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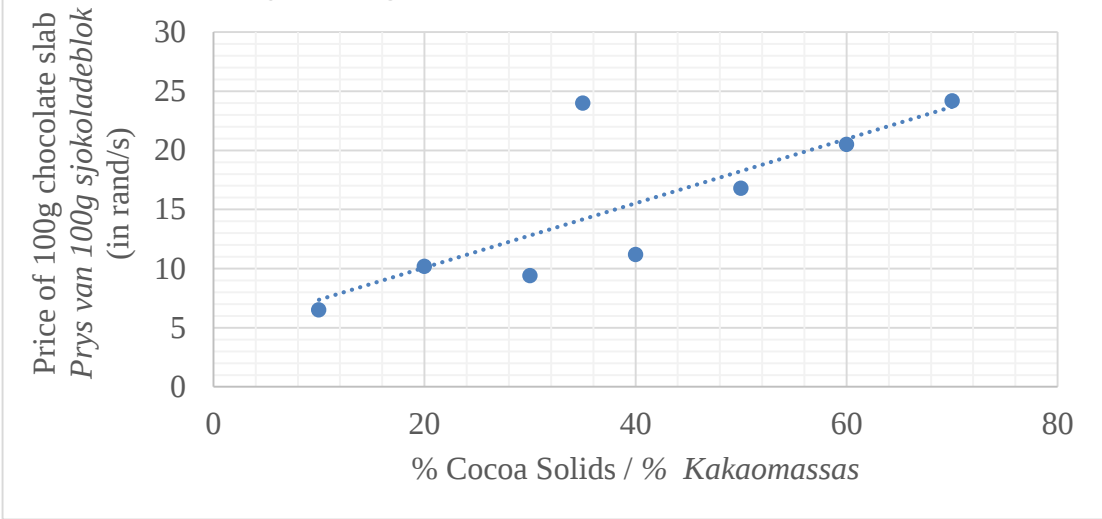
SEPTEMBER 2019

**MATHEMATICS P2/WISKUNDE V2
MARKING GUIDELINE/NASIENRIGLYN**

MARKS/PUNTE: 150

This marking guideline consists of 16 pages./
Hierdie nasienriglyn bestaan uit 16 bladsye.

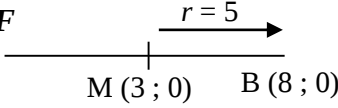
QUESTION 1/VRAAG 1			
1.1	$\bar{x} = \frac{420,8}{80}$ $= 5,26$ Answer only: Full marks <i>Slegs antwoord: Volpunte</i>	$\checkmark \frac{420,8}{80}$ $\checkmark \text{ answer / antwoord}$	(2)
1.2	total of heights / <i>totaal van hoogtes</i> $= 4,86 \times 7 = 34,02$ Error/ <i>fout</i> = $4,98 - 4,89 = 0,09$ new total of heights / <i>nuwe totaal van hoogtes</i> $= 33,93$ new mean / <i>nuwe gemiddelde</i> = $\frac{33,93}{7} = 4,85 \text{ m}$	$\checkmark \text{ error / fout} = 0,09$ $\checkmark \text{ new total / nuwe totaal}$ $\checkmark \text{ answer / antwoord}$	(3)
1.3	Standard deviation of individual heights of the 80 giraffes would be bigger than that of 7 males. There is a bigger spread of heights among population of juveniles and adults and babies. <i>Standaardafwyking van individuele hoogtes van 80 kameelperde sal groter wees as die van die 7 manlike kameelperde.</i> <i>Daar is 'n groter verspreiding van hoogtes onder die jeugdige en volwasse en baba bevolking.</i>	$\checkmark \text{ bigger/larger standard deviation}$ <i>groter standaardafwyking</i> $\checkmark \text{ bigger spread of heights}$ <i>groter verspreiding van hoogtes</i>	(2)
			[7]

