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**PREPARATORY EXAMINATION
VOORBEREIDINGSEKSAMEN**

GRADE/GRAAD 12

MATHEMATICS/WISKUNDE P2

SEPTEMBER 2019

MARKS/PUNTE: 150

MARKING GUIDELINES/NASIENRIGLYNE

**This marking guidelines consists of 17 pages.
*Hierdie nasienriglyne bestaan uit 17 bladsye.***

NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum.
- Assuming answers/values in order to solve a problem is NOT acceptable.

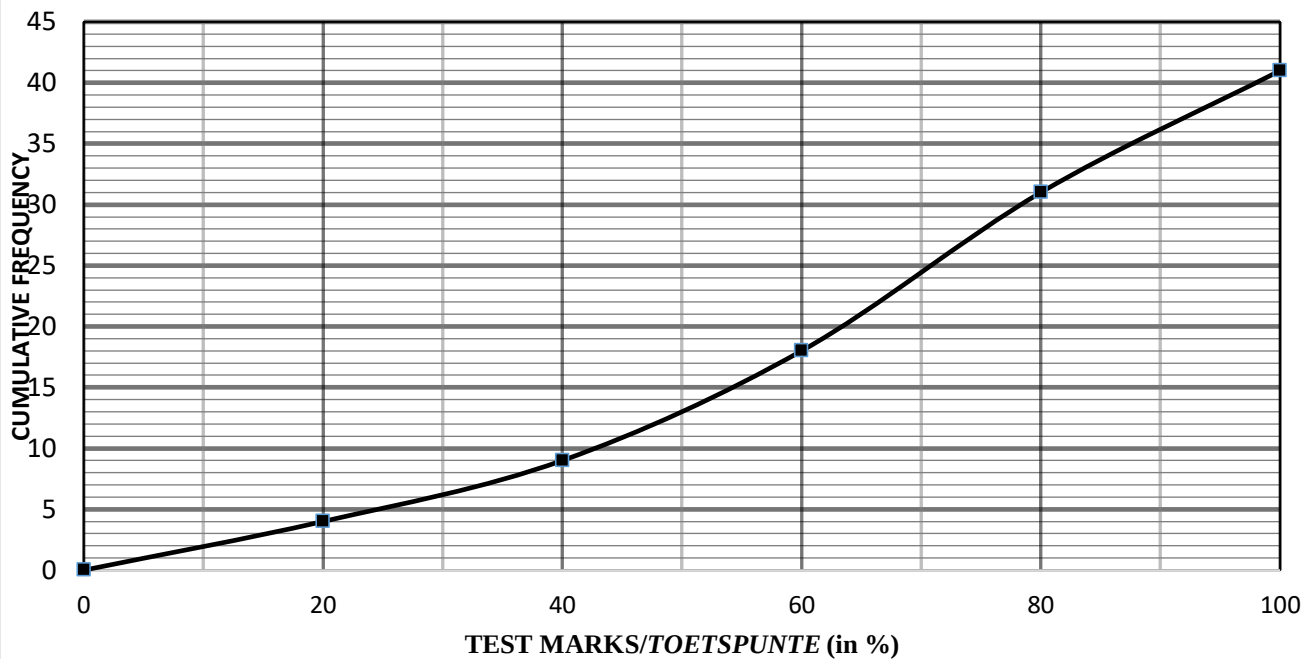
NOTA:

- As 'n kandidaat 'n vraag TWEE KEER beantwoord, merk slegs die EERSTE poging.
- As 'n kandidaat 'n poging om die vraag te beantwoord, doodgetrek het en nie dit oorgedoen het nie, merk die doodgetrekte poging.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienmemorandum toegepas.
- Aanvaarding van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.

GEOMETRY/MEETKUNDE	
S	A mark for the correct statement. (A statement mark is independent of a reason)
	'n Punt vir 'n korrekte bewering. ('n Punt vir 'n bewering is onafhanklik van die rede)
R	A mark for a correct reason. (A reason mark may only be awarded if the statement is correct)
	'n Punt vir 'n korrekte rede. ('n Punt word slegs vir die rede toegeken as die bewering korrek is)
S/R	Award a mark if the statement AND reason are both correct.
	Ken 'n punt toe as beide die bewering EN rede korrek is.

