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EDUCATION
REPUBLIC OF SOUTH AFRICA

**NATIONAL
SENIOR CERTIFICATE**

GRADE 12

MATHEMATICS P2

PREPARATORY EXAMINATION

SEPTEMBER 2022

MARKING GUIDELINE

MARKS: 150

TIME: 3 hours

These marking guideline consists of 15 pages.

NOTE:

- If a candidate answered a QUESTION TWICE, mark only the FIRST attempt.
- If a candidate crossed out an answer and did not redo it, mark the crossed-out answer.
- Consistent accuracy applies to ALL aspects of the marking guidelines.
- Assuming values/answer in order to solve a problem is unacceptable.

GEOMETRY	
S	A mark for a correct statement (A statement mark is independent of a reason.)
R	A mark for a correct reason (A reason mark may only be awarded if the statement is correct.)
S/R	Award a mark if the statement AND reason are both correct.

QUESTION 1

40	47	48	51	53	57	58	58	59	59
60	60	60	60	61	62	63	64	66	69

1.1.1	$\bar{x} = \frac{1155}{20}$ $\bar{x} = 57,75 \text{ kg}$ Answer only: full marks	A✓ 1155 CA✓ answer Penalty 1 mark for rounding here for the entire paper	(2)
1.1.2	$\sigma = 6,73702 \approx 6,74 \text{ kg}$	A✓ answer	(1)
1.2	$(\bar{x} - \sigma ; \bar{x} + \sigma)$ $(57,75 - 6,74 ; 57,75 + 6,74)$ limit = $(51,01 ; 64,49)$ $\therefore 14 \text{ boys}$	CA✓ interval CA✓ answer	(2)
1.3.1	22	A✓ answer	(1)
1.3.2	$\bar{x} = \frac{1320}{22}$ $\bar{x} = 60 \text{ kg}$	CA✓ based on 1.3.1	(1)
1.4	$\bar{x} = \frac{5x+1155}{25} = 60$ $5x+1155=1500$ $5x=345$ $x=69 \text{ kg}$	CA✓ $\frac{5x+1155}{25}$ CA✓ equation CA✓ simplification CA✓ answer	(4)
			[11]

QUESTION 2

2.1

DISTANCE, d (in km)	FREQUENCY	CUMULATIVE FREQUENCY
$0 < d \leq 5$	8	8
$5 < d \leq 10$	41	49
$10 < d \leq 15$	63	112
$15 < d \leq 20$	52	164
$20 < d \leq 25$	41	205
$25 < d \leq 30$	38	243
$30 < d \leq 35$	7	250
TOTAL	250	

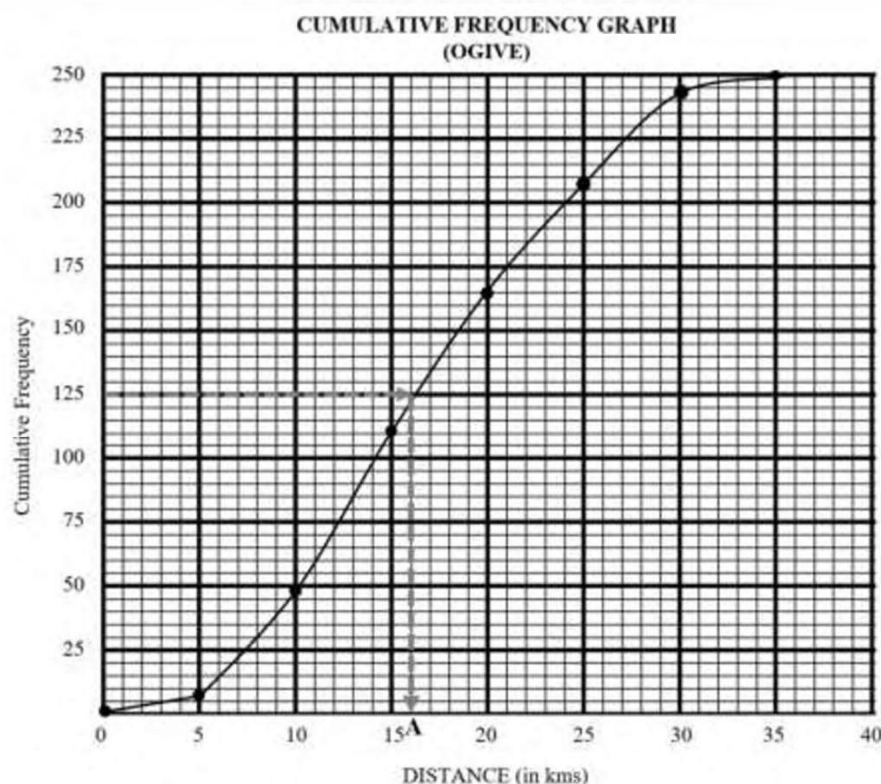
A✓ 8 and 49

CA✓ 112 and 164

CA✓ 205, 243 and 250

(3)

2.2



A✓ grounded at (0 ; 0)

