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GRADE/GRAAD 12

SEPTEMBER 2022

**TECHNICAL MATHEMATICS P2/TEGNIESE WISKUNDE V2
MARKING GUIDELINE/NASIENRIGLYN**

MARKS/PUNTE: 150

This marking guideline consists of 18 pages./
Hierdie nasienriglyn bestaan uit 18 bladsye.

NOTE:

- Continuous accuracy (CA) applies only where indicated in this marking guideline.
- Assuming values/answers in order to solve a problem is unacceptable.

LET WEL:

- *Volgehoue akkuraatheid (CA) is slegs van toepassing soos aangedui in hierdie nasienriglyn.*
- *Aanvaarding van waardes/antwoorde om 'n problem op te los, is onaanvaarbaar.*

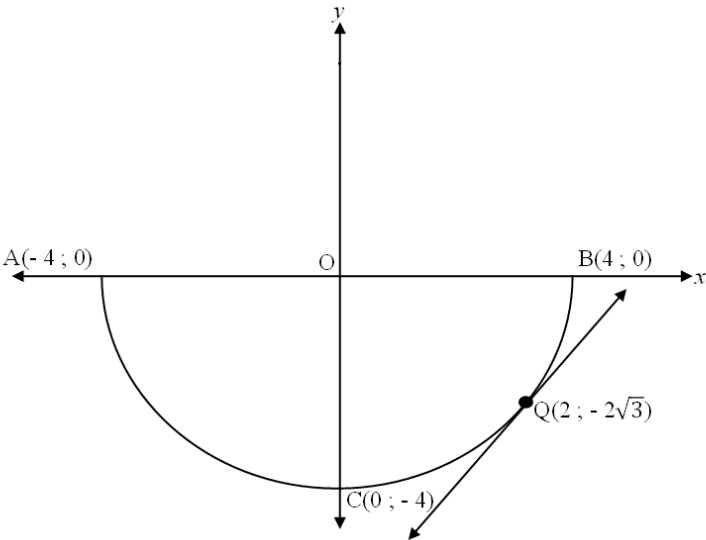
MARKING CODES / NASIENKODES	
M	Method / Metode
A	Accuracy / Akkuraatheid
AO	Answer only / Slegs antwoord
CA	Consistent accuracy / Deurlopende akkuraatheid
F	Formula / Formule
I	Identity / Identiteit
R	Rounding / Afronding
S	Simplification / Vereenvoudiging
ST	Statement / Bewering
RE	Reason / Rede
ST RE	Statement and correct reason / Bewering en korrekte rede
SF	Substitution correctly in correct formula / Korrekte vervanging in die korrekte formule
NPU	No penalty for omitting units / Geen penalisering vir eenhede uitgelaat

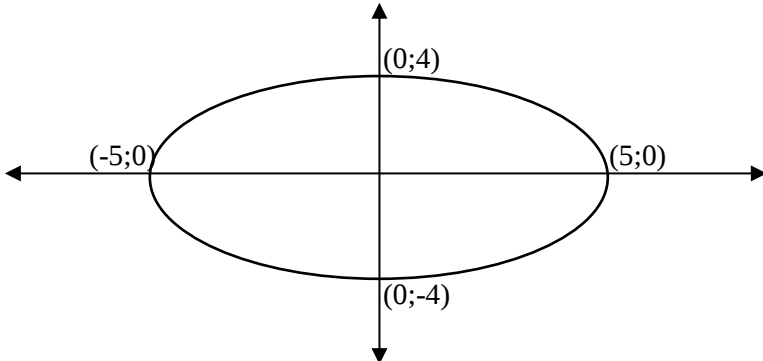
QUESTION/VRAAG 1

1.1	$m_{AD} = \frac{y_2 - y_1}{x_2 - x_1}$ $m_{AD} = \frac{4 - 0}{0 - (-1)}$ $m_{AD} = 4$	✓ SF A ✓ 4 CA (2)
	AO: Full marks / Volpunte	
1.2	$\tan \theta = m_{AD}$ $\tan \theta = 4$ $\theta = \tan^{-1}(4)$ $\theta = 75,96^\circ \approx 76^\circ$	✓ F A ✓ SF CA ✓ 76° CA (3)
1.3	$P\left(\frac{7+6}{2}; \frac{0+(-4)}{2}\right)$ $P\left(\frac{13}{2}; -2\right)$ $P\left(\frac{13}{2}; -2\right)$	✓ SF A ✓ $\left(\frac{13}{2}; -2\right)$ CA (2)
1.4	$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $AB = \sqrt{(0 - 7)^2 + (4 - 0)^2}$ $AB = \sqrt{65}$	✓ SF A ✓ $\sqrt{65}$ CA (2)
	AO: Full marks / Volpunte	