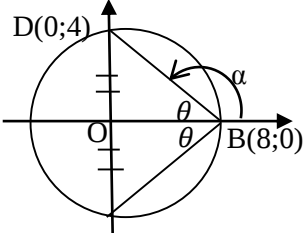
QUESTION 2/VRAAG 2			
2.1	Price of chocolate vs % of cocoa solids Prys van sjokolade vs % van kakaomassas  ✓✓ all points plotted correctly alle punte korrek afgesteek		
2.2	$\hat{y} = a + bx$ $a = 4,64 \quad b = 0,27$ $\hat{y} = 4,64 + 0,27x$	✓ value of/waarde van a ✓ value of/waarde van b ✓ equation / vergelyking	(2)
2.3	See line in 2.1 / Sien lyn in 2.1	✓ correct gradient / korrekte gradiënt ✓ correct line / korrekte lyn	(2)
2.4	$r = 0,78$	✓ $r = 0,78$	(1)
2.5	fairly strong positive correlation in the % of cocoa and the price. redelike sterk positiewe korrelasie tussen die % van kakao en die prys.	✓ correct description of r korrek beskrywing van r	(1)
2.6.1	Brand D / Handelsmerk D OR / OF (35 ; 24)	✓ answer / antwoord	(1)
2.6.2	$\hat{y} = 4,64 + 0,27(35)$ = R14,09 Overpriced by/Te duur: $R24,00 - R14,09 = R9,91$	✓ substitution of 35 vervanging van 35 ✓ R14,09 ✓ R9,91	(3)
			[13]

QUESTION 3 / VRAAG 3			
3.1	D (4 ; 0)	✓ answer / <i>antwoord</i>	(1)
3.2	$m_{DE} = \frac{-\frac{4}{3} - 0}{0 - 4}$ $= -\frac{4}{3} \times \left(-\frac{1}{4} \right)$ $= \frac{1}{3}$	✓ substitution / <i>vervanging</i> ✓ answer / <i>antwoord</i>	(2)
3.3	Angle of inclination of DE / <i>Inklynasiehoek van DE</i> $= \tan^{-1} \frac{1}{3}$ $= 18,43^\circ$ $\hat{ODE} = 18,43^\circ \quad (\text{vert. opp. } \angle s) / (\text{regoorst. } \angle e)$ $\hat{OED} = 71,57^\circ \quad (\text{complementary } \angle s)$ $\quad (\text{komplementêre } \angle e)$ $\therefore \hat{PRB} = 71,57^\circ \quad (\text{corr. } \angle s : DE \parallel BC)$ $\quad (\text{ooreenk. } \angle e : DE \parallel BC)$	✓ $\tan^{-1} \frac{1}{3}$ ✓ $18,43^\circ$ ✓ answer / <i>antwoord</i> ✓ reason / <i>rede</i>	(4)
3.4	$DE = \sqrt{(4-0)^2 + \left(0 + \frac{4}{3}\right)^2}$ $= \frac{4\sqrt{10}}{3}$	✓ substitution / <i>vervanging</i> ✓ answer / <i>antwoord</i>	(2)
3.5	$\frac{AD}{AB} = \frac{3}{9} = \frac{1}{3}$	✓ ratios / <i>verhoudings</i> ✓ simplified answer / <i>vereenvoudigde antwoord</i>	(2)

3.6	$\triangle ABC \parallel \triangle ADE$ $\therefore \frac{AD}{AB} = \frac{DE}{BC} = \frac{1}{3}$ $BC = 3DE$ $= 3 \left(\frac{4\sqrt{10}}{3} \right)$ $\therefore BC = 4\sqrt{10}$ OR/OF equation of BC / <i>vergelyking van BC</i> $y - 6 = \frac{1}{3}(x - 4)$ $\therefore y = \frac{1}{3}x + \frac{14}{3}$ $m_{AC} = \frac{\frac{5}{3}}{-4} = -\frac{5}{12}$ equation of AC / <i>vergelyking van AC</i> $y = -\frac{5}{12}x - \frac{4}{3}$ $\therefore \frac{1}{3}x + \frac{14}{3} = -\frac{5}{12}x - \frac{4}{3}$ $4x + 56 = -5x - 16$ $9x = -72$ $\therefore x = -8$ $y = \frac{1}{3}(-8) + \frac{14}{3}$ $\therefore y = 2$ $C(-8; 2) \text{ and/en } B(4; 6)$ $\therefore BC = \sqrt{(-8 - 4)^2 + (2 - 6)^2} = 4\sqrt{10}$	$\checkmark$ ratio of corresponding sides <i>verhouding van ooreenstemmende sye</i> $\checkmark$ isolating / isoleer BC $\checkmark$ substitution / <i>vervang</i> OR/OF $\checkmark$ equation of BC / <i>vergelyking van BC</i> $\checkmark$ equation of AC / <i>vergelyking van AC</i> $\checkmark$ answer / <i>antwoord</i>	(3)
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3.7.1	Midpoint of DE / <i>Middelpunt van DE</i> $\left(\frac{4+0}{2}, \frac{0-\frac{4}{3}}{2} \right)$ $\left(2; -\frac{2}{3} \right)$	✓✓ coordinates / <i>koördinate</i>	(2)
3.7.2	$m_{\text{bisector}}/m_{\text{halveerlyn}} = -3$ Equation of bisector / <i>Vergelyking van halveerlyn</i> $y + \frac{2}{3} = -3(x - 2)$ $\therefore y = -3x + \frac{16}{3}$	✓ gradient of bisector / <i>gradiënt van halveerlyn</i> ✓ substitution / <i>vervanging</i> ✓ equation / <i>vergelyking</i>	(3)
3.8	LHS/LK = -3 RHS/RK = $-3(4) + \frac{16}{3}$ $= -\frac{20}{3} = -6\frac{2}{3} \approx -6,66$ LHS/LK $\neq$ RHS/RK No, bisector does not pass through A. / <i>Nee, die halveerlyn gaan nie deur A nie</i>	✓ substitution / <i>vervanging</i> ✓ conclusion / <i>gevolgtrekking</i>	(2)
			[21]