CA✓ cumulative frequencies for y-coords

CA✓ 5 other points

A✓ correct smooth shape

(4)

2.3

See ogive for dotted lines and point marked A.
Median = 16 km

OR

Answer only: Full marks (accept 15,16,17)

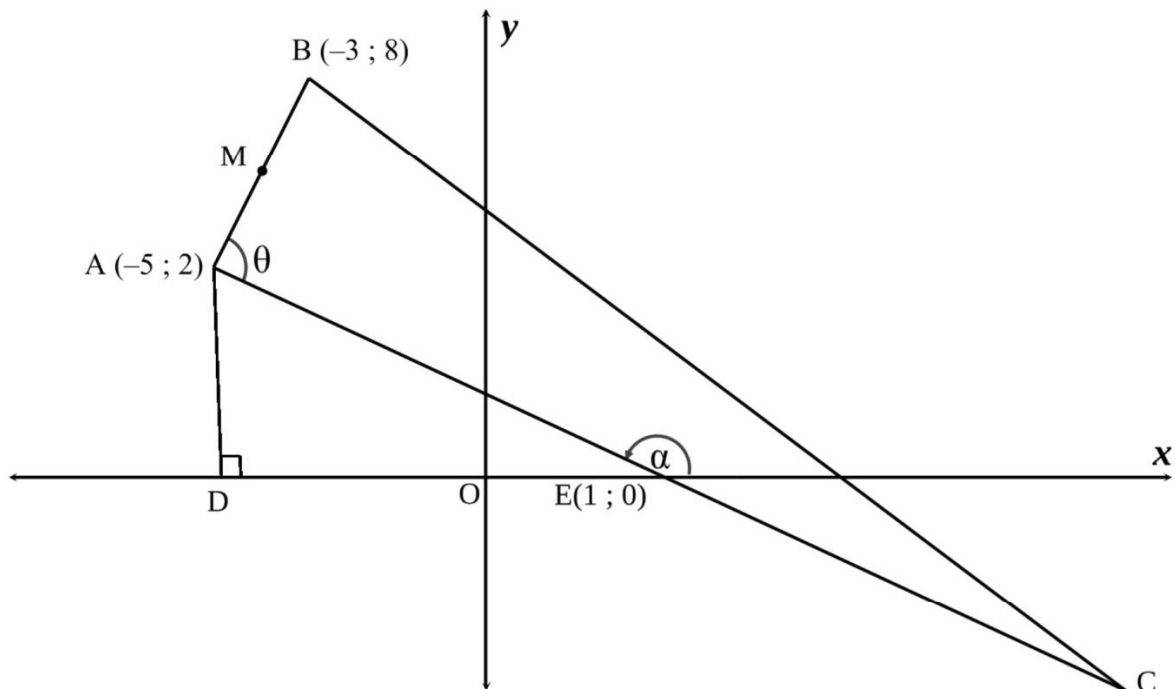
CA✓ indication on graph

CA✓ approx. median

(2)

[9]

QUESTION 3



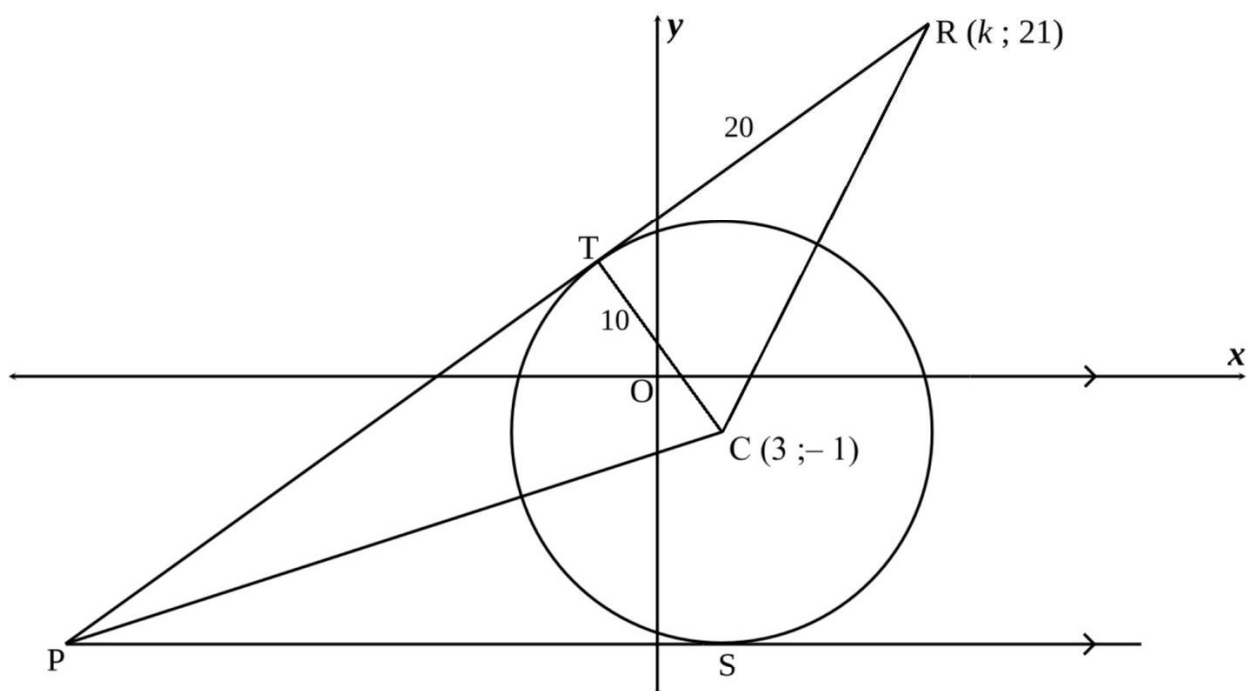
3.1	$M\left(\frac{x_2 + x_1}{2}; \frac{y_2 + y_1}{2}\right)$ $M\left(\frac{-5 - 3}{2}; \frac{2 + 8}{2}\right)$ $M(-4; 5)$ Answer only: full marks	A✓ Substitution of A and B into midpoint formula CA✓ answer	(2)
3.2	$D(-5; 0)$	A✓ answer	(1)
3.3	$\frac{-5 + x_C}{2} = 1 \qquad \frac{2 + y_C}{2} = 0$ $\therefore x_C = 7 \qquad y_C = -2$ $C(7; -2)$ OR $C(1 + 6; 0 - 2) \qquad \text{Using transformations}$ $C(7; -2)$	A✓ midpoint ITO x A✓ midpoint ITO y A✓ x-value A✓ y-value	(2)
3.4	$AC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $AC = \sqrt{(-5 - 7)^2 + (2 + 2)^2}$ $AC = 4\sqrt{10}$	A✓ substitute A and C into distance formula CA✓ answer	(2)

