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**GRADE 12**

**MATHEMATICS PAPER 2**

**September 2018**

**MARKING GUIDELINES**

**MARKS: 150**

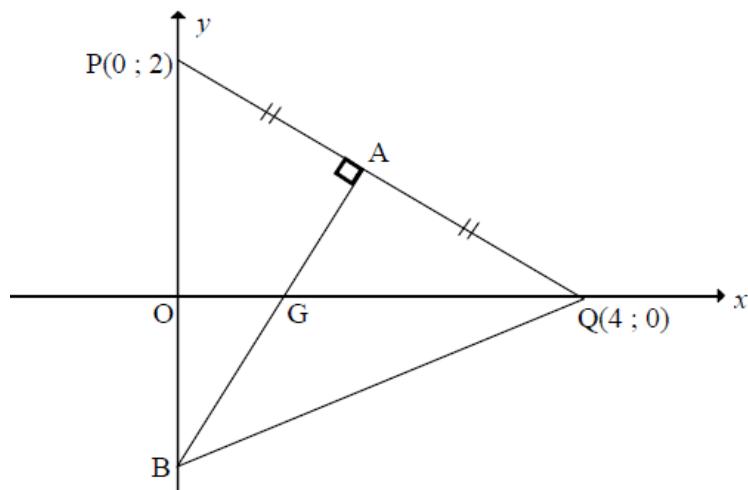
**This marking guideline consist of 20 pages**

**Question 1**

1.1	$\begin{aligned} \text{IQR} &= Q_3 - Q_1 \\ &= 20 - 11 \\ &= 9 \end{aligned}$	✓ $Q_3 - Q_1$ or ✓ $20 - 11$ ✓ 9 (2)
1.2		✓ min and max ✓ median ✓ upper and lower quartile (3)
1.3	Skewed to right or positively skewed	✓ answer (1)
		[6]

**Question 2**

2.1.1	<p>By using a calculator : <math>a = 29,22</math> (<math>29.21542\dots</math>)</p> $b = 0,89$ ( $0,886530\dots$ ) $\therefore$ equation of line of least squares is $y = 29.22 + 0.89x$	<ul style="list-style-type: none"> <li>✓ <math>a</math></li> <li>✓ <math>b</math></li> <li>✓ equation</li> </ul> (3)
2.1.2	$y = 29.22 + (0.89)(32)$ $= 57,7$ OR      57,58 <p>Therefore the employee who undergoes 32 hours of training should produce about 58 units.</p>	<ul style="list-style-type: none"> <li>✓ substitution</li> <li>✓ answer as integer</li> </ul> (2)
2.1.3	<p>Moderate OR not very strong</p> <p>Because the value of <math>r = 0.66</math></p>	<ul style="list-style-type: none"> <li>✓ moderate</li> <li>✓ reason</li> </ul> (2)
2.2.1	$\bar{x} = \frac{45 + 70 + 44 + 56 + 60 + 48 + 75 + 60 + 63 + 38}{10} = \frac{559}{10}$ $= 55.9$	<ul style="list-style-type: none"> <li>✓ sum</li> <li>✓ answer</li> </ul> (2)
2.2.2	$SD = 11.36$ $\bar{x} + SD$ $= 55.9 + 11.36$ $= 67.26$ $\therefore$ 2 employees	<ul style="list-style-type: none"> <li>✓✓ SD</li> <li>✓ 67.26</li> <li>✓ 2 employees</li> </ul> (4)
		[13]

**Question 3**

3.1	$m_{PQ} = \frac{2-0}{0-4}$ $= -\frac{1}{2}$	✓ answer (1)
3.2	$A\left(\frac{0+4}{2}; \frac{2+0}{2}\right)$ $A(2; 1)$	✓ $x_A$ ✓ $y_A$ (2)
3.3	$m_{AB} \cdot m_{PQ} = -1$ $m_{AB} \cdot \left(-\frac{1}{2}\right) = -1$ $m_{AB} = 2$ <p>Equation of AB is <math>y = 2x + c</math>  <math>\therefore 1 = 2(2) + c</math>  <math>c = -3</math></p> <p>Equation of AB is <math>y = 2x - 3</math></p> <p>OR</p>	✓ $m_{AB} = 2$  ✓ substitution of (2;1) and $m$  ✓ equation of AB (3)  ✓ $m_{AB} = 2$

