



# basic education

Department:  
Basic Education  
**REPUBLIC OF SOUTH AFRICA**

**SENIOR CERTIFICATE EXAMINATIONS/  
SENIORSERTIFIKAAT-EKSAMEN  
NATIONAL SENIOR CERTIFICATE EXAMINATIONS/  
NASIONALE SENIORSERTIFIKAAT-EKSAMEN**

**MATHEMATICS P2/WISKUNDE V2**

**MARKING GUIDELINES/NASIENRIGLYNE**

**MAY/JUNE/MEI/JUNIE 2023**

**MARKS: 150  
PUNTE: 150**

**These marking guidelines consist of 21 pages./  
Hierdie nasienriglyne bestaan uit 21 bladsye.**

Chief Examiner/Goewer

Approved by Umakazi External Moderator on 15 May 2023

*Approved*  
*[Signature]*

2023-05-15



**NOTE:**

- If a candidate answers a question TWICE, mark only the FIRST attempt.
- If a candidate has crossed out an attempt at an answer and not redone the question, mark the crossed-out version.
- Consistent accuracy applies in ALL aspects of the marking guidelines. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

**LET WEL:**

- As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.
- As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, merk die doodgetrekte poging.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.
- Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.

GEOMETRY • MEETKUNDE	
S	A mark for a correct statement (A statement mark is independent of a reason)
	'n Punt vir 'n korrekte bewering (‘n Punt vir 'n bewering is onafhanklik van die rede)
R	A mark for the correct reason (A reason mark may only be awarded if the statement is correct)
	'n Punt vir 'n korrekte rede (‘n Punt word slegs vir die rede toegeken as die bewering korrek is)
S/R	Award a mark if statement AND reason are both correct
	Ken 'n punt toe as die bewering EN rede beide korrek is



**QUESTION/VRAAG 1**

1.1.1	$a = 1730,22$ $b = 13,96$ $\hat{y} = 1730,22 + 13,96x$	$\checkmark a = 1730,22$ $\checkmark b = 13,96$ $\checkmark$ equation (3)
1.1.2	$\hat{y} = 1730,22 + 13,96x$ $\hat{y} = 1730,22 + 13,96(28500)$ $\hat{y} = R399\,590,22$  <b>OR/OF</b>  $\hat{y} = R399\,599,64$ (calc)	$\checkmark$ substitution $\checkmark$ answer (2)  $\checkmark\checkmark$ answer (2)
1.1.3	$r = 0,98002 \dots$ $r = 0,98$	$\checkmark$ answer (1)
1.1.4	There is a very strong positive correlation between the amount spent on advertising and sales. / <i>Daar is 'n baie sterk positiewe korrelasie tussen die bedrag spandeer op advertensie en die verkope.</i>	$\checkmark$ strong positive / sterk positief (1)
1.2.1	$\bar{x} = \frac{1\,552\,195}{9}$ $\bar{x} = 172\,466,11$	$\checkmark \bar{x} = \frac{1\,552\,195}{9}$ $\checkmark$ answer (2)
1.2.2	$\sigma = 56\,950,09$	$\checkmark$ answer (1)
1.2.3	$\bar{x} + \sigma$ $= 172\,466,11 + 56\,950,09$ $= 229\,416,20$  2 years/jaar	$\checkmark \bar{x} + \sigma$  $\checkmark$ answer (2)
		<b>[12]</b>



