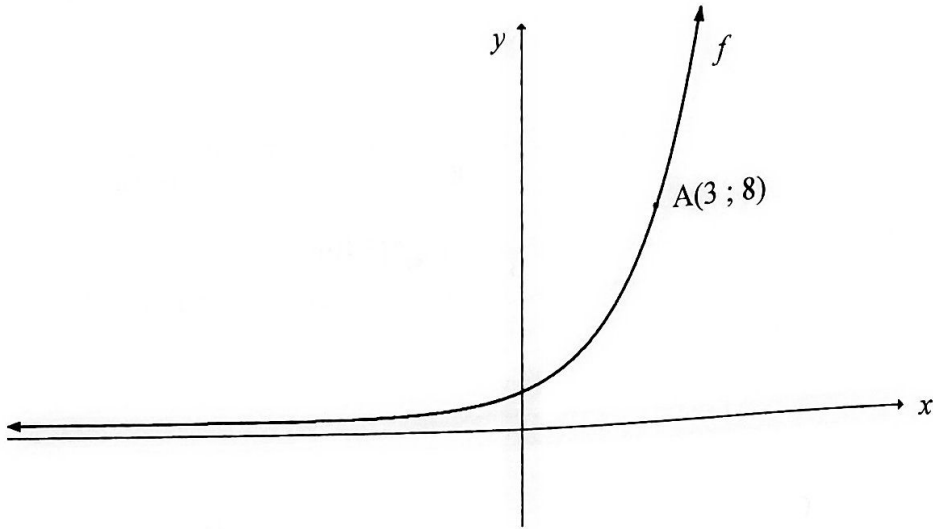


- 4.1 Determine the coordinates of B. (3)
- 4.2 Hence, write down the values of  $p$  and  $q$ . (2)
- 4.3 Describe the nature of roots of the graph of  $t$ , if  $t(x) = -f(x) + 10$ . (2)
- 4.4 The graph of  $h$ , where  $h(x) = g(x+m) + n$ , has asymptotes  $x = 4$  and  $y = 3$ . Write down the value(s) of  $m$  and  $n$ . (2)
- 4.5 The tangent,  $y = 6x + k$ , touches the graph of  $f$  at P. Determine the coordinates of P. (4)
- 4.6 Determine the values of  $x$  for which:
- 4.6.1  $g(x) \geq 10$  (2)
- 4.6.2  $f(x) \cdot g'(x) > 0$  (4)

[19]

**QUESTION 5**

In the diagram below, the graph of  $f(x) = b^x$  is drawn.  $A(3 ; 8)$  is a point on  $f$ .



- 5.1 Calculate the value of  $b$ . (2)
- 5.2 Determine the equation of  $f^{-1}$ , the inverse of  $f$ , in the form  $y = \dots$  (2)
- 5.3 Sketch the graph of  $f^{-1}$ . Clearly show the intercept(s) with the axes, as well as the coordinates of ONE other point. (3)
- 5.4 Determine for which values of  $x$ , will  $f^{-1}(x) < 4$ . (3)
- 5.5 Describe the transformation from  $f$  to  $h(x) = \frac{1}{4}f(x)$ . (3)
- [13]**