	$m_{AB} \cdot m_{PQ} = -1$ $m_{AB} \cdot \left( \frac{-1}{2} \right) = -1$ $m_{AB} = 2$  $y - 1 = 2(x - 2)$ $y - 1 = 2x - 4$  Equation of AB is $y = 2x - 3$	✓ Substitution of (2;1)  ✓ equation of AB  (3)
3.4	B is the point (0 ; -3)  $BQ = \sqrt{(0 - 4)^2 + (-3 - 0)^2}$ $BQ = 5$  <b>OR</b>  $BQ^2 = 4^2 + 3^2$ (Pyth) $BQ = 5$	✓ substitution ✓ answer  ✓ substitution ✓ answer  (2)
3.5	If PBQR is a rhombus then A is the midpoint of BR.  Let the coordinates of R be $(x ; y)$  $\frac{x+0}{2} = 2$ AND $\frac{y-3}{2} = 1$ $x = 4$ $y = 5$ R(4 ; 5)  <b>OR</b>  RQ    PB so $x_R = 4$ $RQ = PB = 5$ , so $y_R = 5$ ∴ R(4 ; 5)	✓✓ x coordinate ✓✓ y coordinate  ✓✓ x coordinate ✓✓ y coordinate  (4)

3.6	$\tan A\hat{G}Q = 2$ $\therefore A\hat{G}Q = 63,43^\circ$  $m_{BQ} = \frac{-3 - 0}{0 - 4}$ $m_{BQ} = \frac{3}{4}$ $\therefore \tan \beta = \frac{3}{4}$ $\therefore \beta = 36,87^\circ$ $\therefore G\hat{Q}B = 36,87^\circ$ (vertically opp angles)  $63,43^\circ = 36,87^\circ + A\hat{B}Q$ (ext $\angle$ of $\Delta$ ) $\therefore A\hat{B}Q = 26,56^\circ$  <b>OR</b> $\tan A\hat{G}Q = 2$ $\therefore A\hat{G}Q = 63,43^\circ$ $\therefore B\hat{G}Q = 180^\circ - 63,43^\circ$ ( $\angle$ s on straight line) $= 116,57^\circ$  $m_{BQ} = \frac{-3 - 0}{0 - 4}$ $m_{BQ} = \frac{3}{4}$ $\therefore \tan \beta = \frac{3}{4}$ $\therefore \beta = 36,87^\circ$  $180 - 116,57^\circ - 36,87^\circ = A\hat{B}Q$ ( $\angle$ in $\Delta$ ) $\therefore A\hat{B}Q = 26,56^\circ$	✓ 63,43°  ✓ $m_{BQ}$  ✓ 36,87°  ✓ exterior angle of triangle ✓ answer (5)
3.7.1	$P\hat{A}B = 90^\circ$ $\therefore PB$ is the diameter (converse : $\angle$ at center = $2 \times \angle$ at circum)	✓ BQ is diameter

	<p>Midpoint PB <math>\left(0 ; -\frac{1}{2}\right)</math></p> $x^2 + \left(y + \frac{1}{2}\right)^2 = r^2$ <p style="text-align: center;">subst A(2 ; 1)</p> $\therefore (2)^2 + \left(1 + \frac{1}{2}\right)^2 = r^2$ $r = \frac{5}{2}$ $x^2 + \left(y + \frac{1}{2}\right)^2 = \frac{25}{4}$ <p style="text-align: center;"><b>OR</b></p> <p style="text-align: center;">subst B(0 ; -3)</p> $2^2 + \left(-3 + \frac{1}{2}\right)^2 = r^2$ $r^2 = \frac{25}{4}$ $x^2 + \left(y + \frac{1}{2}\right)^2 = \frac{25}{4}$ <p style="text-align: center;">subst B(0 ; 2)</p> $\left(2 + \frac{1}{2}\right)^2 = r^2$ $r^2 = \frac{25}{4}$ $x^2 + \left(y + \frac{1}{2}\right)^2 = \frac{25}{4}$	<p>✓✓ midpoint</p> <p>✓ substitution</p> <p>✓ <math>r = \frac{5}{2}</math></p> <p>✓ equation LHS</p> <p>✓ equation RHS</p> <p style="text-align: right;">(6)</p>
3.7.2	$y = 2$ ( $r \perp$ tangent)	✓✓ $y = 2$ (2)
		[25]