3.5	Method: translation $A \rightarrow B: (x; y) \rightarrow (x + 2; y + 6)$ $\therefore$ by symmetry: $C \rightarrow F: C(7; -2) \rightarrow F(7 + 2; -2 + 6)$ $\therefore F(9; 4)$ OR Midpoint of intersection of diagonals = $T(2; 3)$ Let coordinates of F be $(a; b)$ $\frac{a - 5}{2} = 2$ and $\frac{b + 2}{2} = 3$ $a = 9$ and $b = 4$ $\therefore F(9; 4)$	A✓ x-coordinate A✓ y-coordinate OR A✓ x-coordinate A✓ y-coordinate	(2) (2)
3.6	$m_{AB} = \frac{8 - 2}{-3 + 5} = 3$ $\therefore$ gradient of perpendicular bisector: $-\frac{1}{3}$ $\therefore y = -\frac{1}{3}x + c$ sub $(-4; 5)$: $5 = -\frac{1}{3}(-4) + c$ $c = \frac{11}{3}$ $\therefore$ equation of perpendicular bisector: $y = -\frac{1}{3}x + \frac{11}{3}$	A✓ $m_{AB} = 3$ CA✓ $m_{\text{perp bisector}} = -\frac{1}{3}$ CA✓ substitution CA✓ equation	(4)
3.7	$m_{AC} = \frac{2 + 2}{-5 - 7} = -\frac{1}{3}$ $\tan \alpha = -\frac{1}{3}$ $\alpha = \tan^{-1}\left(-\frac{1}{3}\right) + 180^\circ$ $\alpha = 161,57^\circ$ $\therefore \alpha \approx 162^\circ$ OR Accept method using Cosine Rule	A✓ m_{AC} CA✓ $\tan \alpha = -\frac{1}{3}$ CA✓ answer	(3)
3.8	$m_{AB} = 3$ $\therefore$ gradient of new line = 3 (// lines = gradients) $y = 3x + c$ sub $E(1; 0)$: $0 = 3(1) + c$ $= -3$ $y = 3x - 3$	CA✓ equal gradients CA✓ answer	(2)

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3.9	$m_{AB} \times m_{AC} = 3 \times -\frac{1}{3}$ $\therefore m_{AB} \times m_{AC} = -1$ $\therefore AB \perp AC$ $\therefore \theta = 90^\circ$ Accept methods using Cosine Rule & Trig ratios	A✓ $m_{AB} \times m_{AC} = -1$ A✓ answer	(2)
3.10	$AC = 4\sqrt{10}$ units $AB = \sqrt{(-3+5)^2 + (8-2)^2} = 2\sqrt{10}$ units $\therefore \text{Area of } \triangle ABC = \frac{1}{2} AC \cdot AB$ $\therefore \text{Area of } \triangle ABC = \frac{1}{2} (4\sqrt{10})(2\sqrt{10})$ $\therefore \text{Area of } \triangle ABC = 40 \text{ units}^2$	A✓ substitute A and B into distance formula CA✓ length of AB CA✓ substitution CA✓ answer	(4)
			[24]