1.4

OGIVE/OGIEF



- ✓ using the cumulative frequency/gebruik die kumulatiewefrekwensie
- ✓ smooth curve/gladde kurwe
- ✓ using upper limits/gebruik boonste limiete

(3)

1.5

$$\begin{aligned} \text{IQR} &= Q_3 - Q_1 \\ &= 68 - 33 \\ &= 35 \end{aligned}$$

ACCEPT/AANVAAR:

- 32 **OR/OF** 34 lower quartile/laer kwartiel
- 67 **OR/OF** 69 upper quartile/boonste kwartiel

- ✓ L Q
- ✓ U Q
- ✓ IQR

(3)

[12]

QUESTION/VRAAG 2

2.1	$y = A + Bx$ $y = 25,42 + 1,32x$	✓ 25,42 ✓ 1,32 ✓ $y = 25,42 + 1,32x$ (3)
2.2	$y = 25,42 + 1,32(36)$ $y = 72,94$	✓ correct substitution/ <i>korrekte vervanging</i> ✓ answer/ <i>antwoord</i> (2)
2.3	$r = 0,81$ Strong positive/ <i>Sterk positiewe</i>	✓ $r = 0,81$ ✓ Strong/ <i>Sterk</i> ✓ Positive/ <i>Positiewe</i> (3)
[8]		

QUESTION/VRAAG 3

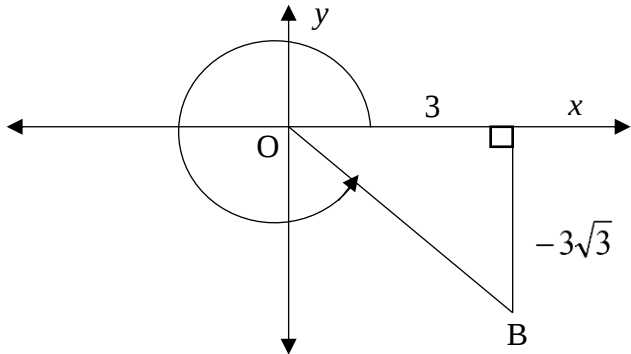
3.1	$m_{BG} = \frac{-4-4}{-3-1}$ $= 2$	✓ substitution/vervangings ✓ $m_{BG} = 2$ (2)
3.2	$y = 2x + c$ $sub(-3; -4)$ $-4 = 2(-3) + c$ OR/OF $\therefore c = 2$ $y = 2x + 2$ $y = 2x + c$ $sub(1; 4)$ $4 = 2(1) + c$ $\therefore c = 2$ $y = 2x + 2$ OR/OF $y - y_1 = m(x - x_1)$ $y + 4 = 2(x - (-3))$ OR/OF $y = 2x + 2$ $y - y_1 = m(x - x_1)$ $y - 4 = 2(x - 1)$ $y = 2x + 2$	✓ substitution/vervangings $(-3; -4)/(1, 4)$ ✓ equation/vergelyking (2) OR/OF ✓ substitution/vervangings $(-3; -4)/(1, 4)$ ✓ equation/vergelyking (2)
3.3.1	$m_{BC} = -\frac{1}{2}$ $-\frac{1}{2} = \frac{k - (-4)}{2 - (-3)}$ $-\frac{1}{2} = \frac{k + 4}{5}$ $-5 = 2k + 8$ $2k = -13$ $k = -\frac{13}{2} = -6\frac{1}{2}$	✓ $m_{BC} = -\frac{1}{2}$ ✓ correct substitution/korrekte vervanging ✓ simplification/vereenvoudiging ✓ k value/k-waarde (4)
3.3.2	By translation/Deur translasie $(x; y) \rightarrow \left(x + 5; y - 2\frac{1}{2}\right)$ $(1; 4) \rightarrow \left(6; 1\frac{1}{2}\right)$ $D\left(6; \frac{3}{2}\right)$	✓ method/metode ✓ x value/x-waarde ✓ y value/y-waarde (3)