**Question 4**

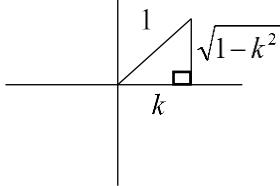
4.1.1	$x^2 + y^2 + 8x + 4y - 38 = 0$ $x^2 + 8x + 16 + y^2 + 4y + 4 = 38 + 16 + 4$ $(x + 4)^2 + (y + 2)^2 = 58$ $B(-4 ; -2)$	<p>✓ <math>(x + 4)^2 + (y + 2)^2</math></p> <p>✓ <math>r^2 = 58</math></p> <p>✓ <math>x_B</math></p> <p>✓ <math>y_B</math>      (4)</p>
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	<p>OR</p> $x_B = \frac{8}{-2} = -4$ $y_B = \frac{4}{-2} = -2$ $B(-4; -2)$	
4.1.2	<p>radius = <math>\sqrt{58}</math></p> <p>OR</p> $r = \sqrt{a^2 + b^2 - c}$ $r = \sqrt{16 + 4 + 38}$ $r = \sqrt{58}$	✓ radius (1)
4.2.1	<p>Centre of second circle is (4 ; 6)</p> <p>Distance between of AB:</p> $\sqrt{(4+4)^2 + (6+2)^2}$ $= \sqrt{128} \text{ OR } 11.31$	✓ centre ✓ substitution ✓ answer (3)
4.2.2	<p>Sum of radii = <math>\sqrt{58} + \sqrt{26} = 12.71</math></p> <p>Distance between centres is 11.31.</p> <p>sum of the radii &gt; distance between the centres</p> <p><math>\therefore</math> the circles must overlap and hence the circles must intersect.</p>	✓✓ sum of radii ✓ conclusion (3)
4.3	<p>AB <math>\perp</math> CD (line from centre <math>\perp</math> chord)</p> $m_{AB} = \frac{6+2}{4+4}$ $= \frac{8}{8}$ $= 1$ $\therefore m_{CD} = -1$ <p>OR</p>	✓S/R ✓subst ✓answer (3) ✓ S/R ✓ subst

	$AB \perp CD$ (line from centre $\perp$ chord) $m_{AB} = \frac{-2 - 6}{-4 - 4}$ $= \frac{-8}{-8}$ $= 1$ $\therefore m_{CD} = -1$	✓ answer (3)
		[14]

**Question 5**

5.1.1	0,76604 $\approx$ 0,77	✓✓ answer (2)
5.1.2	$\begin{aligned} & \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} \\ &= \frac{1 - \frac{\sin^2 \theta}{\cos^2 \theta}}{1 + \frac{\sin^2 \theta}{\cos^2 \theta}} \quad \text{OR} \quad \frac{\cos^2 \theta - \sin^2 \theta}{\cos^2 \theta + \sin^2 \theta} \\ &= \frac{\cos^2 \theta - \sin^2 \theta}{\cos^2 \theta + \sin^2 \theta} \\ &= \frac{\cos^2 \theta - \sin^2 \theta}{\cos^2 \theta} \times \frac{\cos^2 \theta}{\cos^2 \theta + \sin^2 \theta} \\ &= \cos^2 \theta - \sin^2 \theta \\ &= 2\cos^2 \theta - 1 \\ &= \cos 2\theta \end{aligned}$	✓ $\frac{\sin^2 \theta}{\cos^2 \theta}$ ✓ simplify ✓ $\cos^2 \theta + \sin^2 \theta = 1$ ✓ $\cos^2 \theta - \sin^2 \theta$ ✓ $2\cos^2 \theta - 1$ (5)
5.1.3	$\begin{aligned} & \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} = \frac{1}{2} \\ & \therefore \cos 2\theta = \frac{1}{2} \\ & \therefore \text{ref } \angle = 60^\circ \\ & 2\theta = 60^\circ + 360k; \quad k \in \mathbb{Z} \quad \text{or} \quad 2\theta = 300^\circ + 360k; \quad k \in \mathbb{Z} \\ & \theta = 30^\circ + 180k; \quad k \in \mathbb{Z} \quad \theta = 150^\circ + 180k, \quad k \in \mathbb{Z} \end{aligned}$	✓ $\cos 2\theta = \frac{1}{2}$ ✓ $60^\circ$ ✓ $300^\circ$ ✓ $30^\circ$ and $150^\circ$ ✓ $+180k; \quad k \in \mathbb{Z}$ (5)

