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**GRADE 12**

**MATHEMATICS P2 MARKING GUIDE  
WISKUNDE V2 NASIENRIGLYNE**

**AUGUST 2022**

**MARKS/PUNTE: 150**

These marking guidelines consist of 20 pages/Hierdie nasieriglyne bestaan uit 20 bladsye.

**NOTE:**

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

**NOTA:**

- As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.
- As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, sien die doodgetrekte poging na.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.
- Om antwoorde/waardes te aanvaar om 'n probleem op te los, word NIE toegelaat NIE.

GEOMETRY • MEETKUNDE	
<b>S</b>	<b>A mark for a correct statement</b> (A statement mark is independent of a reason)
<b>'n Punt vir 'n korrekte bewering</b> ('n Punt vir 'n bewering is onafhanklik van die rede)	
<b>R</b>	<b>A mark for the correct reason</b> (A reason mark may only be awarded if the statement is correct)
<b>'n Punt vir 'n korrekte rede</b> ('n Punt word slegs vir die rede toegeken as die bewering korrek is)	
<b>S/R</b>	<b>Award a mark if statement AND reason are both correct</b>
	<b><i>Ken 'n punt toe as die bewering EN rede beide korrek is</i></b>

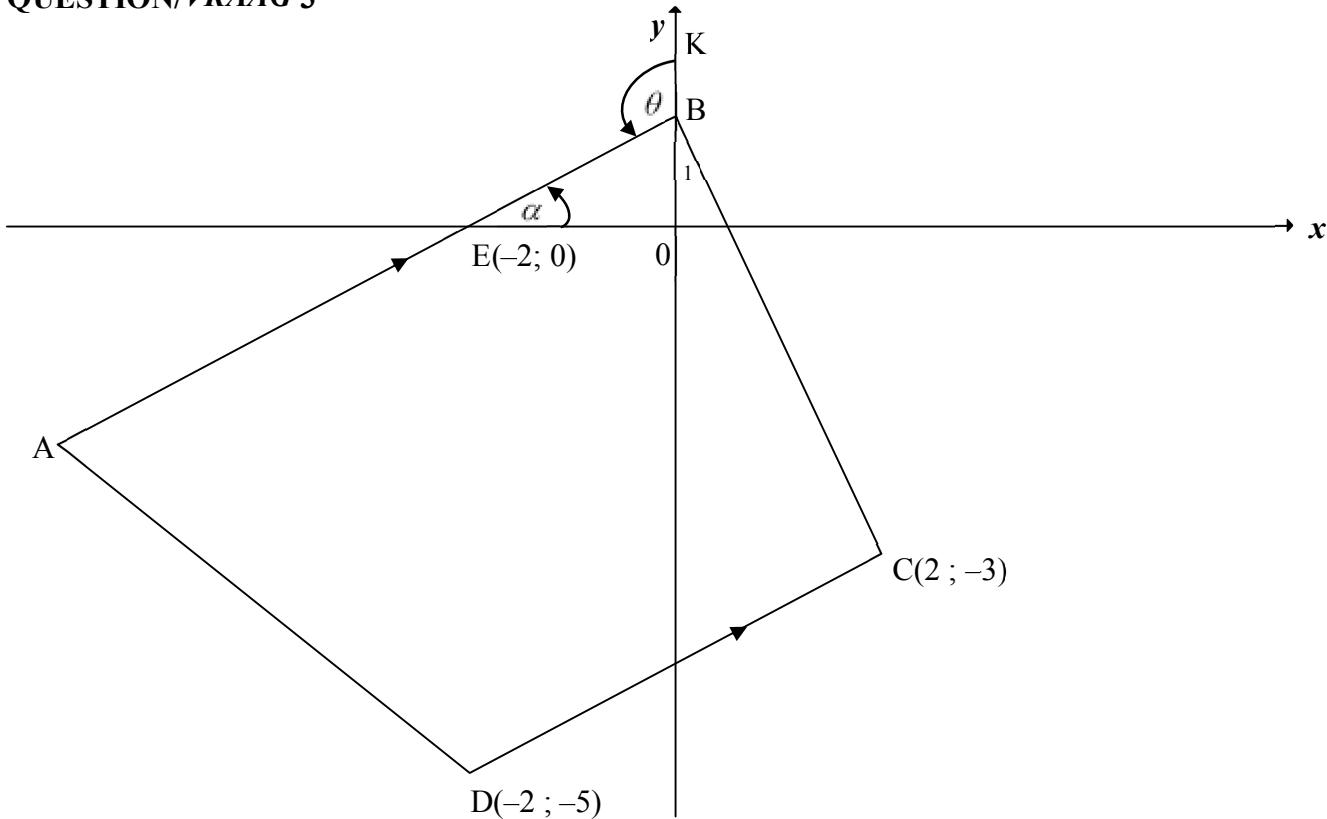
**QUESTION/VRAAG 1**

1.1	45 children	✓ answer (1)																								
1.2	$= \frac{\sum f_x}{n} = \frac{45}{6}$ $= \sum f_x (4 \times 2) + (8 \times 10) + (12 \times 9) + (16 \times 7) + (20 \times 8) + (24 \times 7) + (28 \times 2) x$ $x = \frac{692}{45}$ OR $x = 15,38$ minutes	<b>Answer only: full marks</b> ✓ 692 ✓ answer (2)																								
1.3	<table border="1"> <thead> <tr> <th>Time taken (<math>t</math>) (in minutes)</th> <th>Number of children</th> <th>Cumulative frequency</th> </tr> </thead> <tbody> <tr><td><math>2 &lt; t \leq 6</math></td><td>2</td><td>2</td></tr> <tr><td><math>6 &lt; t \leq 10</math></td><td>10</td><td>12</td></tr> <tr><td><math>10 &lt; t \leq 14</math></td><td>9</td><td>21</td></tr> <tr><td><math>14 &lt; t \leq 18</math></td><td>7</td><td>28</td></tr> <tr><td><math>18 &lt; t \leq 22</math></td><td>8</td><td>36</td></tr> <tr><td><math>22 &lt; t \leq 26</math></td><td>7</td><td>43</td></tr> <tr><td><math>26 &lt; t \leq 30</math></td><td>2</td><td>45</td></tr> </tbody> </table>	Time taken ( $t$ ) (in minutes)	Number of children	Cumulative frequency	$2 < t \leq 6$	2	2	$6 < t \leq 10$	10	12	$10 < t \leq 14$	9	21	$14 < t \leq 18$	7	28	$18 < t \leq 22$	8	36	$22 < t \leq 26$	7	43	$26 < t \leq 30$	2	45	✓ first 4 cum freq correct ✓ last 3 cum freq correct (2)
Time taken ( $t$ ) (in minutes)	Number of children	Cumulative frequency																								
$2 < t \leq 6$	2	2																								
$6 < t \leq 10$	10	12																								
$10 < t \leq 14$	9	21																								
$14 < t \leq 18$	7	28																								
$18 < t \leq 22$	8	36																								
$22 < t \leq 26$	7	43																								
$26 < t \leq 30$	2	45																								
1.4	<p style="text-align: center;"><b>CUMULATIVE FREQUENCY GRAPH (OGIVE)</b></p>	✓ plotting cum freq at upper limits correctly (all points) ✓ shape (smooth) ✓ grounding (2;0)																								