	OR/OF	OR/OF
	$\frac{y - \left(-\frac{13}{2}\right)}{x - 2} = \frac{2}{1}$ $y = 2x - \frac{21}{2} \dots\dots\dots(i)$ $\frac{y - 4}{x - 1} = -\frac{1}{2}$ $2y - 8 = -x + 1$ $2\left(2x - \frac{21}{2}\right) - 8 = -x + 1$ $4x - 21 - 8 = -x + 1$ $\therefore x = 6$ $y = 2(6) - \frac{21}{2}$ $\therefore y = \frac{3}{2}$ $D\left(6; \frac{3}{2}\right)$	✓ method/metode ✓ x value/x-waarde ✓ y value/y-waarde (3)
3.3.3	$m_{CD} = 2$ $\tan \hat{D}\hat{H}X = 2$ $\hat{D}\hat{H}X = \tan^{-1}(2)$ $\hat{D}\hat{H}X = 63,49^\circ$ $\beta = 63,49^\circ \text{ [vertically opposite angles/vertikaal teenoorgestelde hoeke]}$	✓ $m_{CD} = 2$ ✓ $\hat{D}\hat{H}X$ ✓ $\beta = 63,49^\circ$ (3)
3.3.4	$y = 2x + c$ $-\frac{13}{2} = 2(2) + c$ $-\frac{21}{2} = c$ $y = 2x - \frac{21}{2}$ $0 = 2x - \frac{21}{2}$ $\therefore x = 5,25$ $GH = 6,25$ OR/OF $\text{Area/Oppvl} = \frac{1}{2} GH \cdot y_D$ $= \frac{1}{2} \times 6,25 \times 1,5$ $= 4,69 \text{ square units/vierkantteenhede}$ $HD = \sqrt{(6 - 5,25)^2 + \left(0 - \frac{3}{2}\right)^2}$ $= \frac{3\sqrt{5}}{4}$ $\hat{G}\hat{H}\hat{D} = 180^\circ - 63,49^\circ \text{ [}\angle\text{'s in straight line/}\angle\text{' in reguitlyn]}$ $= 116,51^\circ$ $\text{Area of/Oppvl van GHD} = \frac{1}{2} (GH)(HD) \sin \hat{G}\hat{H}\hat{D}$ $= \frac{1}{2} (6,25) \left(\frac{3\sqrt{5}}{4}\right) \sin 116,51^\circ$ $= 4,69 \text{ square units/vierkantteenhede}$	✓ substitution/vervanging $\left(2; -\frac{13}{2}\right)$ ✓ $y = 0$ ✓ $GH = 6,25$ ✓ method/metode ✓ y_D ✓ substitution/vervanging ✓ answer/antwoord (7)

QUESTION/VRAAG 4

4.1.1	centre/middelpunt E(3;1) $(x-3)^2 + (y-1)^2 = r^2$ $(5-3)^2 + (-5-1)^2 = r^2$ $40 = r^2$ $(x-3)^2 + (y-1)^2 = 40$ $x^2 - 6x + 9 + y^2 - 2y + 1 = 40$ $x^2 - 6x + y^2 - 2y = 30$	✓ substitution/vervanging E(3; 1) ✓ substitution/vervanging P(5; -5) ✓ $40 = r^2$ ✓ standard form/standaardvorm (4)
4.1.2	$m_{rad} = \frac{1-(-5)}{3-5}$ $= \frac{6}{-2} = -3$ $m_{tan} = \frac{1}{3}$ [radius $\perp$ tan] $y = \frac{1}{3}x + c$ $-5 = \frac{1}{3}(5) + c$ $c = \frac{-20}{3}$ $y = \frac{1}{3}x - \frac{20}{3}$	✓ correct substitution/korrekte vervanging ✓ $m_{rad} = -3$ ✓ $m_{rad} = \frac{1}{3}$ ✓ substitution/vervanging (5; -5) ✓ equation/vergelyking (5)
4.2.1	centre/middelpunt $= \frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}$ $= \frac{3+5}{2}; \frac{1-5}{2}$ centre/middelpunt: (4; -2)	✓ method/metode ✓ x value/x-waarde ✓ y value/y-waarde (3)
4.2.2	$(x-4)^2 + (y+2)^2 = r^2$ $(3-4)^2 + (1+2)^2 = r^2$ $10 = r^2$ $r = \sqrt{10}$	✓ substitution of centre/vervanging van middelpunt ✓ substitution/vervanging (3;1) ✓ $= \sqrt{10}$ (3)
4.3	$r = \sqrt{40}$ EC $= \sqrt{(9-3)^2 + (3-1)^2}$ $= 2\sqrt{10}$ C is on the circumference/C is op die omtrek	✓ $r = \sqrt{40}$ ✓ distance/afstand EC ✓ motivation/motivering (3)
[18]		