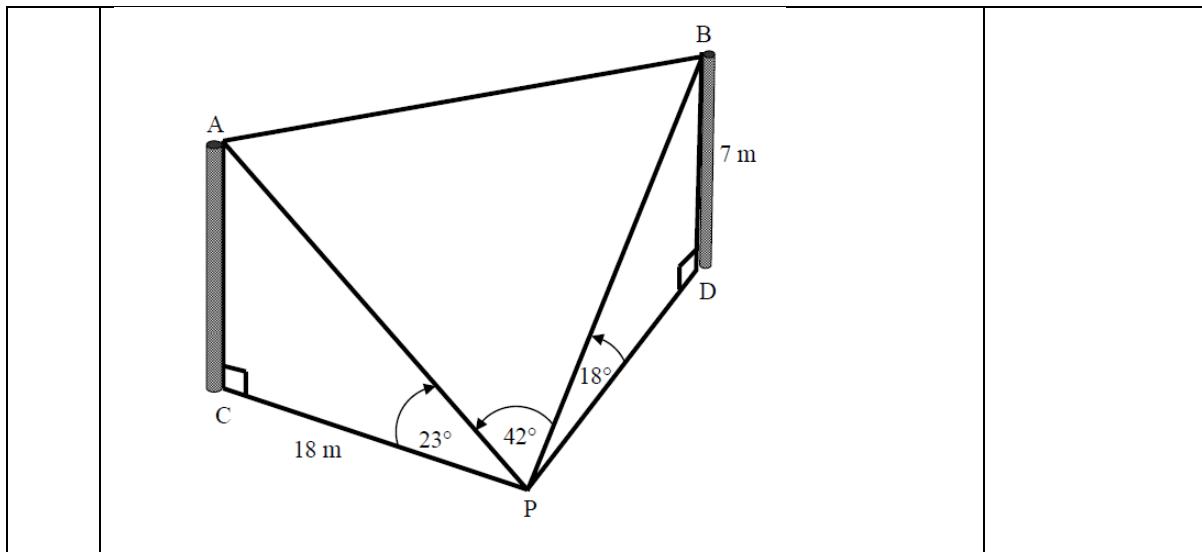
	<b>OR</b> $\frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} = \frac{1}{2}$ $\therefore \cos 2\theta = \frac{1}{2}$ $\therefore \text{ref } \angle = 60^\circ$ $2\theta = \pm 60^\circ + 360.k; k \in \mathbb{Z}$ $\theta = \pm 30^\circ + 180k. k \in \mathbb{Z}$	✓ $\cos 2\theta = \frac{1}{2}$ ✓ $60^\circ$ ✓ $-60^\circ$ ✓ $30^\circ$ and $-30^\circ$ ✓ $+180k; k \in \mathbb{Z}$ (5)
5.2.1	$\sin 245^\circ$ $= \sin(180^\circ + 65^\circ)$ $= -\sin 65^\circ$ $= -\cos 25^\circ$ $= -k$	✓ $-\sin 65^\circ$ ✓ $-\cos 25^\circ$ ✓ $-k$ (3)
5.2.2	$\sin 25^\circ$ $= \sqrt{1 - k^2}$  <b>OR</b> $\sin^2 25^\circ + \cos^2 25^\circ = 1$ $\sin^2 25^\circ = 1 - k^2$ $\sin 25^\circ = \sqrt{1 - k^2}$	 ✓ sketch ✓ answer (2)
5.2.3	$\cos 50^\circ$ $= 2\cos^2 25^\circ - 1$ $= 2k^2 - 1$  <b>OR</b> $\cos^2 25^\circ - \sin^2 25^\circ$ $= (k)^2 - (\sqrt{1 - k^2})^2$ $= k^2 - 1 + k^2$ $= 2k^2 - 1$  <b>OR</b> $1 - \sin^2 25^\circ$	✓ identity ✓ answer ✓ identity ✓ answer ✓ identity ✓ answer (2) (2) (2)