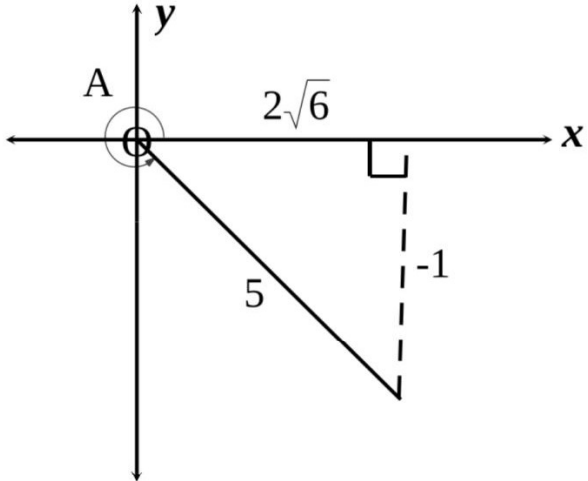
QUESTION 4

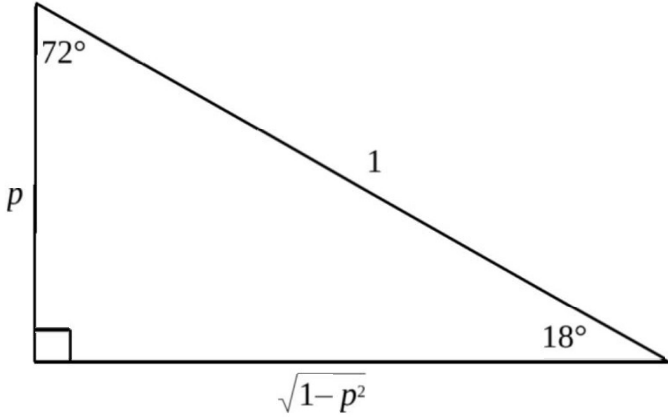


4.1	Radius is perpendicular to tangent	A✓	reason	(1)
4.2	$CR = \sqrt{10^2 + 20^2} = \sqrt{500}$ (pythag) $CR = \sqrt{(k-3)^2 + (21+1)^2} = \sqrt{(k-3)^2 + 484}$ $\therefore \sqrt{(k-3)^2 + 484} = \sqrt{500}$ $\therefore (k-3)^2 + 484 = 500$ $\therefore (k-3)^2 = 16$ $\therefore k-3 = \pm 4$ $\therefore k = -1$ or $k = 7$ but $k \neq -1$ (given that R is the first quadrant) $k = 7$ only	A✓	500	(4)
		A✓	equate	
		CA✓	simplification	
		CA✓	both values and rejection of $k = -1$	
4.3	$(x-3)^2 + (y+1)^2 = 100$	A✓	$(x-3)^2 + (y+1)^2$	(2)
		A✓	100	
4.4	$S(3; -11)$ $\therefore y = -11$	A✓	answer	(1)
4.5.1	$y = -11$ Eq 1 $3y = 4x + 35$ Eq 2 Sub Eq 1 into Eq 2: $3(-11) = 4x + 35$ $4x = -68$ $x = -17$ $\therefore P(-17; -11)$	CA✓	substitution	(2)
		CA✓	x – value	

4.5.2	$PC = \sqrt{(3+17)^2 + (-1+11)^2} = 10\sqrt{5}$ $TC = 10$ $PT^2 = PC^2 - TC^2 \quad (\text{pythag})$ $PT = \sqrt{(10\sqrt{5})^2 - (10)^2}$ $PT = 20 \text{ units}$ OR $PT = PS \quad (\text{tangents from common point})$ $PS = 3 - (-17) = 20 \text{ units}$ $\therefore PT = 20 \text{ units}$	$CA \checkmark \quad PC^2 = 500$ $PC = 10\sqrt{5}$ $CA \checkmark \quad \text{Pythagoras}$ $CA \checkmark \quad \text{answer}$ $A \checkmark \quad \text{S/R}$ $CA \checkmark \quad \text{Substitution}$ $CA \checkmark \quad \text{answer}$	(3)
[13]			