	<input type="text"/>	(3)
1.5	On graph at the $y$ -value of 22,5 or 23 Median = $\pm$ 15 minutes.  <input type="text"/> Answer only: full marks	✓ graph ✓ answer (2)
		[10]

**QUESTION/VRAAG 2**

2.1	$a = 12,44$ $b = 0,98$ $y = 12,44 + 0,98x$  <input type="text"/> Answer only: full marks	✓ value of $a$ ✓ value of $b$ ✓ equation (3)
2.2.1	$\frac{15}{50} \times 100$ Percentage = $= 30\%$	✓ answer (1)
2.2.2	$y^{\wedge} = 12,44 + 0,98x$ $= 12,44 + 0,98(30)$ $y^{\wedge} = 41,84$ $= 42$  <input type="text"/> Answer only: full marks  <b>OR</b> $y^{\wedge} = 41,87$ (if using calculator) $= 42$  <b>OR</b> $y^{\wedge} = \frac{21}{50}$	✓ substitution of 30  ✓ answer as integer  ✓ value of $y$ ✓ answer as integer  (2)  ✓ ✓ answer (2)
2.3.1	standard deviation = 13,88	✓ ✓ answer (2)
2.3.2	$x = 50,67 - 45,67$ $= 5\%$  <input type="text"/> Answer only: full marks	✓ 50,67 - 45,67 ✓ answer (2)
		[10]

**QUESTION/VRAAG 3**

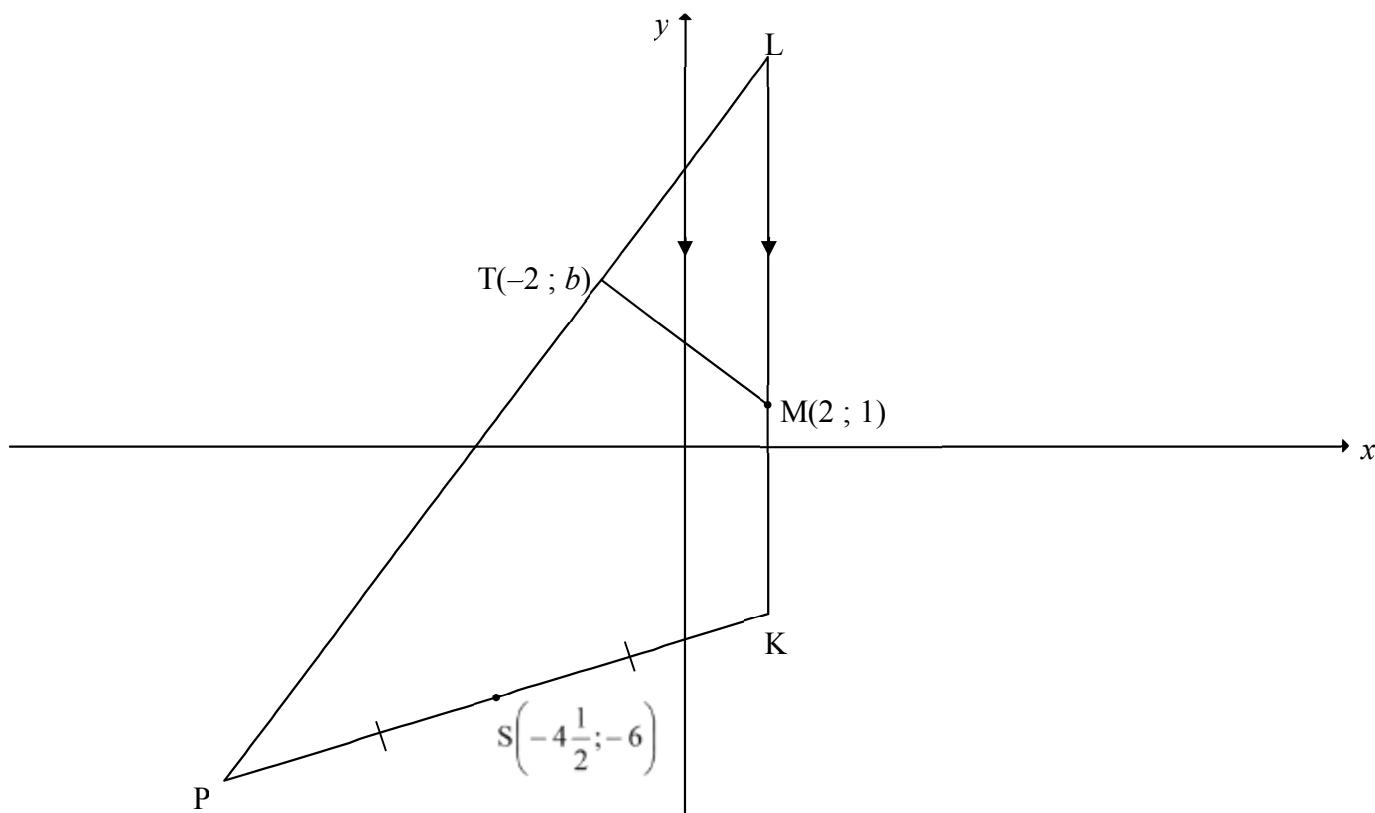
3.1.1	Midpoint of EC: $= \left( \frac{12+2}{2}, \frac{0+(-3)}{2} \right) = \left( 0, -\frac{3}{2} \right)$	✓ x value ✓ y value (2)
3.1.2	$m_{DC} = \frac{-3 - (-5)}{2 - (-2)}$ OR $\frac{-5 - (-3)}{-2 - 2}$ $= \frac{2}{4} = \frac{1}{2}$	✓ substitution  ✓ answer (2)
3.1.3	$m_{AB} = \frac{1}{2} = [AB \parallel DC]$ $y = \frac{1}{2}x + c$ $0 = \frac{1}{2}(-2) + c$ $c = 1$ $\therefore y = \frac{1}{2}x + 1$  <b>OR</b> $y - y_1 = \frac{1}{2}(x - x_1)$ $y - 0 = \frac{1}{2}(x - (-2))$	✓ $m_{AB} = \frac{1}{2}$  ✓ substitution of $(-2; 0)$  ✓ equation (3)