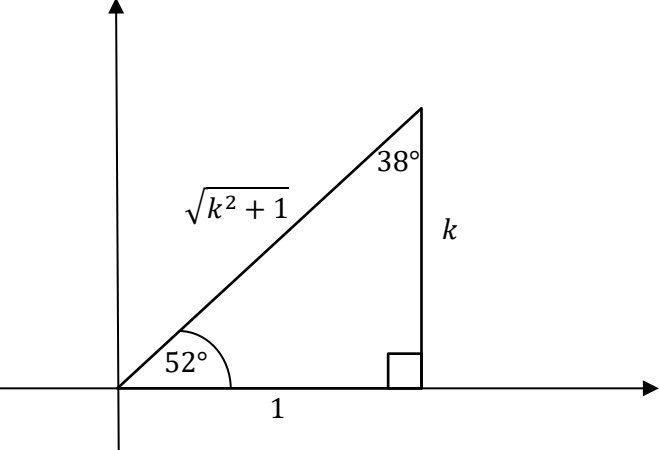
1.5	$m_{BC} = \frac{0-(-4)}{7-6}$ $m_{BC} = 4$	OR/ OF	$m_{BC} = 4$ ($\parallel$ lines / lyne)	$\checkmark m_{\perp} = -\frac{1}{4}\text{CA}$ $\checkmark \text{sub}\left(\frac{13}{2}; -2\right) \text{CA}$ $\checkmark y = -\frac{1}{4}x - \frac{3}{8} \text{A}$ (3)
	$\therefore m_{\perp} = -\frac{1}{4}$ $\therefore y = -\frac{1}{4}x + c$ $\left(\frac{13}{2}; -2\right) : -2 = -\frac{1}{4}\left(\frac{13}{2}\right) + c$ $\therefore -2 = -\frac{13}{8} + c$ $\therefore -\frac{3}{8} = c$ $\therefore y = -\frac{1}{4}x - \frac{3}{8}$		$\therefore m_{\perp} = -\frac{1}{4}$ $\therefore y - y_1 = -\frac{1}{4}(x - x_1)$ $\left(\frac{13}{2}; -2\right) : y - (-2) = -\frac{1}{4}\left(x - \frac{13}{2}\right)$ $\therefore y + 2 = -\frac{1}{4}x + \frac{13}{8}$ $\therefore y = -\frac{1}{4}x + \frac{13}{8} - 2$ $\therefore y = -\frac{1}{4}x - \frac{3}{8}$	
				[12]

QUESTION/VRAAG 2

2.1		
2.1.1	$y = -\sqrt{r^2 - x^2}$ $y = -\sqrt{(-4)^2 - x^2}$ $y = -\sqrt{16 - x^2}$	$\checkmark \text{SF} \quad \text{A}$ $\checkmark \text{Simplification/ Vereenv. CA}$ $\checkmark y = -\sqrt{16 - x^2} \text{CA}$ (3)
2.1.2	$m_{OQ} = \frac{y_2 - y_1}{x_2 - x_1}$ $m_{OQ} = \frac{0 - (-2\sqrt{3})}{0 - 2}$ $m_{OQ} = -\sqrt{3}$	$\checkmark \text{SF} \quad \text{A}$ $\checkmark m_{OQ} = -\sqrt{3}$ CA (2)