## QUESTION/VRAAG 2

2.1	$35 < x \leq 45$	✓ answer (1)																								
2.2	320 people/mense	✓ answer (1)																								
2.3	<table border="1"> <thead> <tr> <th>AGE</th><th>NUMBER OF PEOPLE</th><th>CUMULATIVE FREQUENCY</th></tr> </thead> <tbody> <tr> <td><math>5 &lt; x \leq 15</math></td><td>20</td><td>20</td></tr> <tr> <td><math>15 &lt; x \leq 25</math></td><td>25</td><td>45</td></tr> <tr> <td><math>25 &lt; x \leq 35</math></td><td>60</td><td>105</td></tr> <tr> <td><math>35 &lt; x \leq 45</math></td><td>90</td><td>195</td></tr> <tr> <td><math>45 &lt; x \leq 55</math></td><td>55</td><td>250</td></tr> <tr> <td><math>55 &lt; x \leq 65</math></td><td>40</td><td>290</td></tr> <tr> <td><math>65 &lt; x \leq 75</math></td><td>30</td><td>320</td></tr> </tbody> </table> <div style="text-align: center;"> <p><b>OGIVE/OGIEF</b></p> </div>	AGE	NUMBER OF PEOPLE	CUMULATIVE FREQUENCY	$5 < x \leq 15$	20	20	$15 < x \leq 25$	25	45	$25 < x \leq 35$	60	105	$35 < x \leq 45$	90	195	$45 < x \leq 55$	55	250	$55 < x \leq 65$	40	290	$65 < x \leq 75$	30	320	✓ cumulative frequency ✓ grounding ✓ plotting at upper limit ✓ shape (4)
AGE	NUMBER OF PEOPLE	CUMULATIVE FREQUENCY																								
$5 < x \leq 15$	20	20																								
$15 < x \leq 25$	25	45																								
$25 < x \leq 35$	60	105																								
$35 < x \leq 45$	90	195																								
$45 < x \leq 55$	55	250																								
$55 < x \leq 65$	40	290																								
$65 < x \leq 75$	30	320																								
2.4	Median = 41	✓✓ answer (2)																								

DEPARTMENT OF BASIC EDUCATION

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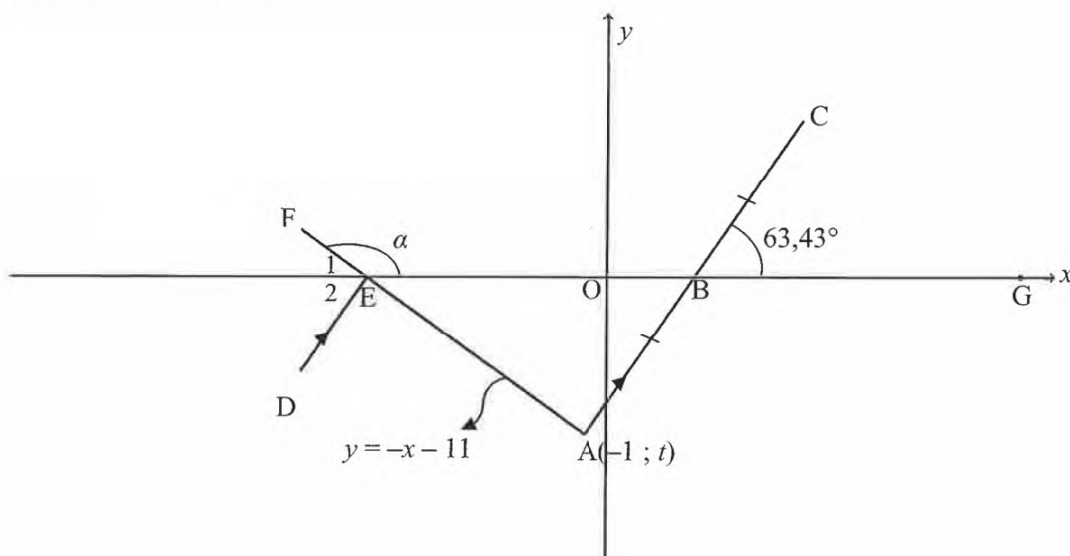
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APPROVED MARKING GUIDELINE