QUESTION/VRAAG 5

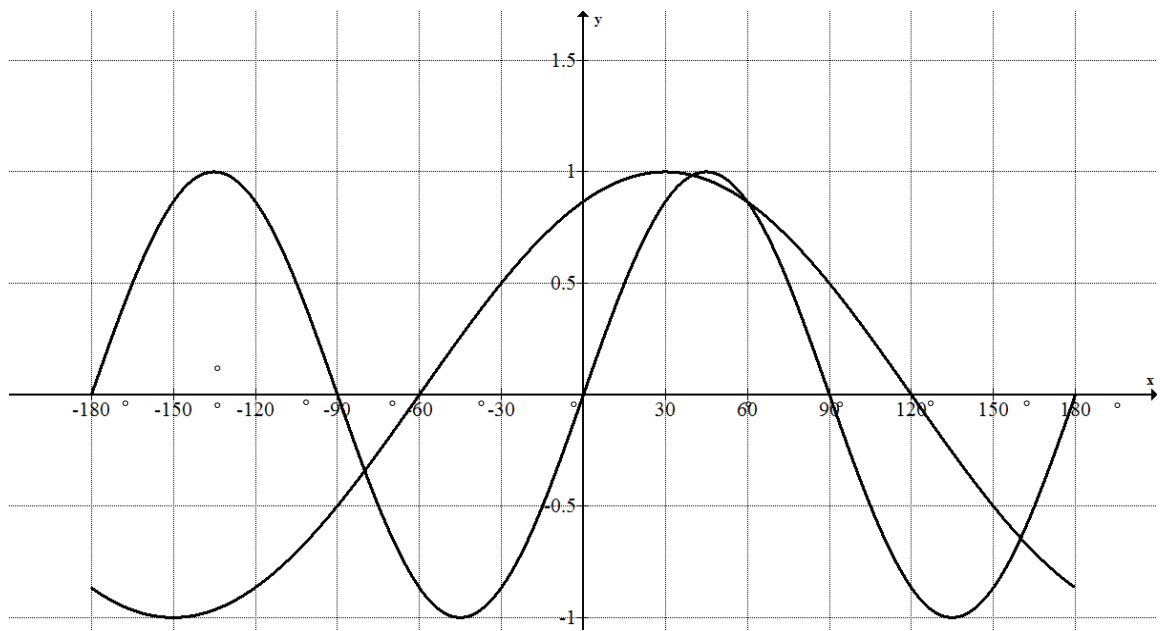
5.1.1	 $(3)^2 + (-3\sqrt{3})^2 = OB^2$ $OB = 6$	✓Pythagoras ✓OB (2)
5.1.2	$\cos(\alpha + 30^\circ)$ $= \cos \alpha \cos 30^\circ - \sin \alpha \sin 30^\circ$ $= \left(\frac{3}{6}\right)\left(\frac{\sqrt{3}}{2}\right) - \left(\frac{-3\sqrt{3}}{6}\right)\left(\frac{1}{2}\right)$ $= \left(\frac{\sqrt{3}}{2}\right)$	✓expansion/uitbreiding ✓✓ratios/verhoudings ✓answer/antwoord (4)
5.2	$\frac{\sin^2(90^\circ - x)\tan(360^\circ - x)}{\sin(-x)}$ $= \frac{\cos^2 x (-\tan x)}{(-\sin x)}$ $= \frac{\cos^2 x \left(-\frac{\sin x}{\cos x}\right)}{-\sin x}$ $= \cos x$	✓$\cos^2 x$ ✓$-\tan x$ ✓$-\sin x$ ✓$\frac{\sin x}{\cos x}$ (4)

5.3	$\cos(60^\circ + \theta) - \cos(60^\circ - \theta)$ $= [\cos 60^\circ \cos \theta - \sin 60^\circ \sin \theta] - [\cos 60^\circ \cos \theta + \sin 60^\circ \sin \theta]$ $= -2 \sin 60^\circ \sin \theta$ $= -2 \cdot \frac{\sqrt{3}}{2} \cdot \sin \theta$ $= -\sqrt{3} \sin \theta$ OR/OF $\cos(60^\circ + \theta) - \cos(60^\circ - \theta)$ $= [\cos 60^\circ \cos \theta - \sin 60^\circ \sin \theta] - [\cos 60^\circ \cos \theta + \sin 60^\circ \sin \theta]$ $= \frac{1}{2} \cos \theta - \frac{\sqrt{3}}{2} \sin \theta - \frac{1}{2} \cos \theta - \frac{\sqrt{3}}{2} \sin \theta$ $= -2 \left(\frac{\sqrt{3}}{2} \right) \sin \theta$ $= -\sqrt{3} \sin \theta$	✓ method/metode ✓ ratios/verhoudings ✓ answer/antwoord (3) OR/OF ✓ method/metode ✓ ratios/verhoudings ✓ answer/antwoord (3)
5.4.1	$LHS = \frac{1 - \sin 2A}{\sin A - \cos A}$ $= \frac{1 - 2 \sin A \cos A}{\sin A - \cos A}$ $= \frac{\sin^2 A + \cos^2 A - 2 \sin A \cos A}{\sin A - \cos A}$ $= \frac{(\sin A - \cos A)(\sin A + \cos A)}{\sin A - \cos A}$ $= \sin A + \cos A$ OR/OF $RHS = \sin A - \cos A \times \frac{\sin A - \cos A}{\sin A - \cos A}$ $= \frac{\sin^2 A - 2 \sin A \cos A + \cos^2 A}{\sin A - \cos A}$ $= \frac{1 - 2 \sin A \cos A}{\sin A - \cos A}$	✓ $2 \sin A \cos A$ ✓ $\sin^2 A + \cos^2 A$ ✓ factors/faktore ✓ answer/antwoord (4) OR/OF ✓ $\frac{\sin A - \cos A}{\sin A - \cos A}$ ✓ identities/identiteite ✓ simplification/vereenvoudiging ✓ answer/antwoord (4)
5.4.2	$\sin A - \cos A = 0$ $\sin A = \cos A$ $\tan A = 1$ $A = 45^\circ$	✓ $\sin A - \cos A = 0$ ✓ answer/antwoord (2)
[19]		