QUESTION 5

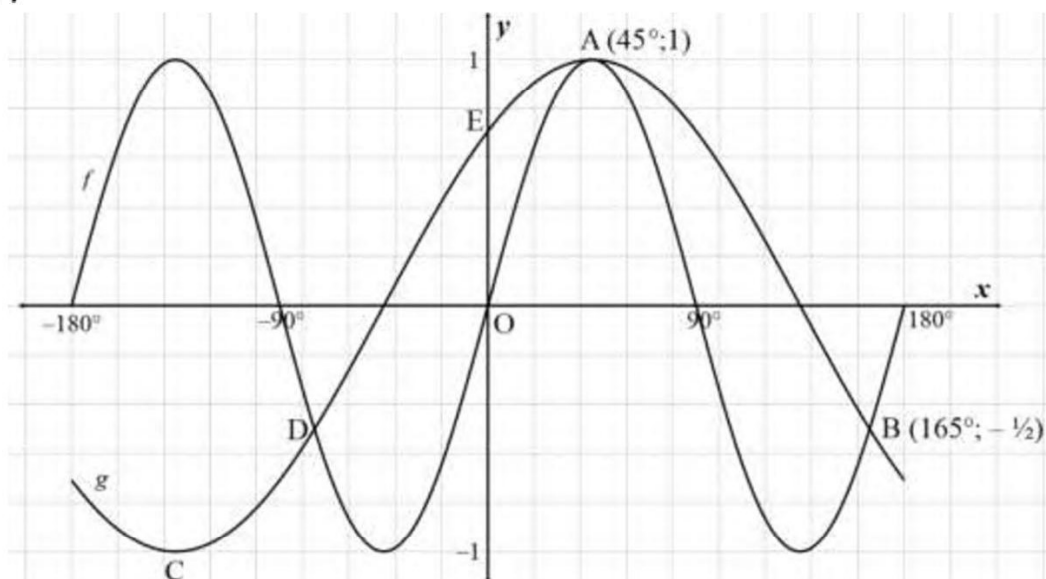
5.1.1	 $y = \sqrt{r^2 - x^2}$ $y = \sqrt{(5)^2 - (2\sqrt{6})^2} = 1$ $\therefore y = -1 \quad (\text{quadrant 4})$ $\therefore -\sqrt{6} \cdot \tan A$ $= -\sqrt{6} \times \left(\frac{-1}{2\sqrt{6}} \right)$ $= \frac{1}{2}$	$A \checkmark \quad \text{diagram}$ $A \checkmark \quad y = -1$ $CA \checkmark \quad \tan A = \frac{2\sqrt{6}}{-1}$ $CA \checkmark \quad \text{answer}$	(4)
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5.1.2	$\sin 2A = 2 \sin A \cdot \cos A$ $= 2 \left(\frac{-1}{5} \right) \left(\frac{2\sqrt{6}}{5} \right)$ $= -\frac{4\sqrt{6}}{25}$	A✓ double angle identity CA✓ $\sin A = \frac{-1}{5}$ CA✓ $\cos A = \frac{2\sqrt{6}}{5}$ CA✓ answer	(4)
5.2			
5.2.1	$\cos 18^\circ = \sqrt{1-p^2}$	A✓ diagram A✓ answer Answer only full marks	(2)
5.2.2	$\cos 48^\circ = \cos(30^\circ + 18^\circ)$ $= \cos 30^\circ \cos 18^\circ - \sin 30^\circ \sin 18^\circ$ $= \left(\frac{\sqrt{3}}{2} \right) \left(\frac{\sqrt{1-p^2}}{1} \right) - \left(\frac{1}{2} \right) \left(\frac{p}{1} \right)$ $= \frac{\sqrt{3} \cdot \sqrt{1-p^2} - p}{2}$ $= \frac{\sqrt{3-3p^2} - p}{2}$	A✓ $(30^\circ + 18^\circ)$ A✓ expansion A✓ special angle substitution CACA✓✓ substitution of $\sin 18^\circ$ and $\cos 18^\circ$	(5)
5.2.3	$\cos 18^\circ = 1 - 2 \sin^2 9^\circ$ $-2 \sin^2 9^\circ = \cos 18^\circ - 1$ $\sin^2 9^\circ = \frac{\cos 18^\circ - 1}{-2}$ $\sin 9^\circ = \sqrt{\frac{\cos 18^\circ - 1}{-2}}$ $\sin 9^\circ = \sqrt{\frac{\sqrt{1-p^2} - 1}{-2}} = \sqrt{\frac{1 - \sqrt{1-p^2}}{2}}$	A✓ double angle expansion A✓ making $\sin 9^\circ$ the subject CA✓ answer	(3)
			[18]