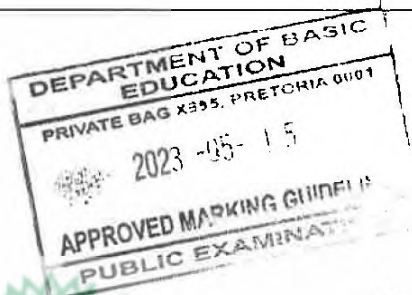
PUBLIC EXAMINATIONS



## QUESTION/VRAAG 3



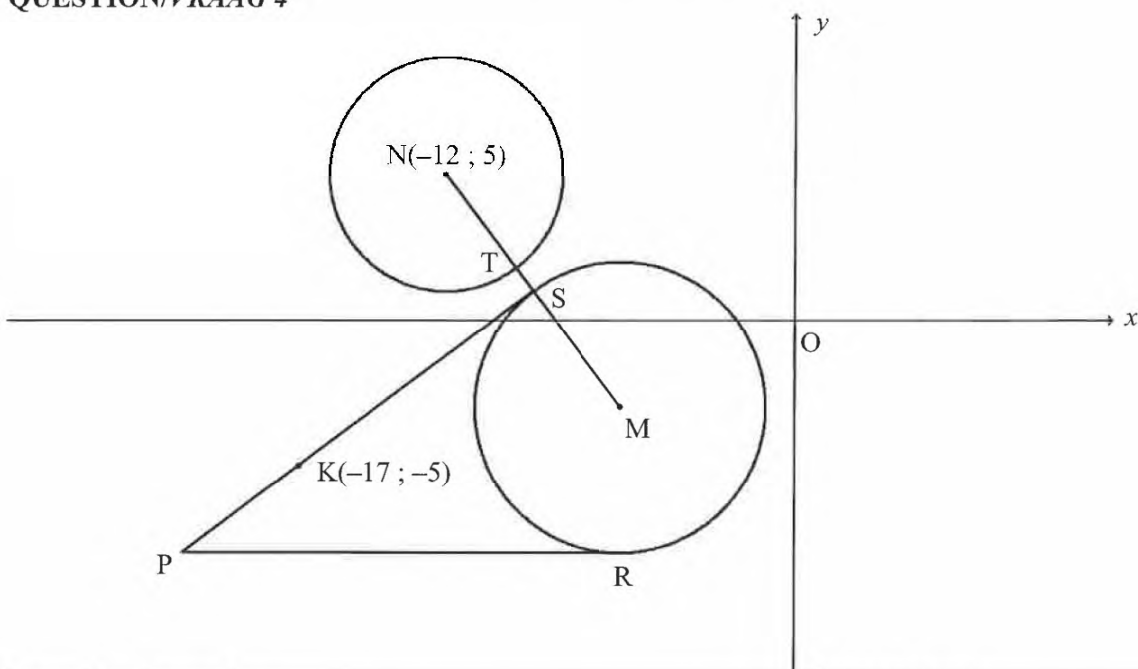
3.1.1	$y = -x - 11$ $A(-1; t)$ $t = -(-1) - 11$ $t = -10$	✓ substitution ✓ value of $t$ (2)
3.1.2	$\tan \alpha = -1$ $\text{ref. } \angle = 45^\circ$ $\therefore \alpha = 135^\circ$	✓ $\tan \alpha = -1$ ✓ $135^\circ$ (2)
3.1.3	$\tan 63,43^\circ = m_{AC}$ $m_{AC} = 2$	✓ $\tan 63,43^\circ = m_{AC}$ ✓ answer (2)
3.2	$m_{AC} = 2$ $A(-1; -10)$ $y = 2x + k$ $-10 = 2(-1) + k$ $k = -8$ $y = 2x - 8$	OR/OF $y - y_1 = 2(x - x_1)$ $y - (-10) = 2(x - (-1))$ $y = 2x - 8$ ✓ substitution of $m$ and $A$ ✓ equation (2)



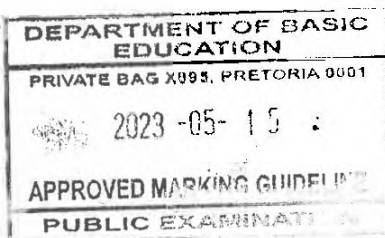
3.3.1	$y = 2x - 8$ $0 = 2x - 8$ $x_B = 4$  $\frac{x_C + (-1)}{2} = 4$ $x_C = 9$  $\frac{y_C + (-10)}{2} = 0$ $y_C = 10$  <b>OR/OF</b> by translation / met translasië  $A \rightarrow B (x; y) \rightarrow (x+5; y+10)$ $B \rightarrow C (4; 0) \rightarrow (4+5; 0+10) = (9; 10)$	$\checkmark x_B = 4$  $\checkmark x_C = 9 \quad \checkmark y_C = 10$ (3)  $\checkmark (x+5; y+10)$ $\checkmark x_C = 9 \quad \checkmark y_C = 10$ (3)
3.3.2	$\hat{A}BE = 63,43^\circ$ $\hat{E}_2 = 63,43^\circ$ $\hat{E}_1 = 45^\circ$ $\hat{F}ED = 108,43^\circ$  <b>OR/OF</b>  $\hat{E}AB = 135^\circ - 63,43^\circ$ $\hat{E}AB = 71,57^\circ$ $\hat{D}EA = \hat{E}AB = 71,57^\circ$ $\hat{F}ED = 108,43^\circ$  <b>OR/OF</b>  $\hat{A}BE = 63,43^\circ$ $\hat{D}EO = 116,57^\circ$ $\hat{F}ED = 360^\circ - (116,57^\circ + 135^\circ)$ $= 108,43^\circ$	[vert. opp $\angle$ 's =] [corres. $\angle$ 's, $DE \parallel AB$ ] [ $\angle$ s on a str line]  $\checkmark \hat{A}BE = 63,43^\circ$ $\checkmark \hat{E}_1 = 45^\circ$ $\checkmark \hat{F}ED = 108,43^\circ$ (3)  $\checkmark \hat{E}AB = 71,57^\circ$ $\checkmark \hat{D}EA = \hat{E}AB = 71,57^\circ$ $\checkmark \hat{F}ED = 108,43^\circ$ (3)  [vert. opp $\angle$ 's] [co-int. $\angle$ 's, $DE \parallel AB$ ]  $\checkmark \hat{A}BE = 63,43^\circ$ $\checkmark \hat{D}EO = 116,57^\circ$ $\checkmark \hat{F}ED = 108,43^\circ$ (3)
3.4	$y = 0$ $x_E = -11$ $\frac{x_G + (-11)}{2} = 4$ $x_G = 19$  $(x-19)^2 + y^2 = 15^2$ $(x-19)^2 + y^2 = 225$	$\checkmark x_E = -11$  $\checkmark x_G = 19$  $\checkmark (x-19)^2 + y^2 \checkmark 225$ (4)
		[18]