QUESTION 4/VRAAG 4			
4.1	$x^2 - 6x + y^2 = 16$ $(x - 3)^2 + (y - 0)^2 = 16 + 9$ $(x - 3)^2 + (y - 0)^2 = 25$ Hence centre / Gevolglik middelpunt (3 ; 0) Radius/Radius = $\sqrt{25} = 5$	✓ completing the square <i>voltooing van vierkant</i> ✓ final form / finale vorm ✓ taking square root / <i>vierkantswortel</i>	(3)
4.2.1	$y = 0$: hence/gevolglik $(x - 3)^2 = 25$ $x - 3 = \pm 5$ $x = 3 \pm 5$ B (8 ; 0) OR / OF 	✓ equating / stel $y = 0$ ✓ solving for x / Los op vir x ✓ coordinates of B <i>koördinate van B</i> OR / OF ✓✓✓ use of horizontal distance / gebruik van <i>horisontale afstand</i>	(3)
4.2.2	$x = 0$: then/dan $(-3)^2 + y^2 = 25$ $9 + y^2 = 25$ $y^2 = 16$ $y = \pm 4$ C(0 ; - 4) OR/OF using Pythagoras / gebruik van Pythagoras : $MD^2 = OM^2 + OD^2$ $5^2 = 3^2 + OD^2$ $4 = OD = OC$ C(0 ; - 4)	✓ equating x to 0 <i>stel x gelyk aan 0</i> ✓ coordinates of C <i>koördinate van C</i> OR/OF ✓ use of Pythagoras <i>gebruik van Pythagoras</i> ✓ coordinates of C <i>koördinate van C</i>	(2)
4.3	$\widehat{MCP} = 90^\circ$ $PM^2 = MC^2 + PC^2$ $(8\frac{1}{3})^2 = 5^2 + PC^2$ $PC = \sqrt{\frac{400}{9}} = \frac{20}{3} = 6,67$ OR / OF $\widehat{POC} = 90^\circ$ $PC^2 = PO^2 + OC^2$ $PO = 8\frac{1}{3} - 5 + 2 = \frac{16}{3}$ and/en $OC = 4$ $PC^2 = (\frac{16}{3})^2 + 4^2$ $PC = \sqrt{\frac{400}{9}} = \frac{20}{3} = 6,67$	✓ radius $\perp$ tangent <i>radius $\perp$ raaklyn</i> ✓ substitution into Pythag. <i>Thm vervanging in Stelling van Pyth</i> ✓ answer / antwoord OR/OF ✓ calculation of PO <i>berekening van PO</i> ✓ substitution into Pythag. <i>Thm vervanging in Stelling van Pyth</i> ✓ answer / antwoord	(3)