	$\begin{aligned} & 1 - 2(\sqrt{1-k^2})^2 \\ & = 1 - 2(1-k^2) \\ & = 1 - 2 + 2k^2 \\ & = 2k^2 - 1 \end{aligned}$	
5.2.3	$\begin{aligned} & \sin 25^\circ \\ & = \sqrt{1-k^2} \end{aligned}$	<p style="text-align: right;">✓ Sketch ✓ answer (2)</p>
5.3.1	$\begin{aligned} & \sqrt{3} \cos \beta + \sin \beta \\ & = 2 \cdot \frac{\sqrt{3}}{2} \cdot \cos \beta + \frac{1}{2} \cdot \sin \beta \\ & = 2 \left( \frac{\sqrt{3}}{2} \cdot \cos \beta + \frac{1}{2} \cdot \sin \beta \right) \\ & = 2(\sin 60^\circ \cdot \cos \beta + \cos 60^\circ \cdot \sin \beta) \\ & = 2 \sin(60^\circ + \beta) \end{aligned}$	<p style="text-align: right;">✓ <math>\times \frac{2}{2}</math> ✓ <math>2 \left( \frac{\sqrt{3}}{2} \cdot \cos \beta + \frac{1}{2} \cdot \sin \beta \right)</math> ✓ <math>\sin 60^\circ</math> ✓ <math>\cos 60^\circ</math> ✓ <math>2 \sin(60^\circ + \beta)</math> (5)</p>
5.3.2	$\begin{aligned} \text{Max - value} &= 2 - 5 \\ &= -3 \end{aligned}$	<p style="text-align: right;">✓✓ answer (2)</p>
		<b>[26]</b>

**Question 6**

6.1		$f(x)$ ✓ shape ✓ x-intercepts ✓ y-intercepts ✓ turning point (4)
6.2	$\begin{aligned} g(2x) &= -\cos 2x \\ \therefore \text{period} &= 180^\circ \end{aligned}$	✓ $g(2x) = -\cos 2x$ ✓ answer (2)

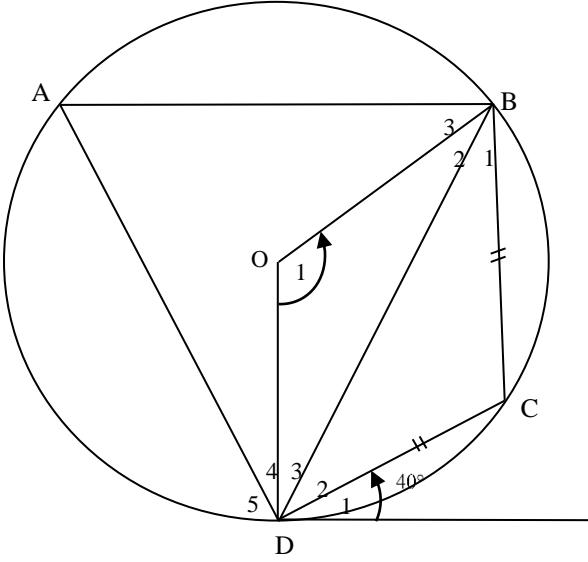
6.3	$0^\circ < x < 60^\circ$ <b>OR</b> $x \in (0^\circ; 60^\circ)$	✓ notation ✓ end points (2)
		[8]