**QUESTION 6**

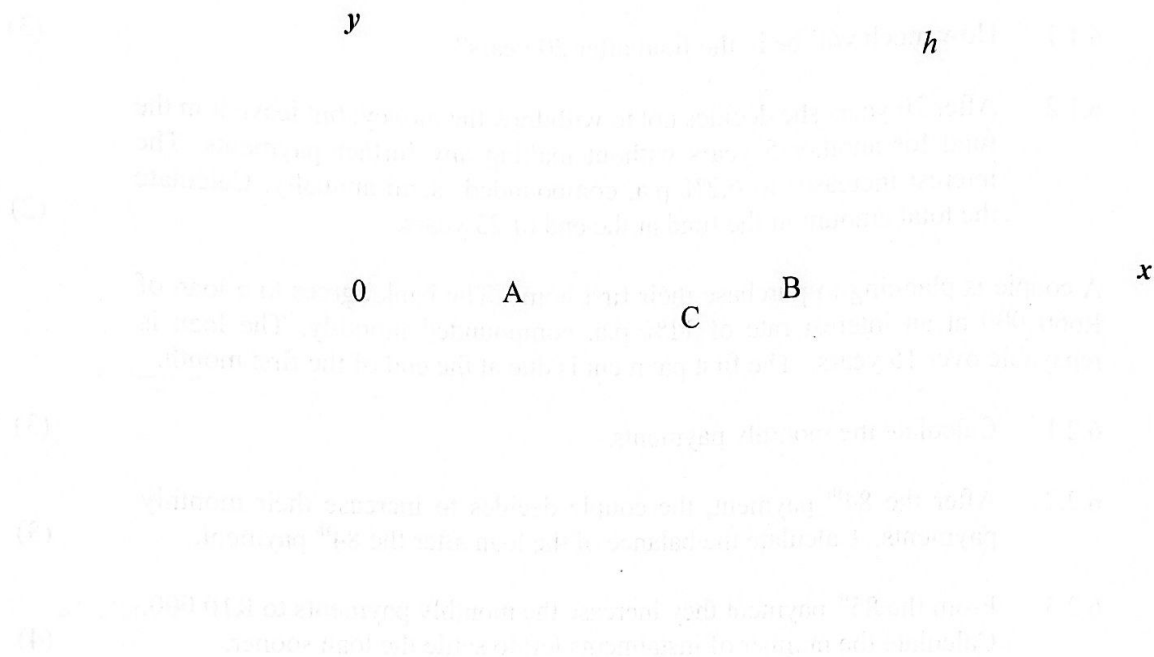
- 6.1 Bonolo Rentsi deposits R4 100 quarterly in a retirement fund for 20 years. The fund earns interest at a rate of 6% p.a. compounded quarterly. The first deposit was made at the end of March of the first year and the last deposit at the end of December of the 20<sup>th</sup> year.
- 6.1.1 How much will be in the fund after 20 years? (3)
- 6.1.2 After 20 years she decides not to withdraw the money, but leave it in the fund for another 5 years without making any further payments. The interest increases to 6,2% p.a. compounded semi-annually. Calculate the total amount in the fund at the end of 25 years. (2)
- 6.2 A couple is planning to purchase their first home. The bank agrees to a loan of R660 000 at an interest rate of 11% p.a. compounded monthly. The loan is repayable over 15 years. The first payment is due at the end of the first month.
- 6.2.1 Calculate the monthly payments. (3)
- 6.2.2 After the 84<sup>th</sup> payment, the couple decides to increase their monthly payments. Calculate the balance of the loan after the 84<sup>th</sup> payment. (3)
- 6.2.3 From the 85<sup>th</sup> payment they increase the monthly payments to R10 000. Calculate the number of instalments left to settle the loan sooner. (4)
- [15]**

**QUESTION 7**

- 7.1 Determine  $f'(x)$  from first principles if  $f(x) = 4x^2 - 3$ . (5)
- 7.2 Determine:
- 7.2.1  $\frac{dy}{dx}$ , if  $y = (3x - 4)(5x + 2)$  (2)
- 7.2.2  $\frac{d}{dx} \left( x\sqrt{x} - \frac{2}{x^2} \right)$  (4)
- [11]**

**QUESTION 8**

In the diagram below, the graph of  $h(x) = (x-1)^2(x+k) = x^3 - 5x^2 + 7x - 3$  is drawn. A and B are the  $x$ -intercepts and C the minimum turning point of  $h$ .

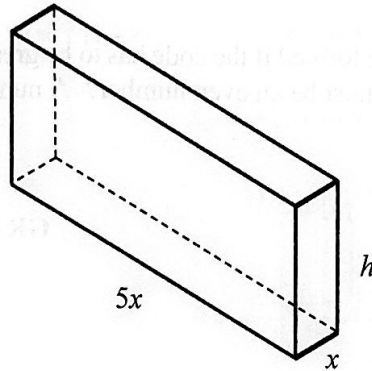


- 8.1 Calculate the coordinates of:
- 8.1.1 A and B (3)
- 8.1.2 C (4)
- 8.2 Determine the value(s) of  $x$  for which:
- 8.2.1 the graph is concave down. (3)
- 8.2.2  $h(-x) > 0$  (2)
- 8.3 Determine the value(s) of  $p$  for which  $h(x) + 4 = p$  has only one solution. (4)
- [16]



**QUESTION 9**

The figure below shows a solid brick in the shape of a rectangular prism. The length is  $5x$  units. The width is  $x$  units and the height is  $h$  units. The total surface area is  $720 \text{ cm}^2$ .



- 9.1 Show that the volume of the brick is given by:  $V = 300x - \frac{25}{6}x^3$  cubic units. (5)
- 9.2 Calculate the maximum volume of the brick. (5)
- [10]**

**QUESTION 10**

- 10.1 Events A and B are given such that  $P(A \text{ or } B) = \frac{3}{5}$  and  $P(A) = \frac{2}{5}$ .  
Determine  $P(B)$  if:
- 10.1.1 A and B are mutually exclusive. (2)
- 10.1.2 A and B are independent events. (3)
- 10.2 Events S and T are independent such that  $P(S) = P(T) = y$  and  $P(S \text{ or } T) = 0,84$ .  
Determine the numerical value of  $y$ . (5)
- [10]**

**QUESTION 11**

A four digit code is created by using the numerals 0 to 6.

- 11.1 How many four digit codes can be formed if the numerals can be repeated? (2)
- 11.2 How many four digit codes can be formed if the code has to be greater than 2 000, but less than 3 000 and the code must be an even number? A numeral must only be used once. (4)  
[6]

**GRAND TOTAL: 150**