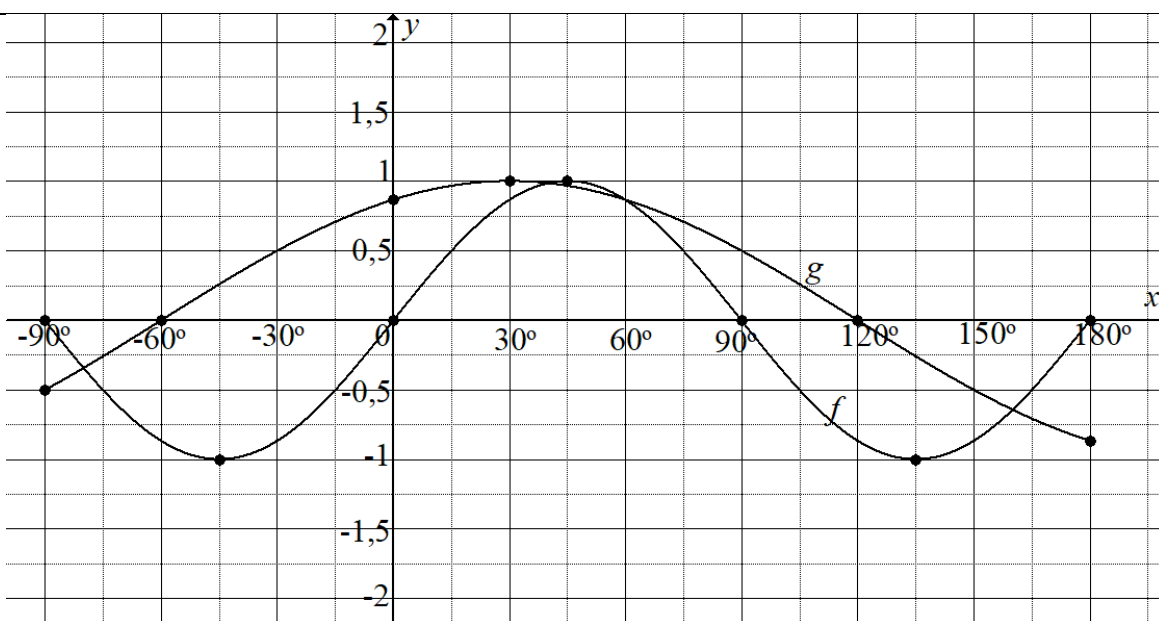
4.4	 $m_{BD} = -\frac{1}{2}$ $\tan^{-1}\left(-\frac{1}{2}\right) = -26,57^\circ$ $\therefore \alpha = 180^\circ - 26,57^\circ$ $\therefore \theta = 180^\circ - 153,43^\circ = 26,57^\circ$ $\widehat{DBC} = 2 \times 26,57^\circ$ $= 53,14^\circ$ OR / OF $\sin \theta = \frac{4}{\sqrt{(8)^2 + (-4)^2}}$ $\sin^{-1}(0,4472...) = 26,57^\circ$ $\widehat{DBC} = 2 \times 26,57^\circ = 53,14^\circ$ OR / OF $\tan \widehat{DBO} = \frac{4}{8} = \frac{1}{2}$ $\widehat{DBO} = 26,57^\circ$ $\widehat{DBC} = 2 \times 26,57^\circ$ $= 53,14^\circ$	✓ gradient of BD / <i>gradiënt van BD</i> ✓ calculation of α / <i>berekening van α</i> ✓ angle θ / <i>hoek θ</i> ✓ doubling the angle / <i>verdubbeling van hoek</i> OR / OF ✓ sin definition / <i>sin-definisie</i> ✓ use of arcsin / <i>gebruik van $\sin^{-1}$</i> ✓ angle θ / <i>hoek θ</i> ✓ doubling the angle / <i>verdubbeling van hoek</i> OR / OF ✓ tan ratio / <i>tan verhouding</i> ✓ use of arctan to find angle / <i>gebruik van $\tan^{-1}$ om hoek te bepaal</i> ✓ angle / <i>hoek</i> ✓ doubling the angle / <i>verdubbeling van hoek</i>	(4)
4.5	New circle centre/Nuwe sirkel middelpunt - $M'(5; 1)$ $C'(2; -3)$ $m_{M'C'} = \frac{4}{3}$ $m_{tan} = -\frac{3}{4}$ $-3 = -\frac{3}{4}(2) + c$ $\therefore c = -\frac{3}{2}$ $\therefore y = -\frac{3}{4}x - \frac{3}{2}$	✓ coordinates of M' and C' / <i>koördinate van M' en C'</i> ✓ gradient of MC / <i>gradiënt van MC</i> ✓ gradient of tangent / <i>gradiënt van raaklyn</i> OR / OF ✓ equation / <i>vergelyking</i>	(4)