QUESTION/VRAAG 6

6.1	$\sin 2x = \sin(90^\circ - (x - 30^\circ)) + 360.k$ $2x = 90^\circ - x + 30^\circ + 360.k$ $2x = 120^\circ - x + 360.k$ $x + 2x = 120^\circ + 360.k$ $3x = 120^\circ + 360.k$ $x = 40^\circ + 120^\circ k, k \in \mathbb{Z}$ OR/OF $2x = 180^\circ - (120^\circ - x)$ $2x = 180^\circ - 120^\circ + x$ $2x - x = 60^\circ$ $x = 60^\circ + 360^\circ k$ ALTERNATIVE/ALTERNATIEF: $\cos(90^\circ - 2x) = \cos(x - 30^\circ) + 360.k$ $90^\circ - 2x = x - 30^\circ + 360.k$ $-3x = -120^\circ + 360.k$ $x = 40^\circ - 120^\circ k, k \in \mathbb{Z}$ OR/OF $90^\circ - 2x = 360^\circ - (x - 30^\circ)$ $-x = 300^\circ + 360^\circ k$ $x = -300^\circ + 360^\circ k$ $x = 60^\circ + 360^\circ k$	✓ method/metode ✓ $2x = 90^\circ - x + 30^\circ + 360.k$ ✓ $x = 40^\circ + 120^\circ k, k \in \mathbb{Z}$ ✓ $2x = 180^\circ - (120^\circ - x)$ ✓ $x = 60^\circ + 360^\circ k$ (5) ALTERNATIVE/ALTERNATIEF: ✓ method/metode ✓ $90^\circ - 2x = x - 30^\circ + 360.k$ ✓ $x = 40^\circ - 120^\circ k, k \in \mathbb{Z}$ ✓ $90^\circ - 2x = 360^\circ - (x - 30^\circ)$ ✓ $x = 60^\circ + 360^\circ k$ (5)
6.2.1	Period = 360°	✓ answer/antwoord (1)
6.2.2	$-150^\circ < x < 30^\circ$	✓ values/waardes ✓ inequalities/ongelykhede (2)

6.2.3



- ✓ x intercepts/x-afsnitte
- ✓ turning points/draaipunte
- ✓ shape/vorm

(3)

6.2.4

$-180^\circ \leq x \leq -90^\circ$; $-60^\circ \leq x \leq 0^\circ$; $90^\circ \leq x \leq 120^\circ$

✓ $-180^\circ \leq x \leq -90^\circ$

✓ $-60^\circ \leq x \leq 0^\circ$

✓ $90^\circ \leq x \leq 120^\circ$

(3)

[14]