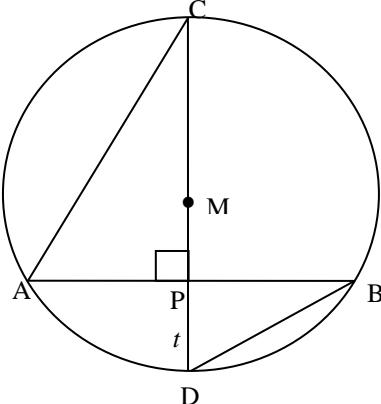
**Question 7**

7.1	$\frac{18}{PA} = \cos 23^\circ$ $PA = \frac{18}{\cos 23^\circ}$ $PA = 19.55\text{m}$ <b>OR</b> $\frac{AP}{\sin C} = \frac{CP}{\sin A}$ $\frac{AP}{\sin 90^\circ} = \frac{18}{\sin 67^\circ}$ $AP = \frac{18 \sin 90^\circ}{\sin 67^\circ}$ $AP = 19.55\text{m}$	✓ Ratio ✓ answer ✓ Ratio ✓ answer (2)
7.2	$AB^2 = (22.65)^2 + (19.55)^2 - (2)(22.62)(19.55) \cdot \cos 42^\circ$ $AB^2 = 237.084\dots$ $AB = 15.40\text{m}$	✓ Use of cosine rule ✓ substitution ✓ 237.0847

		✓ answer (4)
		[6]

**Question 8**

8.1		
8.1.1	$\hat{D}_1 = \hat{B}_1 = 40^\circ$ (tangent - chord theorem) $\therefore \hat{D}_2 = \hat{B}_1 = 40^\circ$ ( $\angle$ 's opp= sides)	✓S ✓R ✓S/R (3)
8.1.2	$\hat{C} = 180^\circ - (40^\circ + 40^\circ)$ ( $\angle$ s in $\Delta$ ) $= 100^\circ$	✓S ✓S (2)
8.1.3	$\hat{A} = 180^\circ - 100^\circ$ (Opposite angles of a cyclic quad) $= 80^\circ$	✓R ✓S (2)
8.1.4	$\hat{O}_1 = 2\hat{A}$ ( $\angle$ at centre = $2 \times \angle$ at circum) $\hat{O}_1 = 160^\circ$ <b>OR</b>	✓R ✓S (2)  ✓R

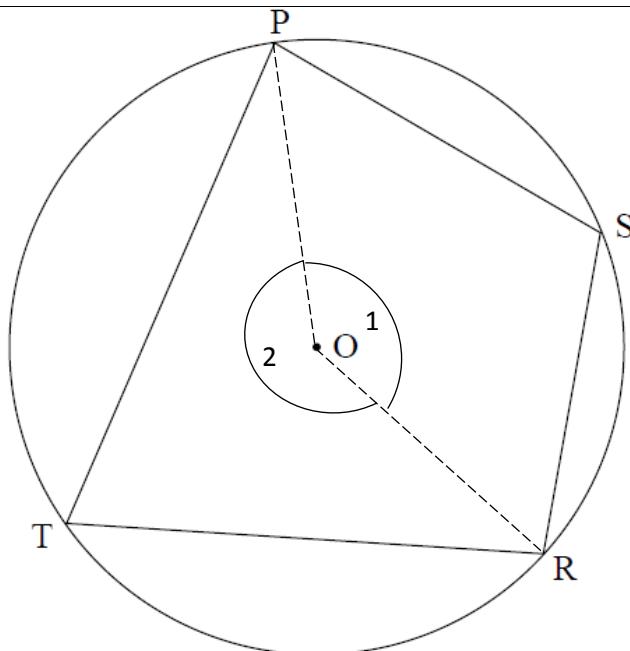
	$\hat{D}_2 = \hat{B}_1 = 40^\circ$ (From 9.1) $\hat{D}_3 = 90^\circ - 40^\circ - 40^\circ$ ( $\tan \perp$ rad) $\hat{D}_3 = 10^\circ$ $\therefore \hat{O}_1 = 180^\circ - 10^\circ - 10^\circ$ (sum of angles in $\Delta$ ) $\hat{O}_1 = 160^\circ$	✓S (2)
8.2		
8.2.1	Line from centre $\perp$ to chord	✓R (1)
8.2.2	$\Delta CAP \parallel \Delta BDP$	
(a)	$\frac{AP}{DP} = \frac{CP}{BP}$ (sides in proportion) $\frac{2t}{t} = \frac{15}{2t}$ $4t^2 = 15t$ $4t^2 - 15t = 0$ $2t(2t - 7.5) = 0$ $\therefore t \neq 0 \quad or \quad t = \frac{15}{4}$	✓S ✓S ✓S ✓S ✓answer (4)
		✓S