## QUESTION/VRAAG 4



4.1	$M(-6; -3)$	✓ $-6$ ✓ $-3$ (2)
4.2.1	$x^2 + y^2 + 24x - 10y + 153 = 0$ $(x+12)^2 + (y-5)^2 = -153 + 144 + 25$ $(x+12)^2 + (y-5)^2 = 16$ $r^2 = 16$ $r = 4$ units	✓ $r^2 = -153 + 144 + 25$  ✓ length of radius (2)
4.2.2	$NM = \sqrt{(-12 - (-6))^2 + (5 - (-3))^2}$ $NM = 10$ units $SM = 5$ units $\therefore TS = 10 - 5 - 4 = 1$ unit	✓ substitution into distance formula ✓ $NM = 10$ units  ✓ $SM = 5$ units ✓ answer (4)
4.3.1	$R(-6; -8)$ $y = -8$	✓ $y_R = -8$ ✓ equation (2)



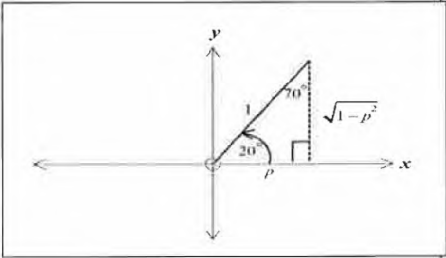

4.3.2	$m_{NM} = \frac{5 - (-3)}{-12 - (-6)}$ $m_{NM} = -\frac{4}{3}$ $m_{\text{tangent}} = \frac{3}{4}$ $-5 = \frac{3}{4}(-17) + c \quad \text{OR/OF} \quad y - y_1 = \frac{3}{4}(x - x_1)$ $c = \frac{31}{4} \quad y - (-5) = \frac{3}{4}(x - (-17))$ $y = \frac{3}{4}x + \frac{31}{4} \quad y = \frac{3}{4}x + \frac{31}{4}$ <p><b>OR/OF</b></p> $NS = SM = 5$ $S\left(\frac{-12-6}{2}; \frac{5-3}{2}\right)$ $S(-9; 1)$ $m_{SK} = \frac{1 - (-5)}{-9 + 17}$ $= \frac{6}{8} = \frac{3}{4}$ $y + 5 = \frac{3}{4}(x + 17)$ $y = \frac{3}{4}x + \frac{31}{4} \quad \text{or} \quad y = \frac{3}{4}x + 7\frac{3}{4}$	<p>✓ substitution</p> <p>✓ <math>m_{NM} = -\frac{4}{3}</math></p> <p>✓ <math>m_{\text{tangent}} = \frac{3}{4}</math></p> <p>✓ substitution of <math>m</math> and <math>N</math></p> <p>✓ equation (5)</p> <p>✓ S midpoint</p> <p>✓ coordinates of <math>S</math></p> <p>✓ <math>m_{\text{tangent}} = \frac{3}{4}</math></p> <p>✓ substitution of <math>m</math> and <math>K(-17; -5)</math> or <math>S</math></p> <p>✓ equation (5)</p>
4.4.1	$-8 = \frac{3}{4}x + \frac{31}{4}$ $-32 = 3x + 31$ $3x = -63$ $x = -21$ $P(-21; -8)$ $R(-6; -8)$ <p><math>PR = PS = 15</math> units [tangents from same point]</p> <p><math>MS = MR = 5</math> units</p> <p>Perimeter PSMR = <math>15 + 15 + 5 + 5</math> = 40 units</p>	<p>✓ <math>-8 = \frac{3}{4}x + \frac{31}{4}</math></p> <p>✓ <math>x = -21</math></p> <p>✓ <math>PR = PS = 15</math> units</p> <p>✓ <math>MS = MR = 5</math> units</p> <p>✓ answer (5)</p>