QUESTION 6

6.1	$\frac{\sin(180^\circ - x) \cdot \tan(x - 180^\circ) \cdot \cos(360^\circ + x)}{\sin^2(180^\circ + x) + \sin^2(90^\circ - x)}$ $= \frac{\sin x \cdot \tan x \cdot \cos x}{\sin^2 x + \cos^2 x}$ $= \sin x \cdot \frac{\sin x}{\cos x} \cdot \cos x$ $= \sin^2 x$	A✓ $\sin x$ A✓ $\tan x$ A✓ $\sin^2 x$ A✓ $\cos^2 x$ A✓ $\tan x = \frac{\sin x}{\cos x}$ CA✓ answer	(6)
6.2	$\frac{\cos 330^\circ \cdot \tan 150^\circ \cdot \sin 12^\circ}{\tan 675^\circ \cdot \cos 258^\circ}$ $= \frac{(\cos 30^\circ) \cdot (-\tan 30^\circ) \cdot (\sin 12^\circ)}{(-\tan 45^\circ) \cdot (-\cos 78^\circ)}$ $= -\frac{(\cos 30^\circ) \cdot (\tan 30^\circ) \cdot (\sin 12^\circ)}{(\tan 45^\circ) \cdot (\sin 12^\circ)}$ $= -\frac{\left(\frac{\sqrt{3}}{2}\right) \left(\frac{\sqrt{3}}{3}\right)}{1}$ $= -\frac{1}{2}$	A✓ $\cos 30^\circ$ A✓ $-\tan 30^\circ$ A✓ coratio A✓ $-\cos 78^\circ$ A✓ $\tan 45^\circ$ A✓ special angles CA✓ answer	(7)
6.3.1	LHS: $\frac{\cos \alpha + \cos 2\alpha}{\sin 2\alpha - \sin \alpha}$ $= \frac{\cos \alpha + (2\cos^2 \alpha - 1)}{(2\sin \alpha \cos \alpha) - \sin \alpha}$ $= \frac{2\cos^2 \alpha + \cos \alpha - 1}{2\sin \alpha \cos \alpha - \sin \alpha}$ $= \frac{(2\cos \alpha - 1)(\cos \alpha + 1)}{\sin \alpha (2\cos \alpha - 1)}$ $= \frac{(\cos \alpha + 1)}{\sin \alpha}$ $= \text{RHS}$	A✓ $\cos$ double angle A✓ $\sin$ double angle A✓ numerator factors A✓ denominator factors	(4)
6.3.2	$\sin 2\alpha - \sin \alpha = 0$ $2\sin \alpha \cos \alpha - \sin \alpha = 0$ $\sin \alpha (2\cos \alpha - 1) = 0$ $\therefore \sin \alpha = 0 \text{ or } 2\cos \alpha - 1 = 0$ $\cos \alpha = \frac{1}{2}$ $\alpha = 0^\circ + k \cdot 180; k \in \mathbb{Z}$ $\alpha = \pm 60^\circ + k \cdot 360; k \in \mathbb{Z}$ N.B. If $\sin \alpha = 0$ is solved only – max. 3/5 marks	A✓ equating to 0 A✓ factors CA✓ $0^\circ + k \cdot 180$ CA✓ $\pm 60^\circ + k \cdot 360$ A✓ $k \in \mathbb{Z}$	(5)
			[22]

QUESTION 7



7.1	$a = -45^\circ$	A✓	answer	(1)
7.2	180°	A✓	answer	(1)
7.3	$C(-135^\circ; -1)$ E: $y = \cos(0^\circ + 45^\circ)$ $y = \frac{\sqrt{2}}{2}$ $E\left(0; \frac{\sqrt{2}}{2}\right)$	A✓	$C(-135^\circ; -1)$	(3)
		A✓	solving for y	
		A✓	$E\left(0; \frac{\sqrt{2}}{2}\right)$	
7.4	Amplitude = 3	A✓	answer	(1)
7.5.1	$x \in [0^\circ; 165^\circ); x \neq 45^\circ$ OR $x \in [0^\circ; 45^\circ) \cup (45^\circ; 165^\circ)$ OR $0^\circ \leq x < 165^\circ; x \neq 45^\circ$	A✓	$[0^\circ; 165^\circ)$	(2)
		A✓	$x \neq 45^\circ$	
		A✓	critical values	
		A✓	notation	
		A✓	$0^\circ \leq x < 165^\circ$	
		A✓	$x \neq 45^\circ$	
7.5.2	$0^\circ \leq x \leq 135^\circ$	A✓	critical values	(2)
		A✓	notation	
7.6	$\sqrt{2} \sin 2x = \cos x + \sin x$ $\sin 2x = \frac{\cos x}{\sqrt{2}} + \frac{\sin x}{\sqrt{2}}$ $\sin 2x = \cos x \frac{1}{\sqrt{2}} + \sin x \frac{1}{\sqrt{2}}$ $\sin 2x = \cos x \cdot \cos 45^\circ + \sin x \cdot \sin 45^\circ$ $\sin 2x = \cos(x - 45^\circ)$	A✓	division of $\sqrt{2}$	
		A✓	identifying compound $\angle$ $\cos(x - 45^\circ)$	

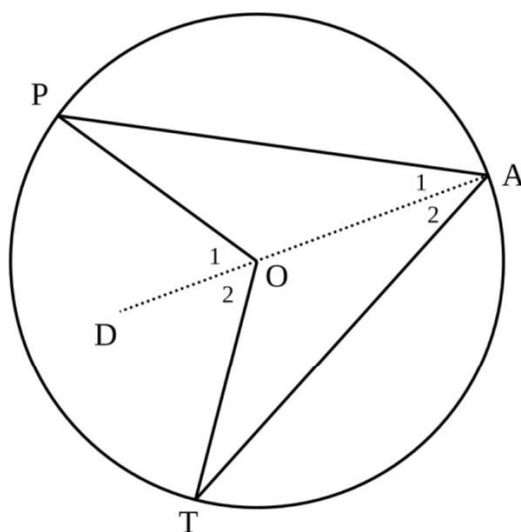
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	Equating the 2 functions gives the points of intersection of the 2 graphs.	A✓ conclusion	(3)
			[13]