2.1.3	$m_{tangent} = \frac{1}{\sqrt{3}}$ $\therefore y = \frac{1}{\sqrt{3}}x + c$ $(0; -5) : -5 = \frac{1}{\sqrt{3}}(0) + c$ $-5 = c$ $\therefore y = \frac{1}{\sqrt{3}}x - 5$ OR/OF	$m_{tangent} = \frac{1}{\sqrt{3}}$ $\therefore y = \frac{1}{\sqrt{3}}x + c$ $(0; -5)$ implies $c = -5$ $\therefore y = \frac{1}{\sqrt{3}}x - 5$	$\checkmark \frac{1}{\sqrt{3}}$ A $\checkmark y = \frac{1}{\sqrt{3}}x - 5$ CA (2)
2.2.1		$\checkmark$ elliptical shape with horizontal axis as major axis / <i>Elliptiese vorm met groter-as as die horisontale-as</i> A $\checkmark$ x-intercepts/ x-afsnitte A $\checkmark$ y-intercepts/y-afsnitte A (3)	
2.2.2	Length of major axis/Lengte van lang-as = $5 - (-5) = 10$ units / eenheid.	$\checkmark$ 10 CA (1)	[11]

QUESTION/VRAAG 3

3.1.1	$\sin(38,9^\circ) + \cos(153,2^\circ)$ $= 1,22$	✓ SF A ✓ 1,22 A (2)
3.1.2	$\sec\left(\frac{38,9^\circ}{3} + 153,2^\circ\right)$ $= \frac{1}{\cos\left(\frac{38,9^\circ}{3} + 153,2^\circ\right)}$ $= -1,03$	✓ SF A ✓ reciprocal ratio / <i>resiprook verh.</i> A ✓ - 1,03 A (3)
3.2.1	 $\therefore \cos 52^\circ = \frac{1}{\sqrt{k^2 + 1}}$	✓ Diagram A ✓ $\sqrt{k^2 + 1}$ A ✓ $\frac{1}{\sqrt{k^2 + 1}}$ CA (3)
3.2.2	$\operatorname{cosec} 38^\circ = \sqrt{k^2 + 1}$	✓ answer/antwoord A (1)
3.2.3	$\sin 232^\circ = \sin(180^\circ + 52^\circ)$ $\sin 232^\circ = -\sin 52^\circ$ $\sin 232^\circ = \frac{-k}{\sqrt{k^2 + 1}}$	✓ Conv./Herleiding A ✓✓ answer/antw. A (3)
3.3	$\frac{1}{2} \operatorname{cosec} 2\theta = 0,814$ $\operatorname{cosec} 2\theta = 1,628$ $\frac{1}{\sin 2\theta} = 1,628$ $1 = 1,628 \times \sin 2\theta$ $\frac{1}{1,628} = \sin 2\theta$ $37,897 \dots^\circ = 2\theta$ $18,95^\circ = \theta$	✓ S A ✓ $\frac{1}{\sin 2\theta}$ A ✓ S CA ✓ $18,95^\circ = \theta$ CA (4)
		[16]