3.1.4	$\tan \alpha = \frac{1}{2} m_{AB}$ $\alpha = 26,57^\circ$ $\theta = 90^\circ + 26,57^\circ$ $= 116,57^\circ$ [ext $\angle$ of $\Delta$ ]	✓ $\tan \alpha = \frac{1}{2}$ ✓ value of $\alpha$ ✓ value of $\theta$ (3)
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3.2	B(0 ; 1) $m_{BC} = \frac{1 - (-3)}{0 - 2}$ OR $m_{BC} = \frac{(-3) - 1}{2 - 0}$ $= -2$ $= -2$ $m_{AB} \times m_{BC} = \frac{1}{2} \times -2$ $= -1$ $\therefore AB \perp BC$	✓ coordinates of B ✓ $m_{BC} = -2$ ✓ product of gradients = -1 (3)
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3.3.1	$\hat{AB} C = 90^\circ$ $\therefore EC$ is diameter [converse: $\angle$ in semi circle] $\therefore$ centre of circle = $\left(0; -\frac{3}{2}\right)$	✓ answer (1)
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3.3.2	$(x - 0)^2 + \left(y + \frac{3}{2}\right)^2 = r^2$ $(0 - 0)^2 + \left(0 + \frac{3}{2}\right)^2 = r^2$ or $(2 - 0)^2 + \left(-3 - \left(\frac{-3}{2}\right)\right)^2 = r^2$ or $R = \frac{EC}{2} = \frac{\sqrt{(2 - 2)^2 + (1 - (-3))^2}}{2}$ or $r = 1 - \left(\frac{-3}{2}\right)$ $r^2 = \frac{25}{4}$ or $r = \frac{5}{2}$ $x^2 + \left(y + \frac{3}{2}\right)^2 = \frac{25}{4}$	✓ substitution of centre ✓ correct substitution of E(-1 ; 0), B(0 ; 1) or C(2 ; -3) to calculate $r^2$ or $r$ ✓ value of $r^2$ or $r$ ✓ equation (4)
		[18]

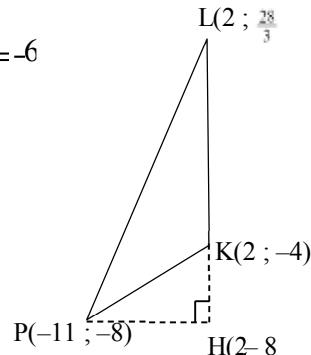
**QUESTION/VRAAG 4**

4.1	$(x-2)^2 + (y-1)^2 = 25$ $(-2-2)^2 + (b-1)^2 = 25$ $(b-1)^2 = 9$ <b>OR</b> $b-1 = \pm 3$ $\therefore b=4 \quad \text{or} \quad b=-2$	$(x-2)^2 + (y-1)^2 = 25$ $(-2-2)^2 + (b-1)^2 = 25$ $16 + b^2 - 2b + 1 = 25$ $b^2 - 2b - 8 = 0$ $\therefore b=4 \quad \text{or} \quad b=-2$	✓ equation of the circle ✓ substitution of point T ✓ simplification ✓ answer (4)
4.2.1	$K(2; 1-5)$ $\therefore K(2; -4)$	<input type="checkbox"/> Answer only: full marks	✓ $x$ value ✓ $y$ value (2)