QUESTION 8

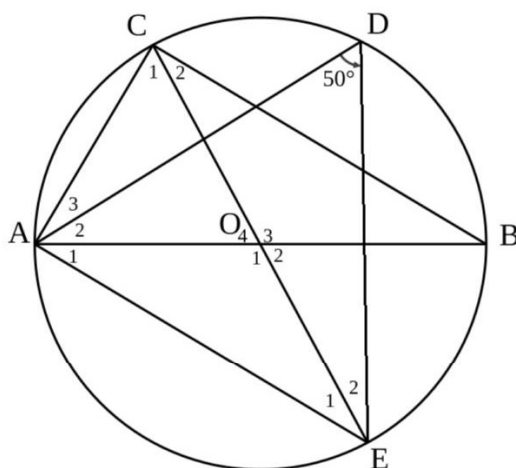
8.1	bisects the chord.	A✓ answer	(1)
8.2.1	AM = 4cm (line from centre $\perp$ chord)	A✓ S A✓R	(2)
8.2.2	$OM = (r - 2)$ $\therefore r^2 = (r - 2)^2 + 4^2$ (pythag) $r^2 = r^2 - 4r + 4 + 16$ $4r = 20$ $r = 5 \text{ cm}$	A✓ $OM = (r - 2)$ CA✓ $r^2 = (r - 2)^2 + 4^2$ CA✓ simplification CA✓ answer	(4)
			[7]

QUESTION 9



9.1	Constr: Draw line AO and extend to D. Proof: $OP = OT$ (radii) $\therefore \hat{A}_1 = \hat{P}$ ($\angle$ s opp = sides) but $\hat{O}_1 = \hat{A}_1 + \hat{P}$ (ext $\angle$ of Δ) $\therefore \hat{O}_1 = 2\hat{A}_1$ Similarly $\hat{O}_2 = 2\hat{A}_2$ $\therefore \hat{O}_1 + \hat{O}_2 = 2(\hat{A}_1 + \hat{A}_2)$ $\therefore \hat{POT} = 2\hat{PAT}$	A✓ construction A✓ S/R A✓ S/R A✓ S A✓ S	(5)
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9.2 Do not mark this question!!! (Maximum for Paper 2 – 141)

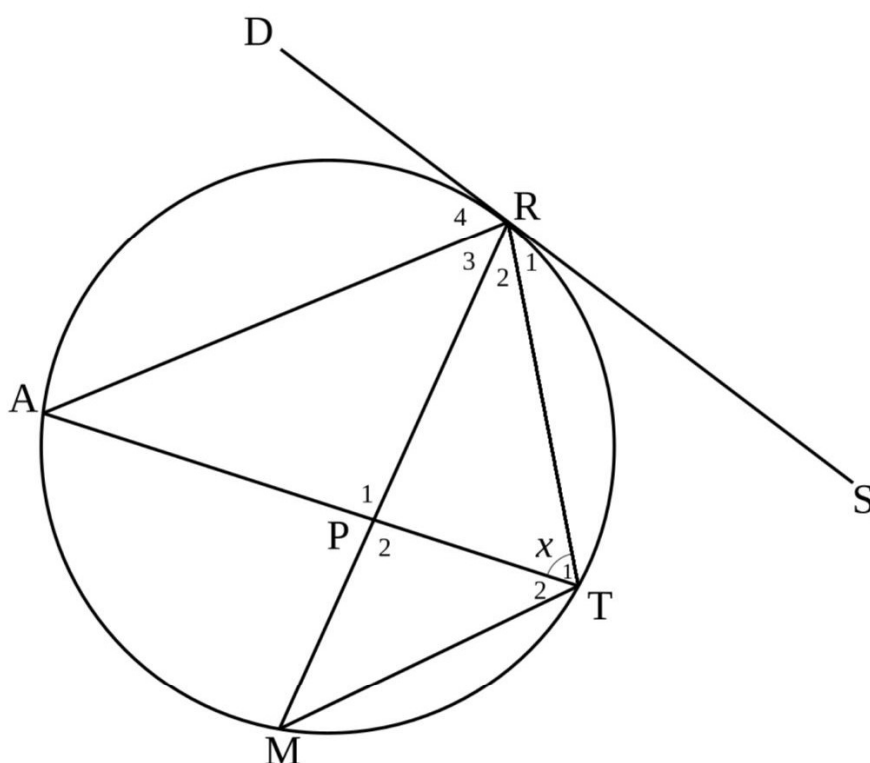


9.2.1a	$\hat{O}_1 = 100^\circ$ ($\angle$ at centre = $2 \times \angle$ at circ)	A✓	S	A✓R	(2)
9.2.1b	$\hat{O}_1 = 100^\circ$ $\hat{A}_1 = \hat{E}_1$ ($\angle$ s opp = radii) $\therefore \hat{E}_1 = \frac{180^\circ - 100^\circ}{2}$ (sum $\angle$ s Δ) $\therefore \hat{E}_1 = 40^\circ$	A✓	S	A✓R	(3)
9.2.2	$\hat{A}_1 = \hat{E}_1$ ($\angle$ s opp = radii) but $\hat{A}_1 = \hat{C}_2$ ($\angle$ s in same segment) $\therefore \hat{E}_1 = \hat{C}_2$ $\therefore AE \parallel CB$ (alt $\angle$ s =) OR $\hat{A}_1 = \hat{E}_1$ ($\angle$ s opp = radii) but $\hat{E}_1 = \hat{B}$ ($\angle$ s in same segment) $\therefore \hat{A}_1 = \hat{B}$ $\therefore AE \parallel CB$ (alt $\angle$ s =) OR	A✓ A✓ A✓ A✓ A✓ A✓ A✓ A✓	S/R S/R S R S/R S/R S R S/R S/R		(4)