	OR / OF	OR / OF	
	Gradient of MC / Gradiënt van MC = $\frac{4}{3}$ Hence gradient of M'C' / Gevolglik gradiënt van M'C' = $\frac{4}{3}$ (MC $\parallel$ M'C') Gradient of tangent at C' / Gradiënt van raaklyn by C' = $-\frac{3}{4}$ (M'C' $\perp$ tang at C') (M'C' $\perp$ raaklyn by C') C' = (2 ; -3) $\therefore y + 3 = -\frac{3}{4}(x - 2)$ $\therefore y = -\frac{3}{4}x - \frac{3}{2}$	✓ gradient of MC / gradiënt van MC ✓ gradient of M'C' / gradiënt van M'C' ✓ coordinates of C' / koördinate van C' ✓ equation / vergelyking	(4)
			[19]
QUESTION 5/VRAAG 5			
5.1.1	1	✓ answer / antwoord	(1)
5.1.2	$\cos 2A$	✓ answer / antwoord	(1)
5.2.1	$3^2 = 2^2 + k^2$ $k = -\sqrt{5}$	✓ distance formula / afstand formule Pythagoras Thm / Stelling ✓ answer with correct sign antwoord met korrekte teken	(2)
5.2.2(a)	$\tan(\theta - 180^\circ) = \tan \theta$ $= -\frac{\sqrt{5}}{2}$	✓ reduction / reduksie ✓ answer / antwoord	(2)
5.2.2(b)	$\frac{1 - \sin^2 2\theta}{1 - 2\sin^2 \theta} = \frac{\cos^2 2\theta}{\cos 2\theta}$ $= \cos 2\theta$ $= 1 - 2\sin^2 \theta$ $= 1 - 2\left(-\frac{\sqrt{5}}{3}\right)^2$ $= 1 - \frac{10}{9}$ $= -\frac{1}{9}$ OR / OF $\frac{1 - \sin^2 2\theta}{1 - 2\sin^2 \theta} = \frac{\cos^2 2\theta}{\cos 2\theta}$ $= \cos 2\theta$ $= 2\cos^2 \theta - 1$ $= 2\left(\frac{2}{3}\right)^2 - 1$ $= \frac{8}{9} - 1$ $= -\frac{1}{9}$	✓ $1 - \sin^2 2\theta = \cos^2 2\theta$ ✓ $1 - 2\sin^2 \theta = \cos 2\theta$ ✓ substitution for sin vervanging vir sin ✓ answer / antwoord OR / OF ✓ $1 - \sin^2 2\theta = \cos^2 2\theta$ ✓ $1 - 2\sin^2 \theta = \cos 2\theta$ ✓ substitution for cos vervanging vir cos ✓ answer / antwoord	

	OR / OF	OR / OF	
	$\frac{1 - \sin^2 2\theta}{1 - 2\sin^2 \theta} = \frac{1 - (2\sin\theta\cos\theta)^2}{1 - 2\sin^2 \theta}$ $= \frac{1 - \left[2\left(-\frac{\sqrt{5}}{3}\right)\left(\frac{2}{3}\right)\right]^2}{1 - 2\left(-\frac{\sqrt{5}}{3}\right)^2}$ $= -\frac{1}{9}$	✓ $\sin^2 2\theta = (2\sin\theta\cos\theta)^2$ ✓ substitution for $\sin \theta$ vervang vir $\sin \theta$ ✓ substitution for $\cos \theta$ vervang vir $\cos \theta$ ✓ answer / antwoord	(4)
5.3	$\sin(-200^\circ) \cdot \cos 310^\circ + \tan(-135^\circ) \cdot \cos 380^\circ \cdot \sin 230^\circ$ $= \sin(20^\circ)(\cos 50^\circ) + (\tan 45^\circ)(\cos 20^\circ)(-\sin 50^\circ)$ $= \sin 20^\circ \cos 50^\circ - (1)\cos 20^\circ \sin 50^\circ$ $= \sin(20^\circ - 50^\circ)$ $= \sin(-30^\circ)$ $= -\frac{1}{2}$	✓ ✓ ✓ ✓ reductions to acute angles / reduksie tot skerphoeke ✓ sin expansion / sin uitbreiding ✓ answer / antwoord	(6)
5.4	$\text{LHS/LK} = \sin 2\theta + \cos(2\theta - 90^\circ)$ $= \sin 2\theta + \sin 2\theta$ $= 2 \sin 2\theta$ $= 2(2\sin \theta \cos \theta)$ $= 4 \sin \theta \cos \theta$ $= \text{RHS/RK}$	✓ $\cos(2\theta - 90^\circ) = \sin 2\theta$ ✓ simplification vereenvoudiging ✓ expansion / uitbreiding	(3)
5.5	$10^{\sin x} + 10^{\sin x} \cdot 10^1 = 110$ $10^{\sin x}(1 + 10) = 110$ $10^{\sin x} = 10^1$ $\therefore \sin x = 1$ $\therefore x = -270^\circ \text{ or/of } x = 90^\circ$	✓ split into product of 2 bases skei in product van 2 basisse ✓ simplification / factorisation vereenvoudiging/faktorisering ✓ division by 11 / deel deur 11 ✓ equating the exponents gelykstel van eksponente ✓ both solutions / beide oplossings	(5)
			[24]