4.2.2	$\frac{4-1}{2-2} = \frac{3}{4}$ $m_{MT} m_{PL} \quad [\text{radius } \perp \text{ tangent}]$ $= \frac{4}{3y} \quad c$ $= \frac{4}{3}x + \quad c$ $4 = \frac{4}{3}(-2) +$ $c = \frac{20}{3}y$ $c = \frac{4}{3}x + \frac{20}{3}$	<ul style="list-style-type: none"> <li>✓ <math>m_{MT}</math></li> <li>✓ <math>m_{PL} = \frac{4}{3}</math></li> <li>✓ substitution of <math>m_{PL}</math> and the point T</li> <li>✓ equation</li> </ul> <p>(4)</p>
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<b>OR</b> $m_{MT} = \frac{4-1}{-2-2} = -\frac{3}{4}$ $m_{PL} = \frac{4}{3} \quad [\text{radius } \perp \text{ tangent}] \quad y$ $-y_1 = \frac{4}{3}(x - x_1)$ $-4 = \frac{4}{3}(x + 2)$ $y = \frac{4}{3}x + \frac{20}{3}$ <b>OR</b> $P(-11; -8)$ $m_{PL} = \frac{4 - (-8)}{-2 - (-11)}$ $= \frac{4}{3}$ $y = \frac{4}{3}x + c$ $-8 = \frac{4}{3}x + c$ $c = \frac{20}{3}$ $y = \frac{4}{3}x + \frac{20}{3}$	<ul style="list-style-type: none"> <li>✓ <math>m_{MT}</math></li> <li>✓ <math>m_{PL} = \frac{4}{3}</math></li> <li>✓ substitution of <math>m_{PL}</math> and the point T</li> <li>✓ equation</li> </ul> <p>(4)</p> <ul style="list-style-type: none"> <li>✓ coordinates of P</li> <li>✓ <math>m_{PL} = \frac{4}{3}</math></li> <li>✓ substitution of <math>m_{PL}</math> and the point P or T</li> <li>✓ equation</li> </ul> <p>(4)</p>
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<p>4.2.3</p> $y_L = \frac{4}{3}(2) + \frac{20}{3} = \frac{28}{3}$ $L\left(2; \frac{28}{3}\right) \text{ and } K(2; 4)$ $LK = \frac{28}{3} - (-4)$ $= \frac{40}{3}$ <p><u>Coordinates of P:</u></p> $\frac{x+2}{2} = -4 \quad \text{and} \quad \frac{y-4}{2} = -6$ $\therefore x = -11 \quad y = -8$ $\therefore P(-11; -8)$ $\perp \text{height (PH)} = 2 - (-11) = 13$ $\text{Area } \Delta PKL = \frac{1}{2} LK \times PH$ $= \frac{1}{2} \left(\frac{40}{3}\right) \times (13)$ $= \frac{269}{3} \text{ OR } 86,67$	<p style="text-align: right;"><math>\checkmark \quad y = \frac{28}{3}</math></p> <p style="text-align: right;"><math>\checkmark \quad \text{length of LK}</math></p> <p style="text-align: right;"><math>\checkmark \quad x_P \quad \checkmark \quad y_P</math></p> <p style="text-align: right;"><math>\checkmark \quad \text{length of } \perp \text{ height}</math></p> <p style="text-align: right;"><math>\checkmark \quad \text{substitution into the area formula}</math></p> <p style="text-align: right;"><math>\checkmark \quad \text{answer}</math></p> <p style="text-align: right;">(7)</p>
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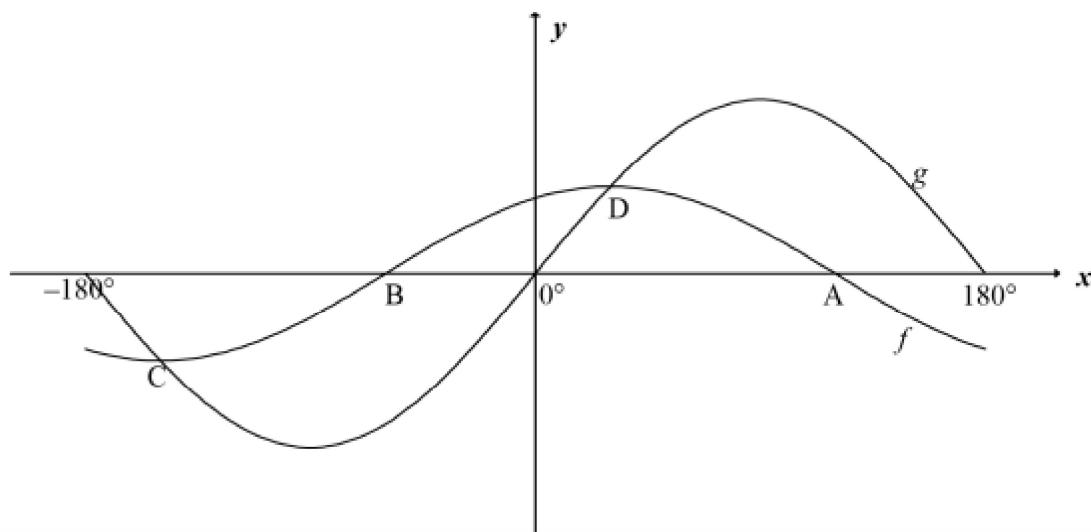
4.2.3	<p><b>OR</b></p> $y_L = \frac{4}{3}(2) + \frac{20}{3} = \frac{28}{3}$ $L\left(2; \frac{28}{3}\right) \text{ and } K(2; 4)$ $LK = \frac{28}{3} - (-4)$ $= \frac{40}{3}$ <p><u>Coordinates of P:</u></p> $\frac{x+2}{2} = -4 \quad \text{and} \quad \frac{y-4}{2}$ $\therefore x = -11 \quad y = -8$ $\therefore P(-11; -8)$ $PK^2 = \sqrt{(-11 - 2)^2 + (-8 - (-4))^2}$ $PK = \sqrt{185} \text{ units}$ $m_{PK} = \frac{-8 - (-4)}{-11 - 2} = \frac{4}{13}$ $\tan \theta = \frac{4}{13} \quad \therefore \theta = 17,1027\dots^\circ$ $\therefore \hat{P}K L = 90^\circ + 17,1027\dots^\circ = 107,1^\circ$ $\text{Area } \Delta PKL = \frac{1}{2} LK \times LK \sin \hat{P}KL$ $= \frac{1}{2} \left(\frac{40}{3}\right) \times \left(\sqrt{185}\right) \sin 107,1^\circ$ $= \frac{269}{3} \quad \text{OR } 86,67$	$\checkmark y_L = \frac{28}{3}$ $\checkmark \text{ length of LK}$ $\checkmark x_P \checkmark y_P$ $\checkmark \hat{P}K L$ $\checkmark \text{ substitution into the area rule}$ $\checkmark \text{ answer}$ (7)
4.3	<p>The centres of the two circles lie on the same vertical line <math>x = 2</math>, and the sum of the radii = 10</p> $n-1 = 10 \quad 1-n = 10$ <p style="text-align: center;">or</p> $n=11 \quad n = -9$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin-left: auto; margin-right: auto;">Answer only: full marks</div>	$\checkmark \text{ correct method}$ $\checkmark \text{ sum of radii} = 10$ $\checkmark n=11 \checkmark n= -9$ (4)
		[21]

**QUESTION/VRAAG 5**

5.1.1	$\sin 191^\circ$ $= -\sin 11^\circ$	$\checkmark -\sin 11^\circ$ (1)
5.1.2	$\cos 22^\circ$ $= \cos(2 \times 11^\circ)$ $= 1 - 2\sin^2 11^\circ$	$\checkmark$ answer (1)
5.2	$\cos(x-180^\circ) + \sqrt{2} \sin(x+45^\circ)$ $= -\cos x + \sqrt{2}(\sin x \cos 45^\circ + \cos x \sin 45^\circ)$ $= -\cos x + \sqrt{2} \left( \sin x \left( \frac{1}{\sqrt{2}} \right) + \cos x \left( \frac{1}{\sqrt{2}} \right) \right)$ $= -\cos x + \sin x + \cos x$ $= \sin x$	$\checkmark -\cos x$ $\checkmark$ expansion $\checkmark$ special angle ratios $\checkmark$ simplification of last 2 terms $\checkmark$ answer (5)
<b>OR</b>		
	$\cos(x-180^\circ) + \sqrt{2} \sin(x+45^\circ)$ $= -\cos x + \sqrt{2}(\sin x \cos 45^\circ + \cos x \sin 45^\circ)$ $= -\cos x + \sqrt{2} \left( \sin x \left( \frac{\sqrt{2}}{2} \right) + \cos x \left( \frac{\sqrt{2}}{2} \right) \right)$ $= -\cos x + \sin x + \cos x$ $= \sin x$	$\checkmark -\cos x$ $\checkmark$ expansion $\checkmark$ special angle ratios $\checkmark$ simplification of last 2 terms $\checkmark$ answer (5)
5.3	$\sin P + \sin Q = \sin P + \cos P$ $(\sin P + \cos P)^2 = \left(\frac{7}{5}\right)^2$ $\sin^2 P + 2 \sin P \cos P + \cos^2 P = \frac{49}{25}$ $2 \sin P \cos P = \frac{49}{25} - 1$ $\sin 2P = \left(\frac{49}{25} - \frac{25}{25}\right)$ $= \frac{24}{25}$	$\checkmark \sin Q = \cos P$ $\checkmark$ squaring $\checkmark$ expansion $\checkmark \sin^2 P + \cos^2 P = 1$ $\checkmark$ answer (5)
		[12]