	<b>OR</b> $15 + t = 2r$ $\therefore r = \frac{15 + t}{2}$ <p>In <math>\Delta MPB</math>:</p> $\left(\frac{15+t}{2}\right)^2 = (2t)^2 + \left(\frac{15+t}{2} - t\right)^2$ $\frac{225 + 30t + t^2}{4} = 4t^2 + \left(\frac{15-t}{2}\right)^2$ $\frac{225 + 30t + t^2}{4} = 4t^2 + \frac{225 - 30t + t^2}{4}$ $225 + 30t + t^2 = 16t^2 + 225 - 30t + t^2$ $16t^2 - 60t = 0$ $4t(4t - 15) = 0$ $t = \frac{15}{4}$	$\checkmark S$ $\checkmark S$ $\checkmark$ answer (4)
	<b>OR</b> $15 + t = 2r$ $t = 2r - 15$ <p>In <math>\Delta MPB</math>:</p> $\left(\frac{15+2r-15}{2}\right)^2 = (2(2r-15))^2 + \left(\frac{15+2r-15}{2} - (2r-15)\right)^2$ $r^2 = 4(4r^2 - 60r + 225) + (r - 2r + 15)^2$ $r^2 = 16r^2 - 240r + 900 + (-r + 15)^2$ $r^2 = 16r^2 - 240r + 900 + r^2 - 30r + 225$ $0 = 16r^2 - 270r + 1125$ $0 = (2r - 15)(8r - 75)$ $\therefore r \neq \frac{15}{2} \quad \text{or} \quad r = \frac{75}{8}$ $\therefore r = \frac{15}{4}$	$\checkmark S$ $\checkmark S$ $\checkmark$ answer (4)
8.2.2 (b)	$\text{Radius} = \frac{15 + \frac{15}{4}}{2}$ $= 9.375 \text{ OR } 9\frac{3}{8}$	$\checkmark$ method $\checkmark$ answer (2)

		[16]
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**Question 9**

9.1



Join PO and OR

✓  
constructionLet  $\hat{O}_1 = 2x$ 

✓ S ✓ R

 $\hat{T} = x$  ( $\angle$  at circ centre = 2  $\angle$  at circumference) $\hat{O}_2 = 360^\circ - 2x$  ( $\angle$ s round a point)

✓ S

 $\hat{S} = 180 - x$  ( $\angle$  at circ centre = 2  $\angle$  at circumference)

✓ S

 $\hat{T} + \hat{S} = 180^\circ - x + x$ 

✓ S

 $\hat{T} + \hat{S} = 180^\circ$ 

(5)

 $\therefore \hat{PTR} + \hat{PSR} = 180^\circ$ 

9.2

9.2.1	$\hat{R}_1 = x$ ( $\angle$ 's opp= radii) $\hat{O}_1 = 180^\circ - 2x$ ( $\angle$ sum in $\Delta QRT$ ) $\hat{P}_1 = 90^\circ - x$ ( $\angle$ circle centre = twice at circum)	$\checkmark S /R$ $\checkmark S$ $\checkmark S \checkmark R$ (4)
9.2.2	$PQ = QR$ (given) $\hat{Q}RP = 90^\circ - x$ ( $\angle$ opp=sides in $\Delta$ ) $\hat{PQR} = 2x$ ( $\angle$ sum in $\Delta PQR$ ) $x + \hat{Q}_2 = 2x$ $\hat{Q}_2 = x$ TQ bisects $\hat{PQR}$	$\checkmark S$ $\checkmark S$ $\checkmark S$ $\checkmark S$ (3)
9.2.3	$\hat{PQR} = 2x$ $\hat{S} = 180^\circ - 2x$ (opp $\angle$ 's of cyclic quad are suppl) $\hat{O}_1 = 180^\circ - 2x$ (FROM 10.2.1) STOR is a cyclic quad (converse – of ext $\angle$ of cyclic quad or ext $\angle$ of quad = int opp $\angle$ )  OR $\hat{PQR} = 2x$ $\hat{S} = 180^\circ - 2x$ (opp $\angle$ 's of cyclic quad are suppl) $\hat{O}_1 = 180^\circ - 2x$ (from 10.2.1) $\hat{O}_2 = 2x$ ( $\angle$ s on str. line) $\hat{S} + \hat{O}_2 = 180^\circ - 2x + 2x$ $\therefore \hat{S} + \hat{O}_2 = 180^\circ$ STOR is a cyclic quad (convse : opp $\angle$ 's are supplementary)	$\checkmark S$ $\checkmark S \checkmark R$ $\checkmark S$ $\checkmark R$ (5) $\checkmark S$ $\checkmark S \checkmark R$ $\checkmark S$ $\checkmark S$ $\checkmark R$ (5)
		[17]