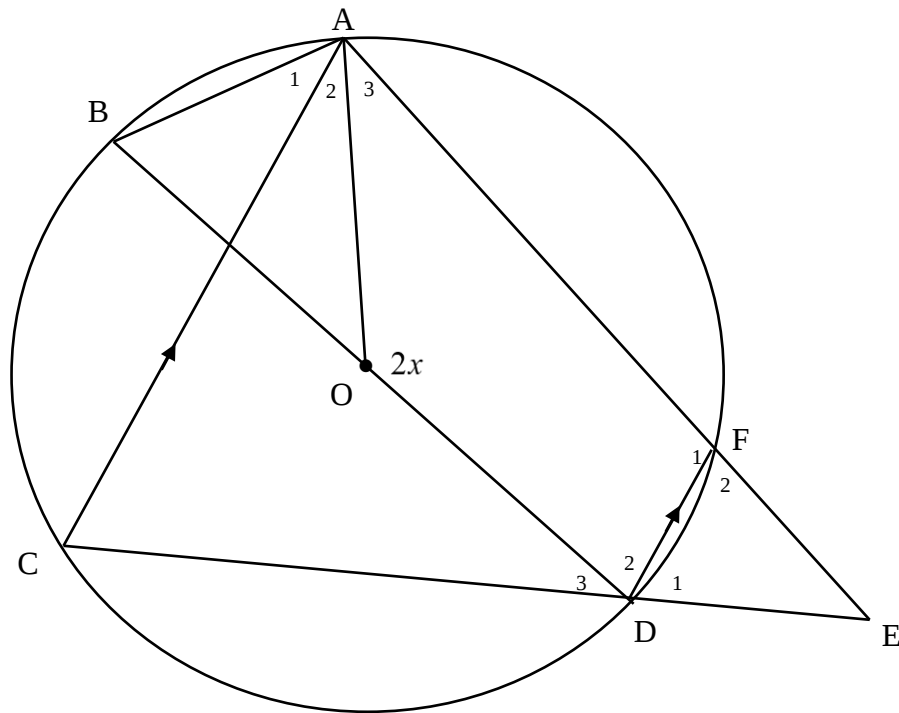
QUESTION/VRAAG 7

7.1	$\hat{BDC} = 180^\circ - 2\alpha$ $\frac{y}{\sin \alpha} = \frac{x}{\sin 180^\circ - 2\alpha}$ $y = \frac{x \sin \alpha}{\sin(180^\circ - 2\alpha)}$ $y = \frac{x \sin \alpha}{2 \sin \alpha \cos \alpha}$ $y = \frac{x}{2 \cos \alpha}$ $\cos \theta = \frac{BD}{AB}$ $AB \cos \theta = BD$ $AB = \frac{BD}{\cos \theta}$ $AB = \frac{x}{2 \cos \alpha} \div \cos \theta$ $AB = \frac{x}{2 \cos \alpha} \times \frac{1}{\cos \theta}$ $AB = \frac{x}{2 \cos \alpha \cos \theta}$	$\checkmark \hat{BDC} = 180^\circ - 2\alpha$ $\checkmark$ method/metode $\checkmark$ substitution/vervanging $\checkmark 2 \sin \alpha \cos \alpha$ $\checkmark AB = \frac{BD}{\cos \theta}$ $\checkmark$ substitution/vervanging BD $\checkmark$ simplification/vereenvoudiging (7)
[7]		

QUESTION/VRAAG 8

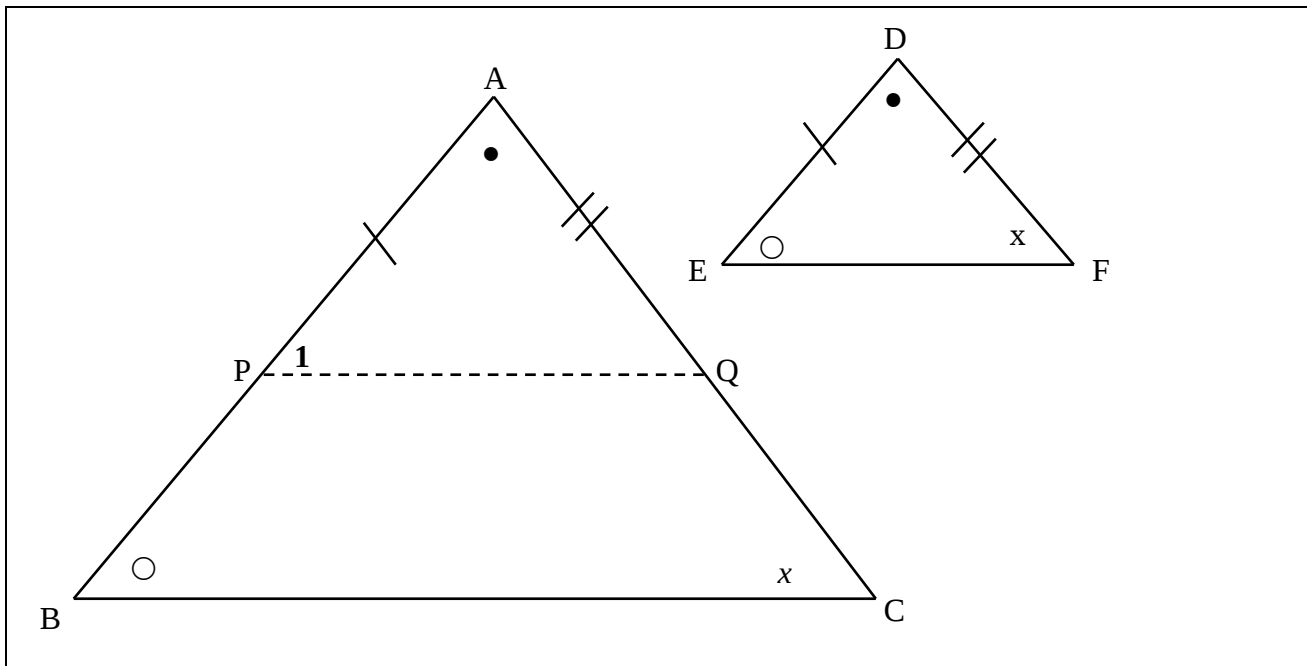
8.1.1	$\hat{H}_3 = 35^\circ$ [tan chord theorem/tan koordteorie] $\hat{E}_4 = \hat{H}_3 = 35^\circ$ [$\angle$ opp = sides/ $\angle$ e teenoor = sye]	$\checkmark$ S $\checkmark$ R $\checkmark$ S/R (3)
8.1.2	$\hat{EKH} = 180^\circ - 2(35^\circ)$ [sum of $\angle$'s in Δ /som van $\angle$ e in Δ] $= 110^\circ$	$\checkmark$ S $\checkmark$ answer/antwoord (2)
8.1.3	$\hat{G} = 180^\circ - 110^\circ$ [opp $\angle$ of cyclic quad/ $\angle$ e teenoor van kdvh] $= 70^\circ$	$\checkmark$ S $\checkmark$ R (2)
8.1.4	$\hat{O}_1 = 220^\circ$ [$\angle$ at centre = $2 \times \angle$ at circumference/midpts $\angle^e = 2$ omtreks $\angle^e$]	$\checkmark$ S $\checkmark$ R (2)
8.2	$(x-4)^2 + 12^2 = x^2$ [Pythagoras] $x^2 - 8x + 16 + 144 = x^2$ $-8x = -160$ $x = 20$	$\checkmark$ S/R $\checkmark$ expansion/ uitbreiding $\checkmark$ simplification/ vereenvoudiging $\checkmark$ answer/antwoord (4)
[13]		