**QUESTION/VRAAG 6**

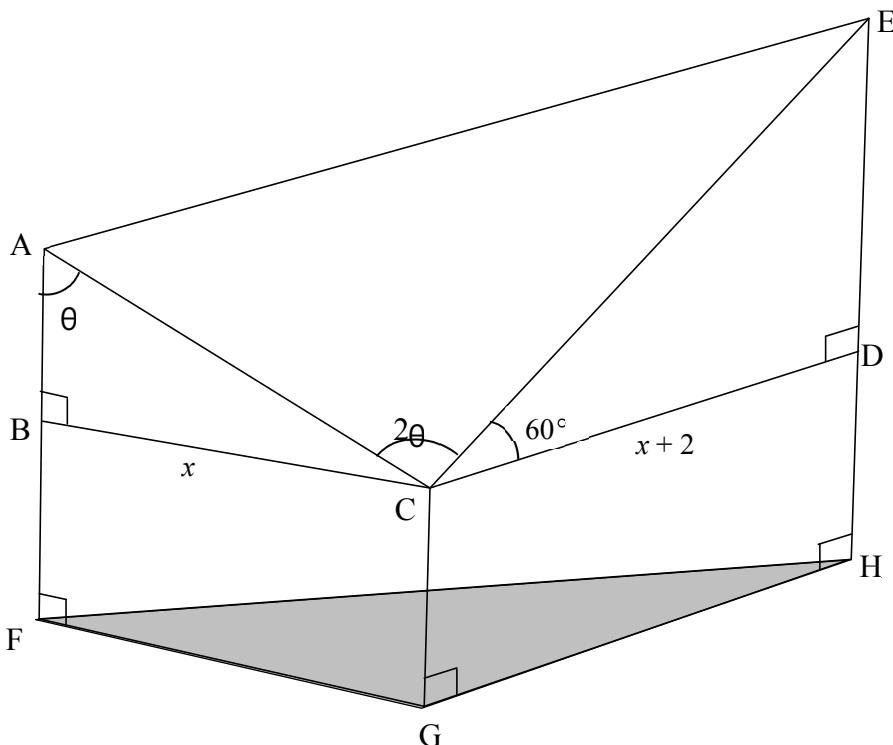
6.1	$\cos(x-30^\circ) = 2\sin x \cos x \cos 30^\circ + \sin x \sin 30^\circ$ $\frac{\sqrt{3}}{2} \sin x \cos 30^\circ = 2\sin x \cos x + \frac{1}{2} \sin x =$ $\frac{\sqrt{3}}{2} \sin x = 2\sin x \cos x + \frac{1}{2} \sin x$ $\frac{\sqrt{3}}{2} = 2\cos x + \frac{1}{2}$ $\tan x = 3$ $x = 30^\circ + k \cdot 180^\circ; k \in \mathbb{Z}$ <p><b>OR</b></p> $x = 30^\circ + k \cdot 360^\circ \text{ or } x = 210^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$	✓ expansion ✓ special $\angle$ s ✓ simplification ✓ equation in tan ✓ $30^\circ$ ✓ $k \cdot 180^\circ; k \in \mathbb{Z}$ <b>OR</b> ✓ $30^\circ$ and $210^\circ$ ✓ $k \cdot 360^\circ; k \in \mathbb{Z}$ (6)
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6.2.1(a)	A( $120^\circ ; 0$ )	✓ answer (1)
6.2.1(b)	C( $-150^\circ ; -1$ )	✓ x value ✓ y value (2)
6.2.2(a)	$x \in (-90^\circ ; 30^\circ)$ OR $-90^\circ < x < 30^\circ$	✓ endpoints ✓ correct interval (2)
6.2.2(b)	$x \in (-160^\circ ; 20^\circ)$ OR $-160^\circ < x < 20^\circ$	✓ endpoints ✓ correct interval (2)
6.2.3	$y = 2^{2 \sin x + 3}$ Range of $y = 2 \sin x$ : $y \in [-2 ; 2]$ OR $-2 \leq y \leq 2$ Range of $y = 2 \sin x + 3$ : $y \in [1 ; 5]$ OR $1 \leq y \leq 5$ Range: $y = 2^{2 \sin x + 3}$ : $y \in [2 ; 32]$ OR $2 \leq y \leq 32$ <div style="border: 1px solid black; padding: 2px; text-align: center;">Answer only: full marks</div>	✓ 1 ✓ 5 ✓ 2 ✓ 32 ✓ correct interval (5)
		[18]

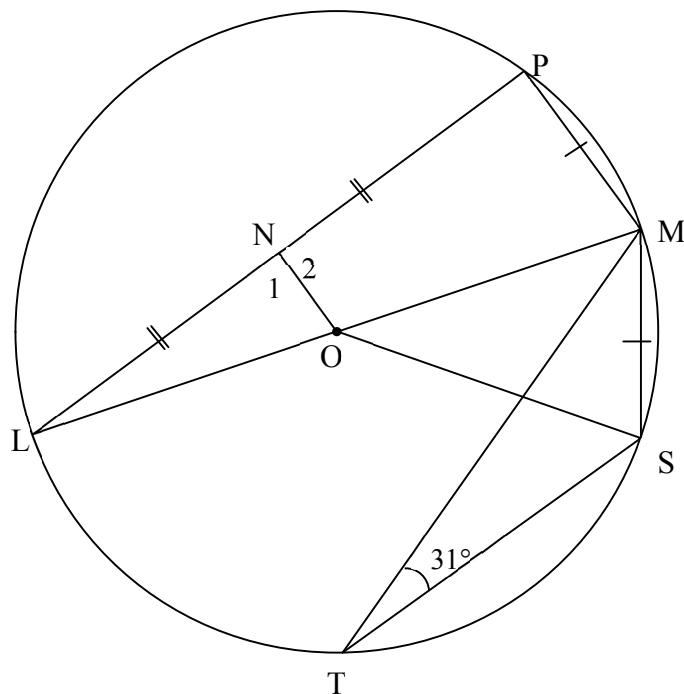
7.1.1	$\sin\theta = \frac{x}{AC}$ $\frac{\sin\theta}{x} = \frac{\sin 90^\circ}{AC}$ <b>OR</b> $AC = \frac{x}{\sin\theta}$	✓ trig ratio ✓ simplification (2)
7.1.2	$\cos 60^\circ = \frac{x+2}{CE}$ $\frac{\sin 30^\circ}{x+2} = \frac{\sin 90^\circ}{CE}$ <b>OR</b> $x+2$ $CE = \frac{x+2}{\sin 30^\circ}$ $= 2(x+2)$ $\frac{1}{2} = 2(x+2)$	✓ trig ratio ✓ making CE the subject (2)
7.2	$\text{Area } \Delta ACE = \frac{1}{2} AC \cdot EC \cdot \sin \hat{A}CE$ $= \frac{1}{2} x (2(x+2)) \sin 2\theta$ $= \frac{x(2(x+2)) \sin 2\theta}{2 \sin \theta}$ $= \frac{x(2(x+2)) \sin 2\theta}{\sin \theta}$	✓ use area rule correctly ✓ substitution of $\frac{x(2(x+2))}{\sin \theta}$ ✓ substitution of $\sin 2\theta$ (3)