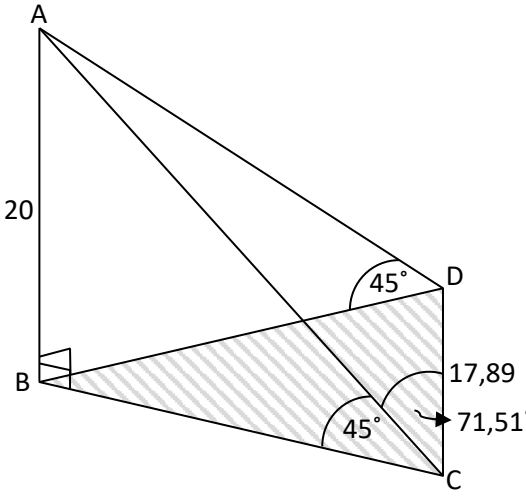
QUESTION/VRAAG 4

4.1	$\operatorname{cosec}^2 \theta$	✓ Answer/Antw.A (1)
4.2	$\frac{\cos(180^\circ + \theta) \cdot \tan(360^\circ - \theta) \cdot \cos^2(360^\circ - \theta)}{\sin(180^\circ - \theta)} + \cos^2 \theta$ $= \frac{-\cos \theta \cdot -\tan \theta \cdot \cos^2 \theta}{\sin \theta} + \cos^2 \theta$ $= \frac{-\cos \theta \cdot \frac{\sin \theta}{\cos \theta} \cdot \cos^2 \theta}{\sin \theta} + \cos^2 \theta$ $= \cos^2 \theta + \cos^2 \theta$ $= 2\cos^2 \theta$	✓ $-\cos \theta$ A ✓ $-\tan \theta$ A ✓ $\cos^2 \theta$ A ✓ $\sin \theta$ A ✓ $\frac{\sin \theta}{\cos \theta}$ A ✓ S A ✓ $2\cos^2 \theta$ CA (7)
4.3	$LHS = \frac{\sec \theta + \operatorname{cosec} \theta}{\sin \theta + \cos \theta}$ $LHS = \frac{\frac{1}{\cos \theta} + \frac{1}{\sin \theta}}{\sin \theta + \cos \theta}$ $LHS = \frac{\frac{\sin \theta + \cos \theta}{\cos \theta \sin \theta}}{\sin \theta + \cos \theta}$ $LHS = \frac{\sin \theta + \cos \theta}{\cos \theta \sin \theta} \times \frac{1}{\sin \theta + \cos \theta}$ $LHS = \frac{1}{\cos \theta \sin \theta}$ $RHS = \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}$ $RHS = \frac{\sin^2 \theta + \cos^2 \theta}{\cos \theta \sin \theta}$ $RHS = \frac{1}{\cos \theta \sin \theta} = LHS$	✓ $\frac{1}{\cos \theta}$ A ✓ $\frac{1}{\sin \theta}$ A ✓ $\frac{\sin \theta + \cos \theta}{\cos \theta \sin \theta}$ CA ✓ $\frac{1}{\cos \theta \sin \theta}$ CA ✓ $\sin^2 \theta + \cos^2 \theta$ CA ✓ $\cos \theta \sin \theta$ CA ✓ identity / identiteit A ✓ $RHS = LHS$ CA (8)
		[16]

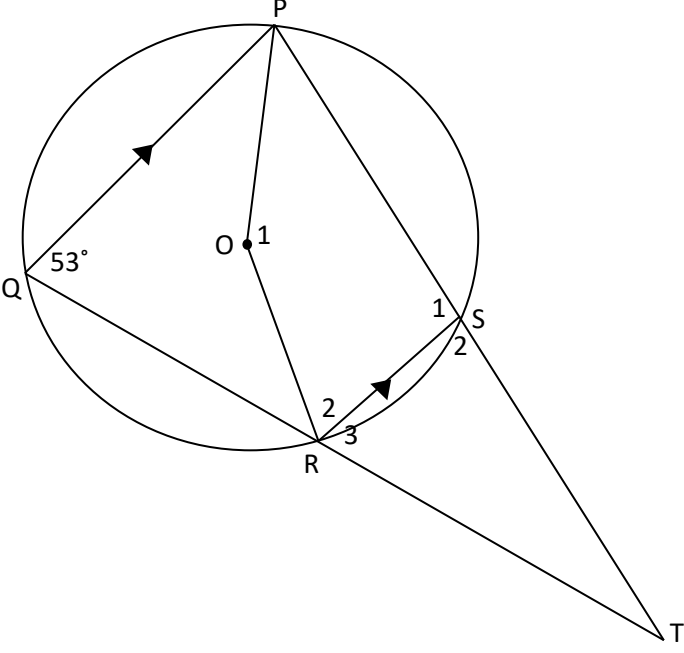
QUESTION/VRAAG 5

5.1		✓ start points/ <i>beginpunte</i> ✓ end points/<i>eindpunte</i> ✓ cos turning points/<i>cos draaipunte</i> ✓ cos x-intercepts/<i>cos</i> x-<i>afsnitte</i> ✓ sin turning points/<i>sin</i> <i>draaipunte</i> ✓ sin x-intercepts/<i>sin</i> x-<i>afsnitte</i> ✓ Points of intersection/ <i>snypunte</i>
5.2	$y \in [0; 2]$ $0 \leq y \leq 2$ OR/ OF	✓ Notation/<i>Notasie</i> A ✓ start and endpoints/ <i>begin- en eindpunte</i> CA
5.3	360°	✓ Answer/Antw. A
5.4	$x = 90^\circ$ and/ <i>en</i> $x = 180^\circ$	✓ $x = 90^\circ$ CA ✓ $x = 180^\circ$ CA
		[12]

