May/June 2023



EDUCATION

MOGALAKWENA DISTRICT

GRADE 12

MATHEMATICS
TERM 2
PRE JUNE EXAM PAPER 1
MAY/JUNE 2023

MARKS: 150

12 |E |I|

TIME: 3Hours

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INSTRUCTIONS AND INFORMATION:

Read the following instructions carefully before answering the questions.

- 1. This question paper consists of 9 questions.
- 2. Answer ALL questions.
- Clearly show ALL calculations, diagrams, graphs, etc, that you have used in determining your answers.
- 4. Answers only will NOT necessarily be awarded full marks.
- If necessary, round off answers correct to TWO decimal places, unless stated otherwise.
- 6. You may use an approved scientific calculator (no programmable and no graphical).
- 7. Diagrams not necessarily drawn to scale.
- 8. An information sheet with formulae is included at the end of the question paper.



1.1 Solve for x:

1.4.1
$$(x-3)(5x+2) = 0$$
 (2)

1.1.2
$$3x^2 - 10x - 1 = 0$$
 (Correct to two decimal places) (3)

$$1.1.3 \quad x(x-4) \ge 21 \tag{5}$$

$$1.1.4 \quad 2.3^x + \frac{3^x}{2} = 7\frac{1}{2} \tag{4}$$

1.2. Solve for x and y simultaneously.

$$x + 2y = 2$$

$$x^2 + 8y = 8 (6)$$

Given: $2^{x+1} + 2^x = 3^{y+2} - 3^y$, where x and y are integers.

Determine the value of x and y.

$$\sqrt{x-2} + 3 = \frac{10}{\sqrt{x-2}}$$
 (5)

1.3 Given:

$$x = \frac{4 \pm \sqrt{16 - 4p}}{2}$$

1.3.1 If p = 4, determine the nature of the roots. (1)

1.3.2 Determine the value(s) of p for which the roots are non-real. (2)

The equations $x^2 + rx + m = 0$ and $x^2 + mx + r = 0$ have real and EQUAL roots. Solve for the values of r and m if r > 0 and m > 0.

[37]

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The sequence: -67; x; y; -28; -19; ... has a quadratic pattern.

- 2.1 Determine the value of x and y (6)
- 2.2 Find an expression for the nth term (4)
- 2.3 Prove that the sequence of numbers will never contain a positive term. (3)

[13]

QUESTION 3

- 3.1 The fourth term of a geometric progression is 24 and the ninth term is 768. (5) Determine the first three terms of the Progression.
- 3.2

If
$$S_n = 2n^2 + 3n$$
 then

3.2.1 Calculate T_{12} (3)

3.2.2 Find T_n in its simplest form. (4)

3.3 Calculate the value of $\sum_{n=2}^{18} (2n-1)$ (3)

- In a converging geometric series $S_{\infty} = \frac{40}{3}$ and $T_2 = \frac{5}{2}$; calculate the possible value(s) the first term of the series. (3)
- 3.5 Given the following geometric sequence:

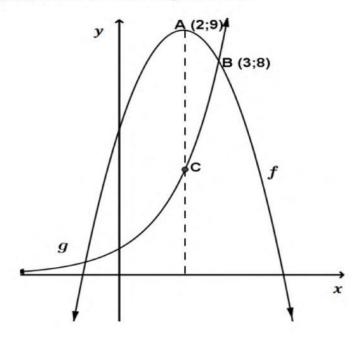
$$\frac{24}{x}$$
 + 12 + 6x + 3x² + ...

- 3.5.1 Calculate the sum to infinity of the series (4)
- 3.5.2 Write down the values of x for which this sequence converges. (2)

[24]



The graphs of f(x) and g(x) are shown in the diagram below.



The turning point of f(x) is A (2; 9) and the graphs f and g intersects at B (3; 8). C is a point on g(x) and is on the axis of symmetry of f.