QUESTION/VRAAG 9

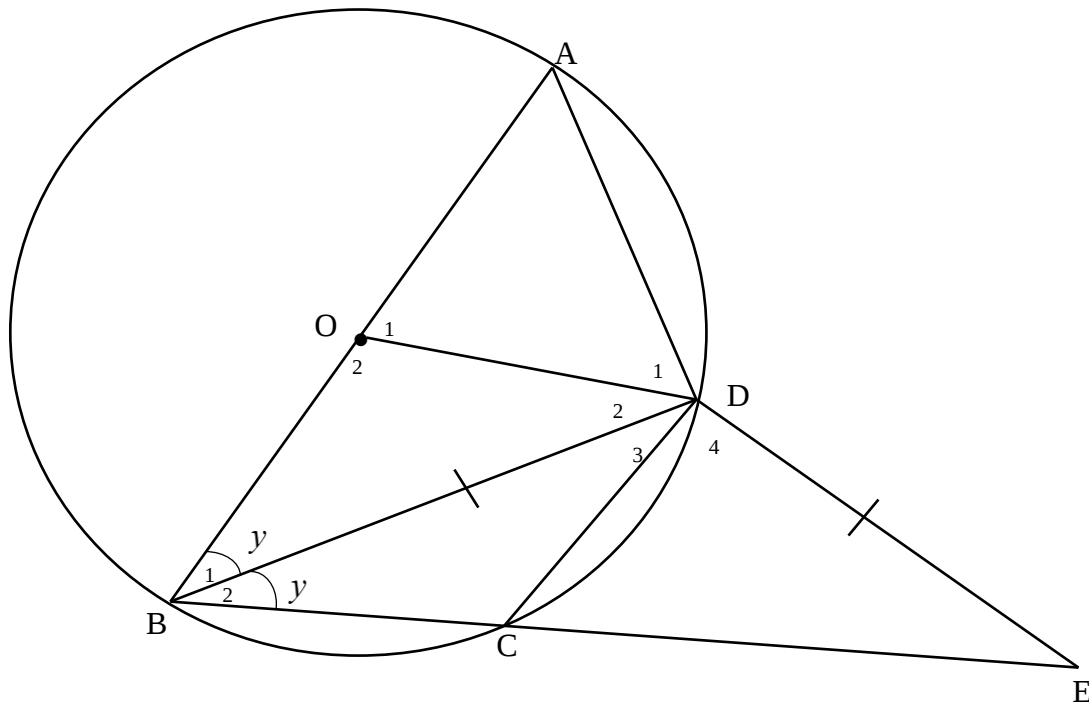


9.1.1	$\hat{C} = x$ [$\angle$ at centre = $2 \times \angle$ at circumference/midpts $\angle = 2 \times \text{omtreks } \angle$] $\hat{B} = x$ [$\angle$ s in same segment/ $\angle$ e in dieselfdesegment] $\hat{D}_1 = x$ [corresp $\angle$ s /ooreenkomstige $\angle$ e; $AC \parallel DF$] $\hat{BAF} = x$ [exterior $\angle$ of cyclic quad/buite $\angle$ kdvh]	$\checkmark$ S/R $\checkmark$ S/R $\checkmark$ S $\checkmark$ R $\checkmark$ S $\checkmark$ R	(6)
9.1.2	$\hat{D}_1 = \hat{F}_2 = x$ $\therefore DE = FE$ [$\angle^s$ opp = sides/ $\angle$ e teenoor = sye] $\hat{E} = 180^\circ - 2x$ [sum of $\angle^s$ in Δ /som van $\angle^e$ in Δ]	$\checkmark \hat{D}_1 = \hat{F}_2$ $\checkmark \hat{E} = 180^\circ - 2x$	(2)
9.1.3	$\hat{E} = 180^\circ - 2x$ [sum of $\angle^s$ in Δ /som van $\angle^e$ in Δ] $\hat{AOD} = 2x$ $\therefore AODE$ is a cyclic quadrilateral/is 'n kdvh [converse of a cyclic quad/omgek van kdvh]	$\checkmark$ S $\checkmark$ R	(2)
9.2	$\frac{AF}{FE} = \frac{CD}{DE}$ [prop theorem/eweredigh] $\frac{12}{8} = \frac{AF}{10}$ $AF = 15$	$\checkmark$ S $\checkmark$ R $\checkmark$ answer/antwoord	(3)
[13]			

QUESTION/VRAAG 10



10.1	$\hat{A} = \hat{D}$ [given/gegee] $AQ = DF$ [construction/konstruksie] $AP = DE$ [construction/konstruksie] $\therefore \triangle APQ \equiv \triangle DEF$ [S/S] $\hat{P}_1 = \hat{E}$ $\hat{P}_1 = \hat{B}$ [$\hat{E} = \hat{B}$] $PQ \parallel BC$ [corresp $\angle$'s/ooreenkomstige $\angle$ e] $\frac{AP}{AB} = \frac{AQ}{AC}$ [$PQ \parallel BC$] But/maar $AP = DE$ and/en $AQ = DF$ $\therefore \frac{DE}{AB} = \frac{DF}{AC}$	$\checkmark$ construction/konstruksie $\checkmark$ S/R $\checkmark \hat{P}_1 = \hat{E}$ $\checkmark$ S/R $\checkmark$ S (5)