QUESTION/VRAAG 6

				
6.1	$\sin 45^\circ = \frac{20}{AC}$ $AC \times \sin 45^\circ = 20$ $AC = \frac{20}{\sin 45^\circ}$ $AC = 20\sqrt{2}$	OR/ OF	$BC = 20$ (sides opp = $\angle$'s / sye teenoor = $\angle$ 'e) $AC = 20\sqrt{2}$ (Pyth)	✓ SF A ✓ answer/antw CA (2)
6.2	$AC = AD = 20\sqrt{2}$ $\hat{CAD} = 36,86^\circ$ (Int. $\angle$'s of Δ / Binne $\angle$ 'e van Δ) $\therefore \text{Area } \Delta ACD = \frac{1}{2} AD \cdot AC \cdot \sin \hat{CAD}$ $\therefore \text{Area } \Delta ACD = \frac{1}{2} (20\sqrt{2}) (20\sqrt{2}) \cdot \sin 36,86^\circ$ $\therefore \text{Area } \Delta ACD = 239,94 \text{ square units / vierkante eenh.}$			✓ F A ✓ SF CA ✓ Answer/Antw. A (3)
	OR / OF			
	$\text{Area } \Delta ACD = \frac{1}{2} DC \cdot AC \cdot \sin \hat{ACD}$ $\therefore \text{Area } \Delta ACD = \frac{1}{2} (17,89) (20\sqrt{2}) \cdot \sin 71,51^\circ$ $\therefore \text{Area } \Delta ACD = 239,94 \text{ square units / vierkante eenh.}$			
				[5]

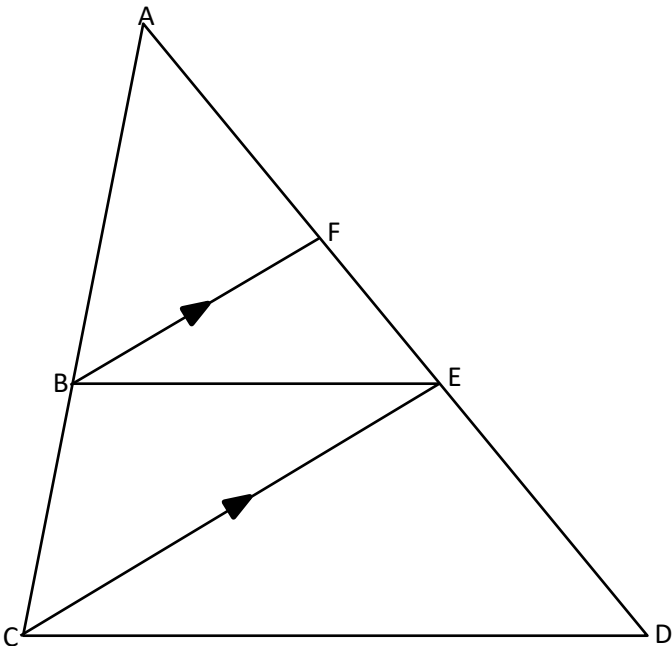
QUESTION/VRAAG 7

7.1	double/twice/dubbel/twee keer	✓	(1)
7.2			
7.2.1	$\widehat{O_1} = 106^\circ$ ($\angle$ at centre = 2 x $\angle$ at circumf. / $\angle$ by middelpt. = 2 x $\angle$ by omtrek)	✓ ST ✓ RE	(2)
7.2.2	$\widehat{S_2} = 53^\circ$ (Ext. $\angle$ of cq / Buite $\angle$ van kvh)	✓ ST ✓ RE	(2)
7.2.3	$\widehat{P} = 53^\circ$ (Corresp. $\angle$ s = / Ooreenkomst. $\angle$ 'e =; QP $\parallel$ SR)	✓ ST ✓ RE	(2)
			[7]