QUESTION 6/VRAAG 6

6.1



✓ completing / voltooiing van
 $f(x) = \sin 2x$ graph/grafiek

(1)

6.2

See graph in 6.1 / Sien grafiek in 6.1

$g(x) = \cos(x - 30^\circ)$
 ✓ y intercept / y-afsnit
 ✓ end points / eindpunte
 ✓ turning point / draaipunte
 ✓ x intercepts / x-afsnitte

(4)

6.3

$\sin 2x = \sin(90^\circ - (x - 30^\circ))$
 $\sin 2x = \sin(120^\circ - x)$
 $2x = 120^\circ - x + k \cdot 360^\circ$ or/of $2x = 180^\circ - (120^\circ - x) + k \cdot 360^\circ$
 $3x = 120^\circ + k \cdot 360^\circ$ or/of $x = 60^\circ + k \cdot 360^\circ$
 $\therefore x = 40^\circ + k \cdot 120^\circ$ or/of $x = 60^\circ + k \cdot 360^\circ ; k \in \mathbb{Z}$
 $k = 0 : \theta = 40^\circ ; 60^\circ$
 $k = -1 : \theta = -80^\circ$

✓ co-ratio on RHS
 ko-verhouding RK
 ✓ simplification
 vereenvoudiging
 ✓ $x = 40^\circ + k \cdot 120^\circ$
 ✓ $x = 60^\circ + k \cdot 360^\circ$
 ✓✓ solutions
 oplossings

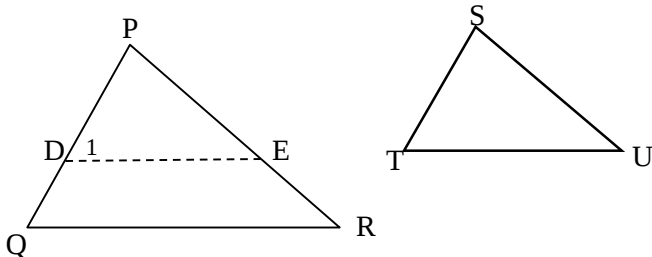
(6)

[11]

QUESTION 7/VRAAG 7			
7.1	$\tan y = \frac{PB}{k}$ $\therefore PB = k \cdot \tan y$ $\tan x = \frac{PB}{BC}$ $\therefore BC = \frac{PB}{\tan x}$ Hence/ <i>Gevolglik</i> $BC = \frac{k \cdot \tan y}{\tan x}$	✓ use of tan ratio <i>gebruik van tan verhouding</i> ✓ $PB = k \cdot \tan y$ ✓ $BC = \frac{PB}{\tan x}$	(3)
7.2	$(AC)^2 = (4,73)^2 + (3)^2 - 2(4,73)(3)(\cos 100^\circ)$ $AC = 6,03 \text{ m}$	✓ use of cosine rule <i>gebruik van cosinusreël</i> ✓ correct substitution in cosine rule <i>korrekte vervanging in cosinusreël</i> ✓ answer / <i>antwoord</i>	(3)
			[6]

QUESTION 8 / VRAAG8			
8.1.1	$\widehat{BAE} = 90^\circ$ ($\angle$ in a semi-circle / $\angle$ in halwe sirkel)	✓ statement/stelling (S) ✓ reason / rede (R)	(2)
8.1.2	$\widehat{E}_1 = 40^\circ$ (sum of $\angle$ s of Δ / som van $\angle$ e van Δ)	✓ statement / S ✓ reason / R	(2)
8.1.3	$\widehat{C}_1 = 40^\circ$ ($\angle$ s subtended by AB OR $\angle$ s in the same segment) ($\angle$ e onderspan deur AB OF $\angle$ e in dieselfde segment)	✓ statement / S ✓ reason / R	(2)
8.1.4	$\widehat{C}_2 = 62^\circ$ (ext. $\angle$ of cyclic quad. / buite $\angle$ van koordev.)	✓ statement / S ✓ reason / R	(2)
8.1.5	$\widehat{ABD} = 62^\circ$ ($\angle$ s subtended by AD OR $\angle$ s in the same segment OR ext. $\angle$ of cyclic quad.) ($\angle$ e onderspan deur AD OF $\angle$ e in dieselfde segment OF buite $\angle$ van koordevierhoek)	✓ statement / S ✓ reason / R	(2)
8.2	equal to the angle in the alternate segment/ <i>gelyk aan die hoek in die oorsaande segment</i>	✓ answer / antwoord	(1)
8.3	R.T.P / Te Bewys: STUR cyclic / koordevierhoek Proof : $\widehat{U}_2 = x$ (tan chord thm)/(raaklyn koord stelling) $\widehat{R}_3 = y$ (tan chord thm)/(raaklyn koord stelling) $\widehat{R}_2 = 180^\circ - (x + y)$ ($\angle$ s on str line)/($\angle$ e op reguitlyn) OR/OF $\widehat{R}_2 = 180^\circ - (x + y)$ (3 $\angle$ s Δ)/(3 $\angle$ e Δ) $T + \widehat{R}_2 = 180^\circ$ STUR cyclic (opposite angles are suppl.) STUR is 'n koordevierhoek (oorstaande hoeke is suppl.)	✓ statement / S ✓ reason / R ✓ S & R ✓ S & R ✓ opp. $\angle$ s of quad. supplementary teenoorst. $\angle$ e van vierhoek supplémentêr	(5)
8.4	$PN = NQ = 8$ units/eenhede (line from the centre $\perp$ chord) (lynstuk vanaf middelpunt $\perp$ koord) $MP^2 = 6^2 + 8^2$ (Pyth. Theorem)/(Pyth. Stelling) $\therefore MP = 10$ units/eenhede $MP = RM = MT = 10$ (radii)/(radiusse) $\therefore RT = 20$ units/eenhede	✓ S & R ✓ S & R ✓ S & R ✓ answer / antwoord	(4)
			[20]