	$= 2x(x+2)\cos\theta$	
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7.3	$\begin{aligned} EC &= 2(12 + 2) = 28 \\ AE^2 &= AC^2 + EC^2 - 2AC \cdot EC \cos \angle ACE \\ &= \left(\frac{12}{\sin 55^\circ}\right)^2 + 28^2 - 2\left(\frac{12}{\sin 55^\circ}\right) \cdot 28 \cos 110^\circ \\ \text{so} \\ AE &= 35,77m \end{aligned}$	<ul style="list-style-type: none"> <li>✓ EC</li> <li>✓ use cosine rule correctly</li> <li>✓ substitution</li> <li>✓ answer</li> </ul> <p>(4)</p>
		[11]

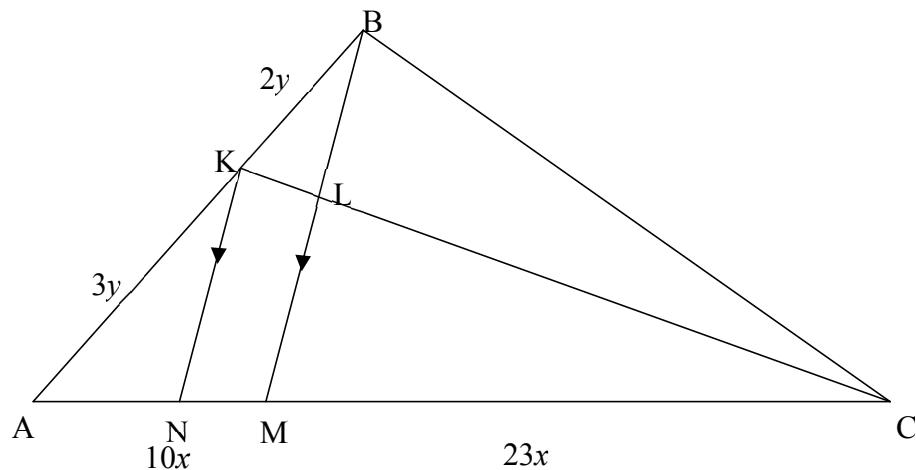
8.1



8.1.1(a)	$\hat{MS} = 62^\circ$ [ $\angle \text{at centre} = 2 \times \angle \text{at circumf/middelpnts} \angle = 2\text{omtreks} \angle$ ]	✓ S ✓ R (2)
8.1.1(b)	$\hat{L} = 31^\circ$ [equal chords; equal $\angle s$ / = koorde; = $\angle e$ ]	✓ S ✓ R (2)
8.1.2	<p><math>LN = NP</math> and <math>LO = OM</math></p> $\therefore ON = \frac{1}{2} PM$ <p>[ midpoint theorem/middelpuntstelling]</p> $\therefore ON = \frac{1}{2} MS$ <p>[<math>PM = MS</math>]</p> <p><b>OR</b></p> <p><math>\hat{N} = 90^\circ</math> [line from centre to midpt chord/lyn v midpt na midpt kd]</p> <p><math>\hat{P} = 90^\circ</math> [<math>\angle</math> in semi-circle/<math>\angle</math> in halfsirkel]</p> <p><math>\hat{L}</math> is common/gemeen</p> <p><math>\therefore \Delta NLO \parallel \Delta PLM (\angle \angle \angle)</math></p> $\frac{NL}{PL} = \frac{NO}{PM} = \frac{1}{2}$ $\therefore ON = \frac{1}{2} PM$	✓ LO = OM  ✓ S ✓ R  ✓ S  ✓ S/R  ✓ S  (4)

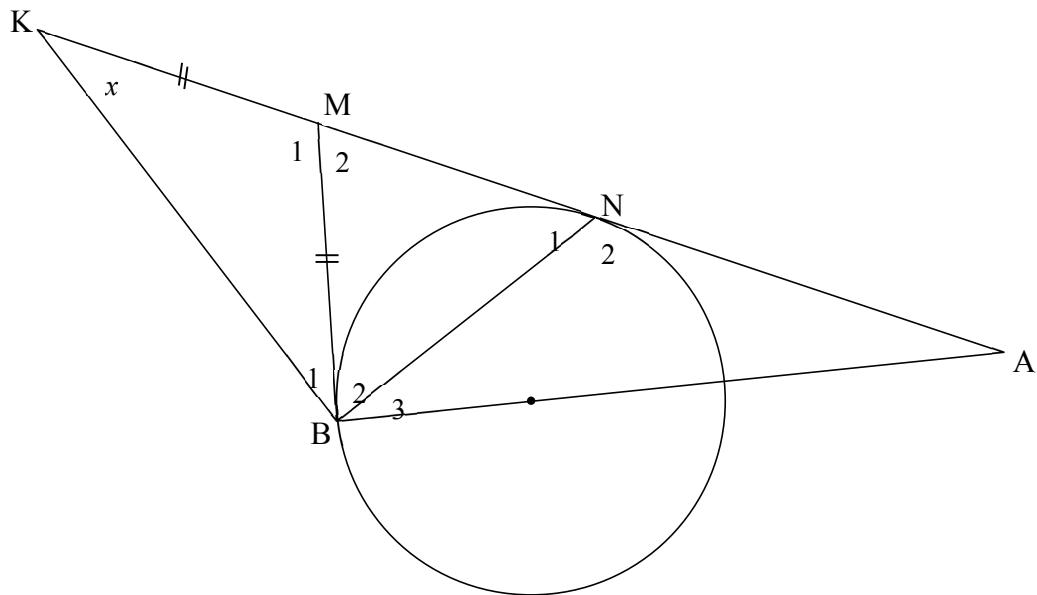
	$\therefore \text{ON} = \frac{1}{2} \text{MS}$ [PM = MS] b	✓ S
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8.2



8.2.1	$\frac{AN}{AM} = \frac{AK}{AB}$ [line $\parallel$ one side of $\Delta OR$ prop theorem; $KN \parallel BM$ / $\frac{AN}{AM} = \frac{3y}{5y} = \frac{3}{5}$ <i>lyn <math>\parallel</math> sy van <math>\Delta OR</math> eweredigheidst; <math>KN \parallel BM</math></i>	✓ R
	$\frac{AN}{AM} = \frac{3}{5}$	✓ S (2)