4.4.2	<p>area of <math>\triangle NPS</math></p> <hr/> <p>area of quadrilateral PSMR</p> $\frac{1}{2} NS.SP$ <hr/> $\frac{1}{2} SP.MS + \frac{1}{2} MR.PR$ $= \frac{\frac{1}{2}(5)(15)}{2\left(\frac{1}{2}\right)(5)(15)}$ $= \frac{1}{2}$ <p><b>OR</b></p> <p><math>\triangle NPS \equiv \triangle SPM \equiv \triangle MPR</math></p> <p>area of <math>\triangle NPS</math></p> <hr/> <p>area of quadrilateral PSMR</p> $= \frac{1}{2}$	<p>✓ substitution</p> <p>✓ answer (2)</p> <p>✓ congruent</p> <p>✓ answer (2)</p> <p>[22]</p>
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## QUESTION/VRAAG 5

5.1	$\frac{1 - \sin(-\theta)\cos(90^\circ + \theta)}{\cos(\theta - 360^\circ)}$ $= \frac{1 - (-\sin\theta)(-\sin\theta)}{\cos\theta}$ $= \frac{1 - \sin^2\theta}{\cos\theta}$ $= \frac{\cos^2\theta}{\cos\theta}$ $= \cos\theta$	✓ $-\sin\theta$ ✓ $-\sin\theta$ ✓ $\cos\theta$  ✓ $\cos^2\theta$ ✓ answer (5)
5.2.1	$\cos 200^\circ$ $= -\cos 20^\circ$ $= -p$	✓ reduction ✓ answer (2)
5.2.2	$\sin(-70^\circ)$ $= -\sin 70^\circ$ $= -\cos 20^\circ$ $= -p$ <p><b>OR/OF</b></p> $\sin(-70^\circ)$ $= -\sin 70^\circ$ $= -p$ 	✓ reduction ✓ answer (2)  ✓ reduction ✓ answer (2)
5.2.3	$\sin 10^\circ$ $\cos(2(10^\circ)) = 1 - 2\sin^2 10^\circ$ $2\sin^2 10^\circ = 1 - \cos 20^\circ$ $\sin 10^\circ = \sqrt{\frac{1 - \cos 20^\circ}{2}}$ $\sin 10^\circ = \sqrt{\frac{1 - p}{2}}$ <p><b>OR/OF</b></p> $\sin 10^\circ$ $\sin(30^\circ - 20^\circ)$ $= \sin 30^\circ \cos 20^\circ - \cos 30^\circ \sin 20^\circ$ $= \frac{1}{2}p - \frac{\sqrt{3}}{2}\sqrt{1-p^2} = \frac{p - \sqrt{3}\sqrt{1-p^2}}{2}$ 	✓ double angle  ✓ $\sin 10^\circ$ as subject  ✓ answer (3)  ✓ using special angle ✓ expanding ✓ answer (3)