QUESTION/VRAAG 8

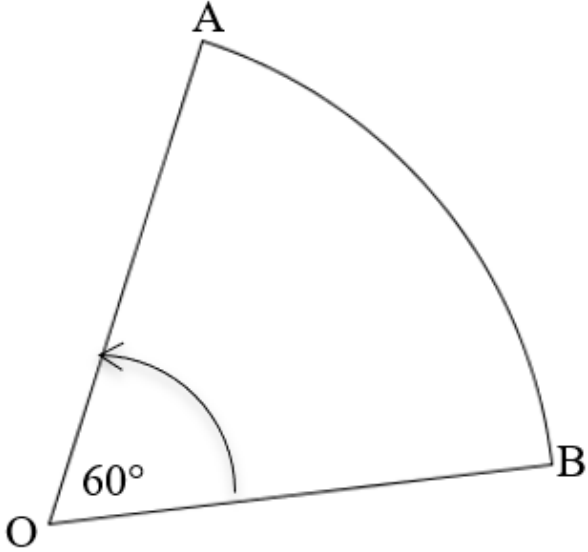
8.1	equal / gelyk	✓ (1)
8.2		
8.2.1	Tangents from same or common pt / raaklyne vanuit dieselfde pt.	✓ ST (1)
8.2.2	$\therefore \hat{P}_4 = \hat{S}_3$ ($\angle$'s opp = sides / $\angle$ 'e teenoor = sye) $\hat{P}_4 = \frac{180^\circ - 80^\circ}{2} = 50^\circ$ (Int. $\angle$'s of Δ / Binne $\angle$ 'e van	✓ ST ✓ RE ✓ ST ✓ RE (4)
8.2.3 (a)	$\hat{P}_2 = 50^\circ$ (tan-chord / raaklyn-koord)	✓ ST ✓ RE (2)
8.2.3 (b)	$\hat{Q}_3 = 50^\circ$ (tan-chord / raaklyn-koord) $\therefore \hat{S}_2 = 50^\circ$ ($\angle$'s opp = sides / $\angle$ 'e teenoor = sye)	✓ ST / RE ✓ ST / RE (2)
8.2.3 (c)	$\hat{R}_2 = 50^\circ$(alt/verw $\angle$'s/e; VQ $\parallel$ RP) OR/OF $\hat{R}_2 = 50^\circ$($\angle$'s in same segment / $\angle$ 'e in dies segm)	✓ ST ✓ RE OR/OF ✓ ST ✓ RE (2)
8.2.3 (d)	$\hat{R}_3 = 50^\circ$ (tan-chord / raaklyn-koord) $\hat{V} = 50^\circ$(corresp/ooreenk $\angle$'s/e; VQ $\parallel$ RP) OR/OF (ext $\angle$ of Δ / buite $\angle$ van Δ)	✓ ST / RE ✓ ST / RE (2)
		[14]

QUESTION/VRAAG 9

9.1	Parallel	✓ A (1)
9.2		
9.2.1	$\frac{AB}{AC} = \frac{AF}{AE}$ (line $\parallel$ to 1 side of Δ / lyn $\parallel$ aan 1 sy van Δ) $\frac{3}{4} = \frac{AF}{36}$ $\frac{3}{4} \times 36 = AF$ $27 = AF$	✓ ST RE ✓ SF ✓ Answer / Antw. (3)
9.2.2	$FE = AE - AF = 36 - 27 = 9$ $\therefore \frac{FE}{ED} = \frac{3}{4}$ $\therefore \frac{9}{ED} = \frac{3}{4}$ $\therefore 36 = 3ED$ $\therefore 12 = ED$	✓ ST ✓ SF ✓ Answer / Antw. (3)
9.3	In proportion / is eweredig	✓ (1)

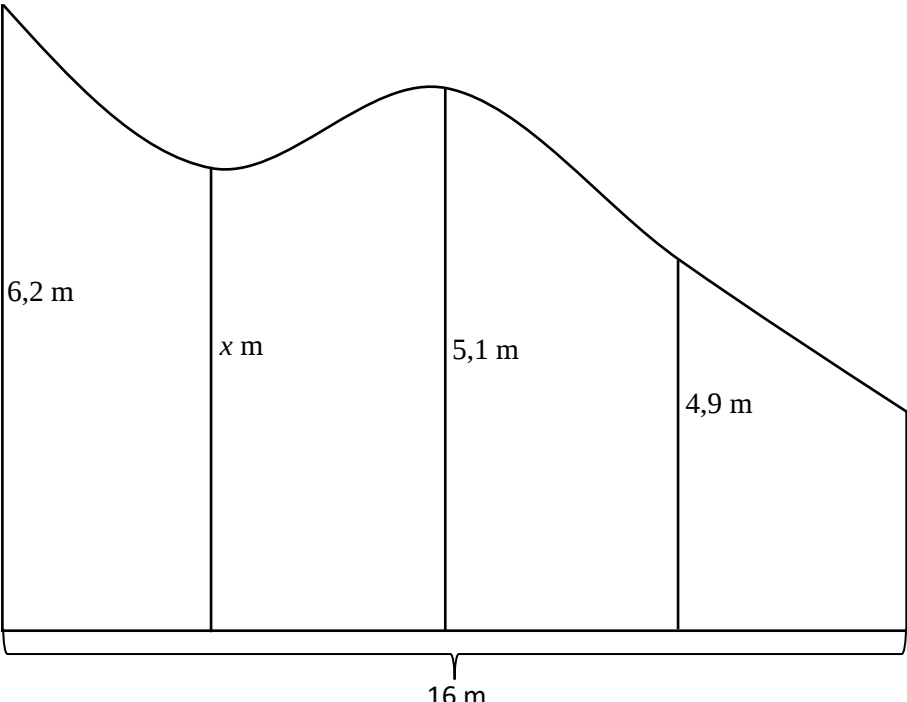
9.4.2 (d)	$\Delta AEC \parallel \Delta ADE \parallel \Delta ABF$ (proved / bewys) $\frac{AD}{AB} = \frac{DE}{BF} = \frac{AE}{AF}$ $\frac{75}{25} = \frac{DE}{BF} = \frac{60}{20}$ $\therefore 75:25 = DE:BF$ $\therefore 3:1 = DE:BF$	✓ ST ✓ ST (2)
		[23]