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10.2.1	$\hat{A}\hat{D}B = 90^\circ$ [$\angle$ in semi-circle/ <i>semi - sirkel</i>] $\hat{A} = 90^\circ - y$ [$\angle$ in semi-circle/ <i>semi - sirkel</i>] $\hat{B}_2 = \hat{E}$ [$\angle^s$ opp = sides/ <i>∠e teenoor = sye</i>] $\hat{D}\hat{C}E = \hat{A} = 90^\circ - y$ [$\text{ext. } \angle \text{ of a cyclic quad} = \text{int. opp } \angle$ <i>/ verlengde } \angle \text{ van 'n Kdvh} = \text{binne teenoorg } \angle</i>] $\therefore \hat{D}_4 = 90^\circ$ [sum of $\angle^s$ in Δ / <i>som van } \angle^e \text{ in } \Delta</i>]	$\checkmark$ S/R $\checkmark$ S $\checkmark$ S/R $\checkmark$ S/R $\checkmark$ S/R	(5)
10.2.2	$\hat{B}_1 = \hat{D}_2 = y$ [$\angle$ opp = sides/ <i>∠e teenoor = sye</i>] $\hat{B}_1 = \hat{B}_2$ [given/ <i>gegee</i>] $\hat{E} = \hat{D}_2$ [proven/ <i>bewys</i>] $\therefore \Delta BOD \parallel \Delta BDE$ [$\angle \angle \angle$]	$\checkmark$ S/R $\checkmark$ S $\checkmark$ R	(3)
10.2.3	$\frac{DE}{OD} = \frac{BE}{BD}$ [$\parallel \Delta$] <i>but/maar</i> $BD = DE$ [given/ <i>gegee</i>] $\therefore \frac{DE}{OD} = \frac{BE}{DE}$ $DE^2 = BE \cdot OD$	$\checkmark$ S $\checkmark$ R $\checkmark$ S $\checkmark$ substitution/ <i>vervang</i>	(4)

[17]

QUESTION/VRAAG 11

11.1	$\frac{ON}{NM} = \frac{OT}{TS} \quad [\text{prop theorem/eweredigh}]$ $\frac{ON}{NM} = \frac{OP}{PQ} \quad [\text{prop theorem/eweredigh}]$ $\therefore \frac{OT}{TS} = \frac{OP}{PQ}$ $\therefore NT \parallel MS$	✓S ✓R ✓S ✓S (4)
11.2	$\frac{ON}{NM} = \frac{OT}{TS} = \frac{3}{5} \quad [\text{prop theorem/eweredigh}]$ $OT = \frac{3}{8} \times 32$ $= 12$ $VT = \frac{5}{8} \times 12$ $= \frac{15}{2} \text{ or } 7,5$	✓S/R ✓OT ✓method/metode ✓ answer/antwoord (4)
		[8]

TOTAL/TOTAAL: 150