	<b>OR/OF</b> $\sin 10^\circ$ $\sin(70^\circ - 60^\circ)$ $= \sin 70^\circ \cos 60^\circ - \cos 70^\circ \sin 60^\circ$ $= p \cdot \frac{1}{2} - \sqrt{1-p^2} \times \frac{\sqrt{3}}{2} = \frac{p - \sqrt{3}\sqrt{1-p^2}}{2}$  <b>OR/OF</b> $\sin 10^\circ$ $= \cos 80^\circ$ $\cos(60^\circ + 20^\circ)$ $= \cos 60^\circ \cos 20^\circ - \sin 60^\circ \sin 20^\circ$ $= \frac{1}{2}p - \frac{\sqrt{3}}{2}\sqrt{1-p^2}$	✓ using special angle ✓ expanding  ✓ answer (3)
5.3	$\cos(A + 55^\circ)\cos(A + 10^\circ) + \sin(A + 55^\circ)\sin(A + 10^\circ)$ $= \cos[A + 55^\circ - (A + 10^\circ)]$ $= \cos 45^\circ$ $= \frac{1}{\sqrt{2}} \quad \text{or} \quad \frac{\sqrt{2}}{2}$	✓✓ compound identity  ✓ answer (3)
5.4.1	$\begin{aligned} \text{LHS} &= \frac{\cos 2x + \sin 2x - \cos^2 x}{\sin x - 2 \cos x} & \text{RHS} &= -\sin x \\ &= \frac{\cos^2 x - \sin^2 x + 2 \sin x \cos x - \cos^2 x}{\sin x - 2 \cos x} \\ &= \frac{-\sin^2 x + 2 \sin x \cos x}{\sin x - 2 \cos x} \\ &= \frac{-\sin x(\sin x - 2 \cos x)}{\sin x - 2 \cos x} \\ &= -\sin x \\ \therefore \text{LHS} &= \text{RHS} \end{aligned}$	✓ $\cos^2 x - \sin^2 x$ ✓ $2 \sin x \cos x$  ✓ common factor of $-\sin x$ (3)
5.4.2	$\begin{aligned} &\frac{\cos 2x + \sin 2x - \cos^2 x}{-3 \sin^2 x + 6 \sin x \cos x} \\ &= \frac{\cos 2x + \sin 2x - \cos^2 x}{-3 \sin x(\sin x - 2 \cos x)} \\ &= \frac{\cos 2x + \sin 2x - \cos^2 x}{(\sin x - 2 \cos x)} \times \frac{1}{-3 \sin x} \\ &= (-\sin x) \times \frac{1}{-3 \sin x} \\ &= \frac{1}{3} \end{aligned}$	✓ common factor of $-3 \sin x$  ✓ substitution ✓ answer (3)



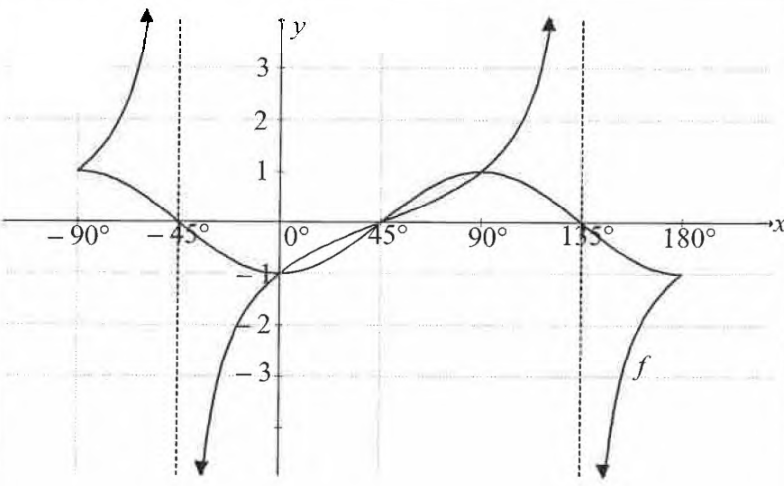
5.5.1	$3 \tan 4x = -2 \cos 4x$ $3 \left( \frac{\sin 4x}{\cos 4x} \right) = -2 \cos 4x$ $3 \sin 4x + 2 \cos^2 4x = 0$ $3 \sin 4x + 2(1 - \sin^2 4x) = 0$ $-2 \sin^2 4x + 3 \sin 4x + 2 = 0$ $2 \sin^2 4x - 3 \sin 4x - 2 = 0$ $(2 \sin 4x + 1)(\sin 4x - 2) = 0$ $\sin 4x = -\frac{1}{2} \quad \text{or} \quad \sin 4x \neq 2$	✓ identity  ✓ $1 - \sin^2 4x$  ✓ standard form ✓ factors  (4)
5.5.2	$\sin 4x = -\frac{1}{2}$ <i>ref.</i> $\angle = 30^\circ$  $4x = 210^\circ + k \cdot 360^\circ$ or $4x = 330^\circ + k \cdot 360^\circ$ $x = 52,5^\circ + k \cdot 90^\circ ; k \in \mathbb{Z}$ $x = 82,5^\circ + k \cdot 90^\circ ; k \in \mathbb{Z}$	✓ $210^\circ ; 330^\circ$ ✓ $52,5^\circ ; 82,5^\circ$ ✓ $k \cdot 90^\circ ; k \in \mathbb{Z}$  (3)
		[28]