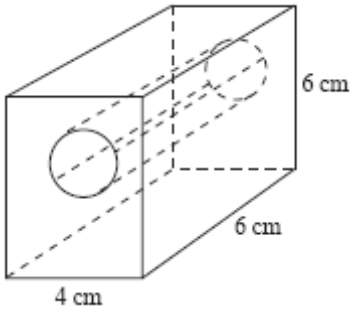
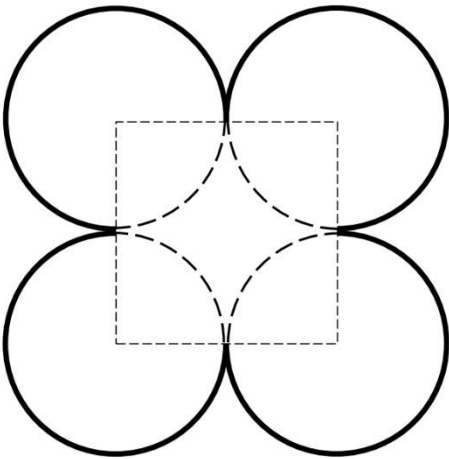
QUESTION/VRAAG 10

10.1		
10.1.1	$\theta = 60^\circ \times \frac{\pi}{180^\circ} = \frac{\pi}{3} \text{ rad}$ $\therefore s = r\theta$ $\therefore s = 5 \left(\frac{\pi}{3} \right)$ $\therefore s = \frac{5}{3}\pi$	✓ $\frac{\pi}{3}$ A ✓ F A ✓ SF CA ✓ $\frac{5}{3}\pi$ CA (4)
10.1.2	$\text{Area} = \frac{r^2\theta}{2}$ $\text{Area} = \frac{(5)^2 \left(\frac{\pi}{3} \right)}{2}$ $\text{Area} = \frac{25}{6}\pi$	✓ F A ✓ SF CA ✓ $\frac{25}{6}\pi$ CA (3)

10.2				
10.2.1	$\omega = 2\pi n$ $\omega = 2\pi(30)$ $\omega = 60\pi \text{ rad/s}$	1800 rev / min 1800 rev / 60 sec 30 rev / sec	✓ Conv. / Herl. ✓ F ✓ SF ✓ 60π	A A CA CA (4)
10.2.2	$v = \pi D n$ $v = \pi(0,42)(30)$ $v = \frac{63}{5}\pi \text{ m/s}$	$D = 420 \div 1000$ $\therefore D = 0,42 \text{ m}$ 1800 rev / min 1800 rev / 60 sec 30 rev / sec	✓ Conv. / Herl. ✓ F ✓ SF ✓ $\frac{63}{5}\pi$	A A CA CA (4)
10.2.3	$h^2 - 4dh + x^2 = 0$ $h^2 - 4(42)h + (25)^2 = 0$ $h^2 - 168h + 625 = 0$ $\therefore h = 164,19 \text{ or / of } h = 3,81$ $\therefore US = 3,81 \text{ cm}$	250 mm = 25 cm 420 mm = 42 cm	✓ Conv. / Herlei ✓ F ✓ SF ✓ Both answers of h / Beide antw. vir h ✓ US = 3,81 cm	A A CA CA CA (5)
				[20]