QUESTION 9/VRAAG9			
9.1.1	$\frac{AD}{DE} = \frac{AC}{CF}$ (prop. theorem; $DC \parallel EF$) <i>(Ewaredigh. stelling ; $DC \parallel EF$)</i> $\frac{12}{3} = \frac{AC}{5}$ $20 = AC$	✓ S & R ✓ substitution / <i>vervanging</i> ✓ answer / <i>antwoord</i>	(3)
9.1.2	$AO = 10$ (diagonals of a parallelogram bisect) <i>(hoeklyne van 'n parallelogram halveer)</i>	✓ answer / <i>antwoord</i>	(1)
9.1.3	$\triangle ADC \parallel \triangle AEF$ ($\angle, \angle, \angle$) $\frac{AD}{AE} = \frac{DC}{EF}$ ($\parallel \Delta$ s: sides in prop.) <i>($\parallel \Delta$e : sye is eweredig)</i> $\frac{12}{15} = \frac{14}{EF}$ $EF = \frac{14 \times 15}{12}$ $EF = 17,5$	✓ S & R ✓ statement / S ✓ answer / <i>antwoord</i>	(3)
9.2	$\frac{\text{Area } \triangle ADC}{\text{Area } \triangle AEF} = \left(\frac{12}{15}\right)^2$ $= \left(\frac{4}{5}\right)^2 = \frac{16}{25}$ $\frac{\text{Area } \triangle ADO}{\text{Area } \triangle ADC} = \frac{1}{2}$ $\frac{\text{Area } \triangle ADC}{\text{Area } \triangle AEF} \times \frac{\text{Area } \triangle ADO}{\text{Area } \triangle ADC} = \frac{\text{Area } \triangle ADO}{\text{Area } \triangle AEF}$ But/Maar: $\frac{\text{Area } \triangle ADC}{\text{Area } \triangle AEF} \times \frac{\text{Area } \triangle ADO}{\text{Area } \triangle ADC} = \frac{16}{25} \times \frac{1}{2}$ $= \frac{8}{25}$ $\therefore \frac{\text{Area } \triangle ADO}{\text{Area } \triangle AEF} = \frac{8}{25}$ OR/OF $\frac{\text{Area } \triangle ADO}{\text{Area } \triangle AEF} = \frac{\frac{1}{2} AD \cdot AO \sin \hat{DAO}}{\frac{1}{2} AE \cdot AF \sin \hat{DAO}}$ $= \frac{12 \times 10}{15 \times 25}$ $= \frac{8}{25}$	(Area => Oppervlakte) ✓ $\frac{\text{Area } \triangle ADC}{\text{Area } \triangle AEF} = \frac{16}{25}$ ✓ $\frac{\text{Area } \triangle ADO}{\text{Area } \triangle ADC} = \frac{1}{2}$ ✓ simplification / <i>vereenvoudiging</i> OR/OF ✓ use of area rule <i>gebruik van oppervlakte reël</i> ✓ area of $\triangle ADO$ ✓ area of $\triangle AEF$	(3)
			[10]