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	$\hat{CAE} = 90^\circ$ ($\angle$ sin semi $\square$) $\hat{ACB} = 90^\circ$ ($\angle$ sin semi $\square$) $\hat{CAE} + \hat{ACB} = 180^\circ$ $\therefore AE \square CB$ (co - int $\angle$ s)	A✓ S A✓ R	(4)
			[14]

QUESTION 10

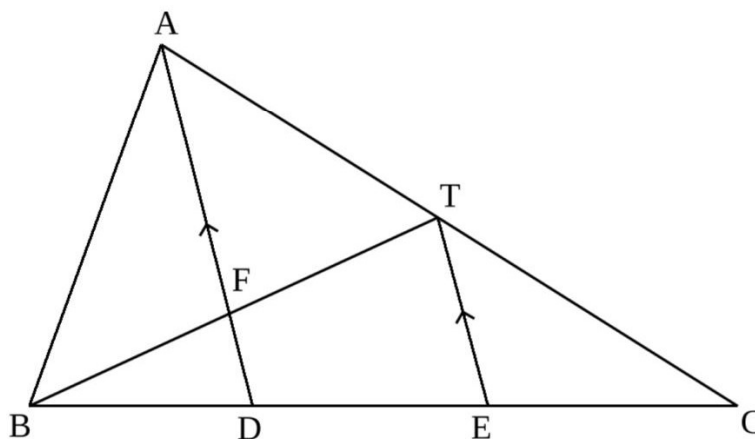


10.1.1	$\hat{R}_3 = \hat{T}_2$ ($\angle$ s in same segment) $\hat{R}_4 = \hat{T}_1$ (tan chord theorem) but $\hat{T}_1 = \hat{T}_2$ (given AT bisects $\widehat{MR}$) $\therefore \hat{R}_3 = \hat{R}_4$	A✓ S A✓R A✓ S A✓R	(4)
10.1.2	In $\triangle APR$ and $\triangle MPT$ 1. $\hat{A} = \hat{M}$ ($\angle$ sin same segment) 2. $\hat{P}_1 = \hat{P}_2$ (vert opp $\angle$ s) 3. $\hat{R}_3 = \hat{T}_2$ (remaining $\angle$ s $\triangle$) $\therefore \triangle APR \square \triangle MPT$ ($\angle \angle \angle$)	A✓ S/R A✓ S/R A✓ R	(3)

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10.2	$\frac{AR}{MT} = \frac{PR}{PT}$ $AR = \frac{3}{2}MT$ $\therefore \frac{AR}{MT} = \frac{3}{2}$ $\therefore \frac{PT}{PR} = \frac{2}{3}$	($\parallel \Delta s$) (given)	A✓ S A✓R	
			A✓ S	(3)
				[10]

QUESTION 11



11.1	$\frac{CE}{ED} = \frac{1}{2}$	A✓ S	(1)
11.2	$DE = \frac{2}{3}(9\text{cm}) = 6\text{cm}$	A✓ S	(1)
11.3	$\frac{TE}{2} = \frac{BE}{BD} = \frac{2}{1}$ ($\parallel \parallel$ triangles) $\therefore TE = 4\text{cm}$ Accept solution using the Midpoint theorem	A✓ S/R A✓ S	 (2)
11.4.1	$\frac{\text{Area of } \triangle ADC}{\text{Area of } \triangle ABD} = \frac{\frac{1}{2}DC \times h}{\frac{1}{2}BD \times h} = \frac{6\text{cm}}{6\text{cm}} = 1$	A✓ Areas A✓ Answer	(2)

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11.4.2	Area of $\triangle TEC$ Area of $\triangle ABC$ $= \frac{\text{Area of } \triangle TEC}{\text{Area } \triangle TBC} \times \frac{\text{Area of } \triangle TBC}{\text{Area } \triangle ABC}$ $= \frac{EC}{BC} \times \frac{TC}{AC}$ $= \frac{1}{4} \times \frac{1}{3}$ $= \frac{1}{12}$ OR Area of $\triangle TEC = \frac{1}{4}(\text{Area of } \triangle TBC)$ (common vertex=altit.) $= \frac{1}{4}\left(\frac{1}{3} \text{Area of } \triangle ABC\right)$ (common vertex=altit.) $\frac{\text{Area of } \triangle TEC}{\text{Area of } \triangle ABC} = \frac{1}{12}$ OR Accept area rule with the use of the angle of $\hat{C}$.	A✓ S A✓ S A✓ Answer A✓ S A✓ S A✓ S	(3) (3)
			[9]
TOTAL:			150