8.2.2	<p>AM <math>\frac{10x}{\underline{\hspace{1cm}}}</math> <math>\underline{\hspace{1cm}} = \underline{\hspace{1cm}}</math> [given]</p> <p>MC <math>\frac{23x}{\underline{\hspace{1cm}}}</math></p> <p><math>AM = 5y = 10x \therefore y = 2x</math></p> <p>LC MC</p> <p><math>\frac{\underline{\hspace{1cm}}}{KL} = \frac{\underline{\hspace{1cm}}}{NM}</math> [line    one side of <math>\Delta</math> OR prop theorem; KN    LM/</p> <p><math>\frac{23x}{2y} = \frac{23x}{4x} = \frac{23}{4}</math></p> <p><b>OR</b></p> <p>AM <math>\frac{10x}{\underline{\hspace{1cm}}}</math> <math>\underline{\hspace{1cm}} = \underline{\hspace{1cm}}</math> [given]</p> <p>MC <math>\frac{23x}{\underline{\hspace{1cm}}}</math></p> <p>AN <math>\frac{3y}{\underline{\hspace{1cm}}} = \frac{6x}{\underline{\hspace{1cm}}}</math></p> <p><math>\frac{MN}{2y} = \frac{23x}{4x}</math></p> <p>LC MC</p> <p><math>\frac{\underline{\hspace{1cm}}}{KL} = \frac{\underline{\hspace{1cm}}}{NM}</math> [line    one side of <math>\Delta</math> OR prop theorem; KN    LM/</p> <p><math>\frac{23x}{2y} = \frac{23x}{4x} = \frac{23}{4}</math></p>	<p>✓ S</p> <p>✓ R</p> <p>✓ S (3)</p> <p>✓ S</p> <p>✓ R</p> <p>✓ S (3)</p>
		[13]

**9**

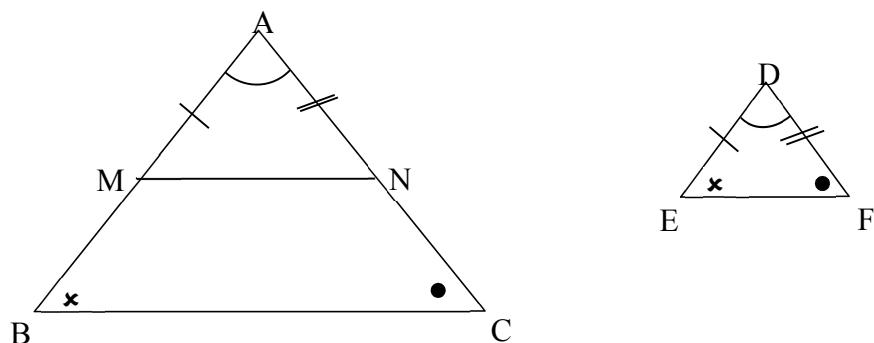
9.1	$B^\circ_1 = x$ [∠'s opp = sides/∠e teenoor = sye] $M^\circ_2 = 2x$ [ext ∠ of Δ] OR $M^\circ_1 = 180^\circ - 2x$ [∠s of Δ] $BM = MN$ [2 tans from a common point/raaklyne vanuit dieselfde punt] $N^\circ_1 = \frac{180^\circ - 2x}{2} = 90^\circ - x$ [∠'s opp = sides/∠e teenoor = sye] <b>OR</b> $NM = BM$ [2 tans from a common point/raaklyne vanuit dieselfde punt] $B^\circ_2 = N^\circ_1$ [∠'s opp = sides/∠e teenoor = sye] $B^\circ_1 = x$ [∠'s opp = sides/∠e teenoor = sye] In $\Delta KBN:$ $x + x + B^\circ_2 + N^\circ_1 = 180^\circ$ [sum of ∠'s of Δ] $2x + 2N^\circ_1 = 180^\circ$ $x + N^\circ_1 = 90^\circ$ $N^\circ_1 = 90^\circ - x$	✓S ✓S ✓R ✓S ✓R ✓answer ✓S ✓R ✓S ✓R ✓S ✓answer
		(6)

9.2	$\text{MB}^{\wedge} \text{A} = \text{B}^{\wedge} 2 + \text{B}^{\wedge} 3 = 90^{\circ} \text{ [tangent } \perp \text{diameter / raaklyn } \perp \text{ middellyn]}$ $\text{B}^{\wedge} 3 = 90^{\circ} - \text{B}^{\wedge} 2$ $= 90^{\circ} - (90^{\circ} - x) = x$ $\text{B}^{\wedge} 3 = \text{K}^{\wedge} = x$ <p><math>\therefore \text{AB}</math> is a tangent / <i>raaklyn</i> converse tan-chord theorem / <i>omgekeerde raakl koordst]]</i></p>	$\checkmark \text{S } \checkmark \text{R}$ $\checkmark \text{S}$ $\checkmark \text{S}$ $\checkmark \text{R}$ (5)
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	<b>OR</b> $\text{B}^{\wedge} 2 = \text{N}^{\wedge} 1$ $\text{B}^{\wedge} 1 + \text{B}^{\wedge} 2 = x + (90^{\circ} - x) = 90^{\circ}$ <p><math>\therefore \text{KN}</math> is diameter / <i>middellyn</i> [converse <math>\angle</math> in semi-circle / <i>omgekeerde <math>\angle</math> in halfsirkel</i>]</p> $\text{MB}^{\wedge} \text{A} = \text{B}^{\wedge} 2 + \text{B}^{\wedge} 3 = 90^{\circ} \quad [\text{tangent } \perp \text{diameter}]$ <p><math>\therefore \text{AB}</math> is a tangent / <i>raaklyn</i> converse tan-chord theorem / <i>omgekeerde raakl koordst]]</i></p>	$\checkmark \text{S}$ $\checkmark \text{R}$ $\checkmark \text{S } \checkmark \text{R}$ $\checkmark \text{R}$ (5)
		[11]