QUESTION/VRAAG 11

11.1	 Diagram showing a trapezoidal area divided into four vertical strips. The total width is 16 m. The heights of the strips from left to right are 6,2 m, x m, 5,1 m, and 4,9 m. The rightmost strip is a triangle with a height of 2 m at its base.	
$Area = a \left(\frac{O_1 + O_n}{2} + O_2 + O_3 + \dots + O_{n-1} \right)$ $73,6 = 4 \left(\frac{6,2 + 2}{2} + x + 5,1 + 4,9 \right)$ $73,6 = 4(14,1 + x)$ $18,4 = 14,1 + x$ $4,3 \text{ m} = x$ OR/OF $Area = a(m_1 + m_2 + m_3 + \dots + m_{n-1})$ $73,6 = 4 \left(\frac{6,2 + x}{2} + \frac{x + 5,1}{2} + 5 + 3,45 \right)$ $18,4 = \frac{11,3 + 2x}{2} + 8,45$ $9,95 = \frac{11,3 + 2x}{2}$ $19,9 = 11,3 + 2x$ $8,6 = 2x$ $4,3 \text{ m} = x$	$a = \frac{16}{4}$ $a = 4$	✓ F A ✓ $a = 4$ A ✓ SF CA ✓ S CA ✓ $4,3 \text{ m} = x$ CA (5) OR/OF ✓ F A ✓ $a = 4$ A ✓ SF CA ✓ S CA ✓ $4,3 \text{ m} = x$ CA (5)

11.2			
	<i>Vol. of block of wood</i> = $l \times b \times h$ <i>Vol. of block of wood</i> = $4 \times 6 \times 6$ <i>Vol. of block of wood</i> = 144 cm^2 <i>Vol. of cylinder</i> = $\pi r^2 h$ <i>Vol. of cylinder</i> = $\pi (0,75)^2 (6)$ <i>Vol. of cylinder</i> = $10,60 \text{ cm}^2$ $\therefore$ <i>Vol. of remaining block</i> = $144 - 10,60$ $\therefore$ <i>Vol. of remaining block</i> = $133,40 \text{ cm}^2$	$d = 1,5$ $\therefore r = 0,75$	✓ 144 cm^2 CA ✓ $10,60 \text{ cm}^2$ CA ✓ Method / Metode ✓ $133,40 \text{ cm}^2$ CA (4)
11.3			
	<i>circumference of a circle</i> = $2\pi r$ $\therefore 200 = 2\pi r$ $\therefore \frac{200}{2\pi} = r$ $\therefore 31,83 \text{ cm} = r$ <i>dist. from centre of circle to midpt of poster</i> = $21,21 \text{ cm}$ (Pyth) $\therefore$ <i>total radius needed</i> = $21,21 + 15 = 36,21 \text{ cm}$ $\therefore 36,21 > 31,83$ $\therefore$ The poster will not fit in the circular space on the wall / Die plakkaat sal nie in die sirkelvormige spasie op die muur pas nie.		✓ radius of wall space / radius van muur spasie ✓ Distance / afstand ✓ total radius / totale radius ✓ Answer / Antw. ✓ Concl. / Afleid.

	OR/OF	OR/OF
	circumference of a circle = $2\pi r$ $\therefore 200 = 2\pi r$ $\therefore \frac{200}{2\pi} = r$ $\therefore 31,83 \text{ cm} = r$ Area of wall = πr^2 $\therefore \text{Area of wall} = \pi(31,83)^2$ $\therefore \text{Area of wall} = 3183 \text{ cm}^2$ Minimum required dimensions /minimum benodigde afmetings: 60 by 60 Area of poster = $l \times b$ $\therefore \text{Area of poster} = 60 \times 60$ $\therefore \text{Area of poster} = 3600 \text{ cm}^2$ $\therefore$ The poster will not fit in the circular space on the wall / Die plakkaat sal nie in die sirkelvormige spasie op die muur pas nie.	✓ radius of wall space / radius van muur spasie ✓ Area of wall / Area van muur ✓ Dimension of poster / Afmetings van plakkaat ✓ Answer / Antw. ✓ Concl. / Afleid. (5)
		[14]
		TOTAL /TOTAAL: 150