**Question 10**

10.1	$\hat{Q}_3 = \hat{R}_1 = x$ (ext angle of cyclic quad...) and (RA bisects $\hat{R}$ ) $\hat{R}_2 = \hat{Q}_2 = x$ (angles in the same segment) $\hat{R}_1 = \hat{R}_2$ $\therefore \hat{Q}_2 = \hat{Q}_3$ <b>OR</b> $\hat{Q}_2 + \hat{Q}_3 = \hat{R}_1 + \hat{R}_2$ (ext $\angle$ of cyclic quad) But $\hat{Q}_2 = \hat{R}_2$ ( $\angle$ s in same segment) $\hat{R}_1 = \hat{R}_2$ $\therefore \hat{Q}_3 = \hat{Q}_2$	✓S ✓R ✓S ✓R ✓S (5)
10.2	$\hat{Q}_3 = \hat{B} = x$ ( $\angle$ s opp=sides, $AQ = AB$ ) $\hat{Q}_3 = \hat{R}_1 = \hat{B} = x$ (from 1.1) $\therefore TR = TB$ (sides opp = $\angle$ s)	✓ S/R ✓R (2)
10.3	$\hat{P} = \hat{A}_1$ ( $\angle$ s in same segment) $\hat{A}_1 = \hat{Q}_3 + B$ (ext $\angle$ of $\Delta ABC$ ) $\hat{Q}_3 + \hat{B} = 2\hat{Q}_3$ ( $\hat{Q}_3 = \hat{B}$ $\angle$ s opp = sides) $2\hat{Q}_3 = 2\hat{R}_1$ (from 11.2) $\therefore 2\hat{R}_1 = P\hat{R}T$ $\therefore \hat{P} = T\hat{R}P$	✓S ✓R ✓S/R (3)

	<b>OR</b>  $T\hat{R}P = 2x$ $\hat{A}_1 = \hat{Q}_3 + B = 2x$ (ext $\angle$ of $\triangle ABC$ ) $\hat{P} = \hat{A}_1 = 2x$ ( $\angle$ s in same segment) $= T\hat{R}P$	✓ S ✓ R ✓S/R (3)
		[10]

**Question 11**

11.1	<p>In <math>\triangle BPE</math> and <math>\triangle BDA</math></p> <ol style="list-style-type: none"> <li>1. <math>\hat{B}_1 = \hat{B}_1</math> common</li> <li>2. <math>\hat{P}_2 = \hat{D} = 90^\circ</math> <math>\angle</math> in semi-circle</li> <li>3. <math>\hat{B}\hat{A}\hat{D} = \hat{E}_3</math> <math>\angle</math> in <math>\Delta</math>s</li> </ol> <p><math>\therefore \triangle BPE \equiv \triangle BDA</math> (equiangular OR <math>\angle\angle\angle</math>)</p>	✓S ✓S ✓R ✓R (4)
11.2	$\frac{BP}{BD} = \frac{BE}{AB} \quad \text{From Q11.1}$ $AB = \frac{BD \cdot BE}{BP}$ $AB^2 = \frac{BD^2 \cdot BE^2}{BP^2}$ <p>In <math>\triangle BPE</math>;</p> $BE^2 = BP^2 + PE^2 \quad (\text{pyth})$ $AB^2 = \frac{BD^2 \cdot (BP^2 + PE^2)}{BP^2}$ $AB^2 = \frac{BD^2 \cdot BP^2}{BP^2} + \frac{BD^2 \cdot PE^2}{BP^2}$ $AB^2 = BD^2 + \frac{BD^2 \cdot PE^2}{BP^2}$	✓ S/ratio ✓S ✓S ✓ BE <sup>2</sup> = BP <sup>2</sup> + PE <sup>2</sup> ✓ substitution ✓ simplification (6)
		[10]
	<b>TOTAL 150</b>	