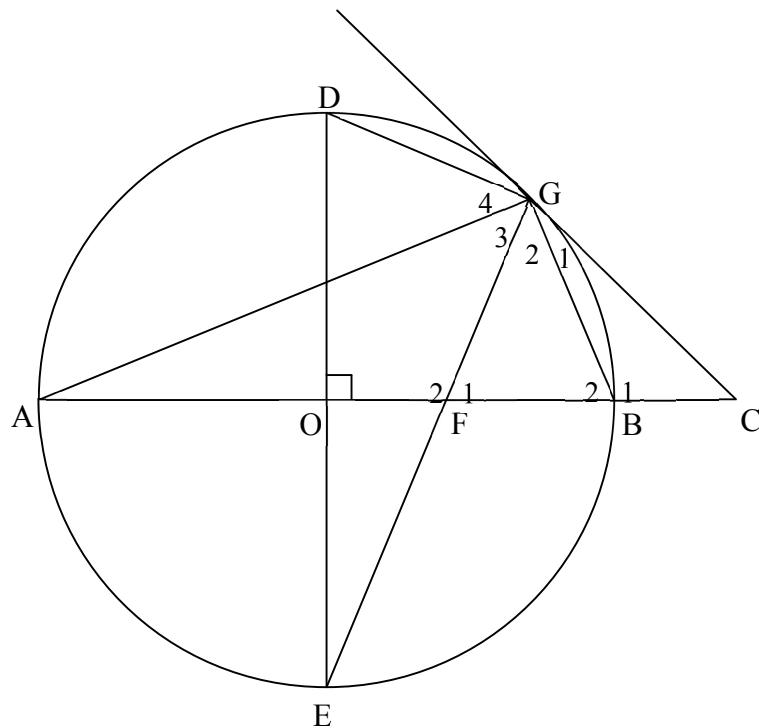
**QUESTION 10**

10.1



10.1	<p>Constr: Let M and N lie on AB and AC respectively such that <math>AM = DE</math> and <math>AN = DF</math>. Draw MN.</p> <p><i>Konst: Merk M en N op AB en AC onderskeidelik af sodanig dat <math>AM = DE</math> en <math>AN = DF</math>. Verbind MN.</i></p> <p>Proof:</p> <p>In <math>\triangle AMN</math> and <math>\triangle DEF</math></p> <p><math>AM = DE</math> [Constr]</p> <p><math>AN = DF</math> [Constr]</p> <p><math>\hat{A} = \hat{D}</math> [Given]</p> <p><math>\therefore \triangle AMN \cong \triangle DEF</math> (SAS)</p> <p><math>\therefore \hat{AM} = \hat{N} = \hat{E} = \hat{B}</math></p> <p><math>MN \parallel BC</math> [corresp <math>\angle</math>'s are equal/ooreenkomsige <math>\angle</math>e =]</p> <p><math>\frac{AB}{AC} = \frac{AM}{AN}</math> [line <math>\parallel</math> one side of <math>\triangle</math> OR prop theorem; <math>MN \parallel BC</math>] <math>AM \parallel AN</math></p> <p><math>\therefore \frac{AB}{AC} = \frac{AM}{AN}</math> [AM=DE and AN=DF]</p>	<p>✓ Constr / Konstr</p> <p>✓ <math>\triangle AMN \cong \triangle DEF</math></p> <p>✓ SAS</p> <p>✓ <math>MN \parallel BC</math> and R</p> <p>✓ <math>\frac{AB}{AC} = \frac{AM}{AN}</math> ✓R</p>
		(6)

10.2



10.2.1(a)	$\hat{DOB} = 90^\circ$ $\hat{DGF} = \hat{G}_3 + \hat{G}_4 = 90^\circ$ [angle in semi-circle/ <i>∠ in halfsirkel</i> ] $\hat{DOB} + \hat{DGF} = 180^\circ$ $\therefore$ DGFO is a cyclic quad. [converse: opp ∠s of cyclic quad/ <i>omgekeerde teenoorst ∠e v koordevh</i> ] OR $\angle s \text{ of quad} = 180^\circ / \angle e \text{ van koordevh} = 180^\circ$ OR $\hat{EOB} = 90^\circ$ $\hat{DGF} = \hat{G}_3 + \hat{G}_4 = 90^\circ$ [angle in semi-circle/ <i>∠ in halfsirkel</i> ] $\hat{EOB} = \hat{DGF}$ $\therefore$ DGFO is a cyclic quad. . . [converse: ext ∠ = opp int ∠/ <i>omgekeerde buite ∠ = teenoorst ∠</i> ] OR $\text{ext } \angle \text{ of quad} = \text{opp int } \angle / \text{buite } \angle \text{ v vh} = \text{teenoorst } \angle$	✓ S ✓ R  ✓ R  ✓ S ✓ R (3)  ✓ R (3)
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10.2.1(b)	$F^\wedge_1 = D^\wedge$ [ext $\angle$ of cyclic quad/buite $\angle$ v koordevh]  $G^\wedge_1 + G^\wedge_2 = D^\wedge$ [tan-chord theorem/raakl koordst]  $\therefore F^\wedge_1 = G^\wedge_1 + G^\wedge_2$  $\therefore GC = CF$ [sides opp equal $\angle$ s/sye teenoor = $\angle e$ ]	✓ S ✓ R ✓ S ✓ R  ✓ R (5)
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10.2.2(a)	$\begin{aligned} AB &= DE = 14 & [\text{diameters}/\text{middellyne}] \\ \therefore OB &= 7 \text{ units} \\ \therefore BC &= OC - OB = 11 - 7 \\ &\quad = 4 \text{ units} \end{aligned}$ <p style="border: 1px solid black; padding: 5px; display: inline-block;">Answer only: full marks</p>	<span style="color: green;">✓ S</span> <span style="color: green;">✓ S</span> <span style="color: green;">✓ S</span> <span style="color: green;">(3)</span>
10.2.2(b)	<p>In <math>\Delta CGB</math> and <math>\Delta CAG</math> ]</p> $\begin{aligned} G^\wedge &= A^\wedge = x & [\text{tan-chord theorem}/\text{raakkoords}] \\ C^\wedge &= C^\wedge & [\text{common}] AG \\ \Delta CGB &\parallel\Delta CAG & \angle, \angle, \angle \\ \frac{CG}{CB} &= \frac{CA}{CG} \\ \frac{CG}{4} &= \frac{CA}{CG} \\ \frac{18}{CG} &= \frac{CA}{CG} \quad \text{or } 6\sqrt{or} 8,49 \text{ units} \\ CG^2 &= 72 \\ CG &= \sqrt{72} \end{aligned}$	<span style="color: green;">✓ S/R</span> <span style="color: green;">✓ S</span> <span style="color: green;">✓ S</span> <span style="color: green;">✓ CA = 18</span> <span style="color: green;">✓ answer</span> <span style="color: green;">(5)</span>
10.2.2(c)	$\begin{aligned} OF &= OC - FC \\ &= \sqrt{72} \quad 11 - \\ \tan E &= \frac{OF}{OE} \\ &= \frac{\sqrt{72}}{7} \\ &= 0,36 \\ E^\wedge &= 19,76^\circ \end{aligned}$ <p><b>OR</b></p> $\begin{aligned} OF &= OC - FC \\ &= 11 - \sqrt{72} \\ FE^2 &= OE^2 + OF^2 \\ &= 7^2 + (11 - \sqrt{72})^2 \\ FE &= 7,437.. = 7,44 \\ \cos E &= \frac{OE}{FE} \\ &= \frac{7}{7,44} \end{aligned}$ <p style="text-align: right;"><math>E^\wedge = 19,76^\circ = 0,338</math></p>	<span style="color: green;">✓ OF</span> <span style="color: green;">✓ trig ratio</span> <span style="color: green;">✓ substitution</span> <span style="color: green;">✓ answer</span> <span style="color: green;">(4)</span>

	$= \frac{7}{7,44} = 0,94$ $\hat{E} = 19,76^\circ$	<ul style="list-style-type: none"><li>✓ substitution</li><li>✓ answer</li></ul> (4)
		[26]

	<b>TOTAL/TOTAAL:</b>	<b>150</b>
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