QUESTION 10/VRAAG 10		
10.1		
	Construction: Mark D on PQ and E on PR such that PD = ST and PE = SU. Join DE. Konstruksie: Merk D op PQ en E op PR sodat PD = ST en PE = SU. Verbind DE. Proof/Bewys: In $\triangle PDE$ and/en $\triangle STU$ $\hat{P} = \hat{S}$ (given) / (gegee) PD = ST (construction) / (konstruksie) PE = SU (construction) / (konstruksie) $\triangle PDE \equiv \triangle STU$ (SAS) $\therefore \hat{D}_1 = \hat{T}$ ($\equiv \Delta$'s) But/Maar: $\hat{Q} = \hat{T}$ (given) / (gegee) $\therefore \hat{D}_1 = \hat{Q}$ $\therefore DE \parallel QR$ (corr. $\angle$ s =) / (ooreenk. $\angle$ e =) $\therefore \frac{PD}{PQ} = \frac{PE}{PR}$ (prop. theorem; $DE \parallel QR$) $\therefore \frac{ST}{PQ} = \frac{SU}{PR}$	✓ construction / konstruksie ✓ S & R ✓ $\hat{D}_1 = \hat{T}$ ✓ $\hat{D}_1 = \hat{Q}$ ✓ reason for lines $\parallel$ rede vir $\parallel$ lyne ✓ prop. theorem; $DE \parallel QR$ eweredigh. stelling; $DE \parallel QR$
10.2.1	$\hat{A} = x$ (tan chord thm)/(raakl koord stelling) $\hat{C}_3 = x$ (angles opp. = sides)/(hoeke teenoor = sye)	✓ statement(S) ✓ reason(R) ✓ S & R
10.2.2	R.T.P/Te Bewys: $\triangle TOC \parallel \triangle BPC$ $\hat{A}CB = 90^\circ$ ($\angle$ in the semi-circle)/($\angle$ in halwe sirkel) Proof/Bewys : $\hat{C}_3 = \hat{C}_1 = x$ (proved)/(reeds bewys) $\hat{T}_2 = 90^\circ + x$ (ext. $\angle$ of Δ) / (buite $\angle$ van Δ) $\hat{B}_1 = 90^\circ + x$ (ext. $\angle$ of Δ) / (buite $\angle$ van Δ) $\therefore \hat{T}_2 = \hat{B}_1$ $\therefore \hat{O}_2 = \hat{P}$ (sum of $\angle$ s in Δ) / (som van $\angle$ e in Δ) $\therefore \triangle TOC \parallel \triangle BPC$ ($\angle$, $\angle$, $\angle$) OR/OF $\hat{A}CB = 90^\circ$ ($\angle$ in the semi-circle) / (hoek in halwe sirkel) $\hat{B}_2 = 90^\circ - x$ (sum of $\angle$ s in Δ) / (som van $\angle$ e in Δ) $\therefore \hat{P} = 90^\circ - 2x$ (ext. $\angle$ of Δ) / (buite $\angle$ van Δ) $\hat{O}_1 = 2x$ ($\angle$ at centre = $2 \times \angle$ at circum.)/(Middelpunts $\angle$ = $2 \times$ Omtrekshoek) $\therefore \hat{O}_2 = 90^\circ - 2x$ ($SO \perp AB$) $\therefore \hat{O}_2 = \hat{P}$ $\hat{C}_3 = \hat{C}_1 = x$ (proved above) / (alreeds bo bewys) $\therefore \triangle TOC \parallel \triangle BPC$ ($\angle$, $\angle$, $\angle$)	✓ S & R ✓ S ✓ S & R ✓ S ✓ R OR/OF ✓ S & R ✓ S ✓ S & R ✓ S ✓ R

10.2.3	R.T.P/Te Bewys: $TO \cdot PC = OB \cdot BP$ Proof/Bewys: $\frac{TO}{BP} = \frac{OC}{PC}$ But/Maar $OC = OB$ (radii)/(radiusse) $\therefore \frac{TO}{BP} = \frac{OB}{PC}$ $\therefore TO \cdot PC = OB \cdot BP$	✓ sides in prop. sy is eweredig ✓ S	(2)
10.2.4	In $\triangle OPC$: $OP^2 = OC^2 + PC^2$ (Pyth. theorem/stelling) But/Maar: $OB = OC = BP$ (radii)/(radiusse) $\therefore (2OC)^2 = OC^2 + PC^2$ $4OC^2 = OC^2 + PC^2$ $\therefore PC^2 = 3OC^2$	✓ S & R ✓ $OB = OC = BP$ ✓ $(2OC)^2 = OC^2 + PC^2$	(3)
			[19]
TOTAL/TOTAAL:			150