4.1 Show that the function f can be defined by the equation: (4)

$$f(x) = -x^2 + 4x + 5$$

- 4.2 Write down the equation of the axis of symmetry of f. (1)
- 4.3 The graph g(x), has the equation $y = a^x$. Determine the value of a. (2)
- 4.4 If it is given that (-1; 0) is one root of f, write down the coordinates of the other root. (1)
- 4.5 For which value(s) of x will f(x) < 0? (2)
- 4.6 Determine the length of AC. (2)
- 4.7 Discuss the nature of the roots of h(x) if, h(x) = f(x) 9. (2)

 [14]

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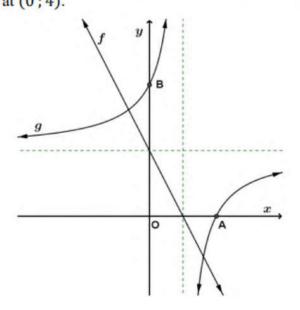
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QUESTION 5

In the diagram below are the sketches of: f(x) = -2x + 2 and $g(x) = \frac{a}{x+p} + q$ The graph of g cuts the y-axis at (0; 4).



- 5.1 Calculate the values of p and q (3)
- 5.2 Show that a = -2 (2)
- 5.3 Determine the coordinates of point A the x intercept of g(x) (2)
- 5.4 The value of q is increased by 1 unit. What effect will it have on the graph of g? (1)
- 5.5 Write the equations of the asymptotes. (2) [10]

QUESTION 6

Given:
$$p(x) = \left(\frac{1}{4}\right)^x$$

- 6.1 Write down the equation of p^{-1} in the form $y = \cdots$ (2)
- 6.2 Sketch the graphs of p and p⁻¹ on the given system of axes on the diagram sheet. (5)
 Show clearly all the intercepts with the axes as well as the line of symmetry.
- Determine the value(s) of x for which $p^{-1}(x) \ge 1$ (2)



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Write down the equation of the graph of h(x), if h(x) is formed by shifting the graph of p(x) 2 units to the right and then 3 units up.

(2)

[11]

QUESTION 7

7.1 Determine
$$f'(x)$$
 from first principles if $f(x) = 5 - 2x^2$. (5)

7.2 Determine $\frac{dy}{dx}$ if:

7.2.1
$$y = 7x^4 + \frac{2x^2}{\sqrt{x}}$$
 (3)

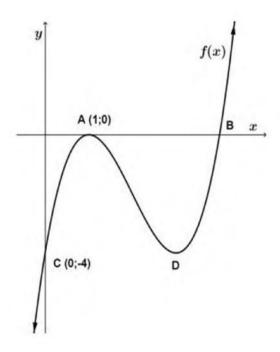
$$7.2.2 xy = 5 (2)$$

7.2.3
$$D_{\infty} \begin{bmatrix} 3x^2 - 7x - 6 \end{bmatrix}$$
 (4)

[14]



Given that $f(x) = x^3 - 6x^2 + 9x - 4$ with x-intercepts at A (1; 0) and B, y-intercept at C(0; -4). A and D are the turning points of f.

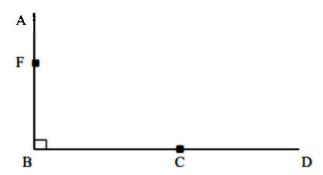


- 8.1 Calculate the coordinates of B. (4)
- 8.2 Calculate the coordinates of the turning point D. (5)
- 8.3 Calculate the x-coordinate of the point of inflection of f. (2)
- 8.4 Write down the values of k for which f(x) = k will have only ONE root. (2)
- 8.5 Determine the values of x where f'(x) > 0 (3)
- 8.6 Determine the gradient of the line DC. (1)

[17]



Two cyclists start to cycle at the same time. One starts at point B and is heading due north to point A, whilst the other starts at point D and is heading due west to point B. The cyclist starting from B cycles at 30 km/h while the cyclist starting from D cycles at 40 km/h. The distance between B and D is 100 km. After time t (measured in hours), they reach points F and C respectively.



- 9.1 Determine the distance between F and C in terms of t. (4)
- 9.2 After how long will the two cyclists be closest to each other? (4)
- 9.3 What will the distance between the cyclists be at the time determined in QUESTION 9.2?

[10]