GP



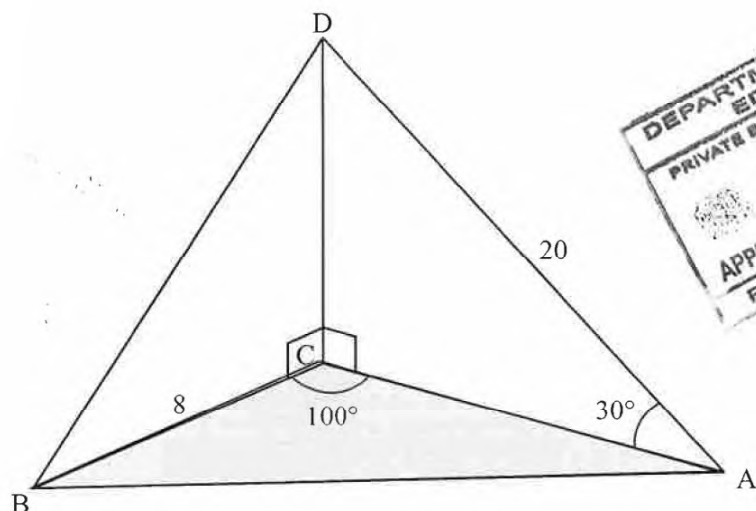


## QUESTION/VRAAG 6

6.1	Period = $180^\circ$	✓ answer (1)
6.2		✓ x-intercepts ✓ turning points ✓ end points (3)
6.3	$y \in [-1; 1]$ <b>OR/OF</b> $-1 \leq y \leq 1$	✓ answer (1)
6.4	$g(x) = -\cos 2x$ $g(x + 45^\circ) = -\cos 2(x + 45^\circ)$ $= -\cos(2x + 90^\circ)$ $= \sin 2x$	✓ $-\cos 2(x + 45^\circ)$ ✓ answer (2)
6.5.1	$x \in (-90^\circ; -45^\circ)$ <b>OR/OF</b> $-90^\circ < x < -45^\circ$	✓✓ $x \in (-90^\circ; -45^\circ)$ (2)
6.5.2	$2\cos 2x - 1 > 0$ $\cos 2x > \frac{1}{2}$ $-\cos 2x < -\frac{1}{2}$ $x \in (-30^\circ; 30^\circ)$ <b>OR/OF</b> $-30^\circ < x < 30^\circ$	✓ $\cos 2x > \frac{1}{2}$ ✓ $-\cos 2x < -\frac{1}{2}$ ✓ $x = \pm 30^\circ$ ✓ interval (4)
		[13]



## QUESTION/VRAAG 7

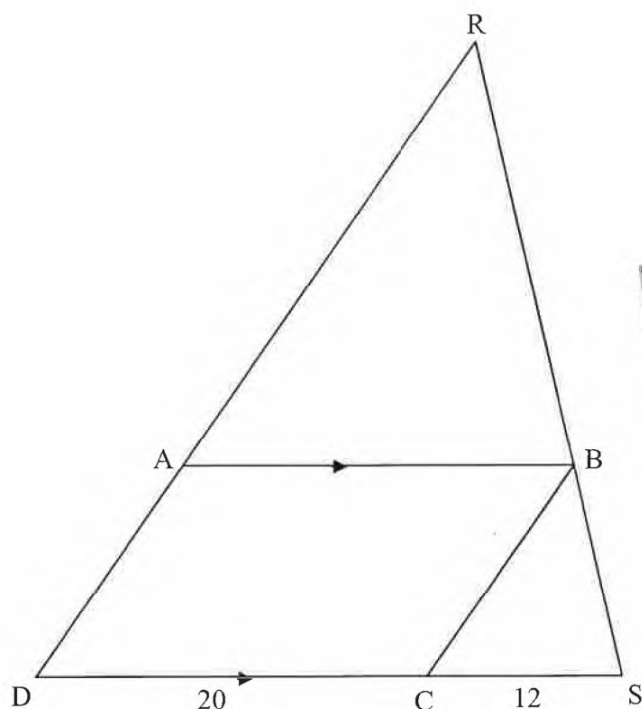


7.1.1	$\frac{AC}{20} = \cos 30^\circ$ $AC = 20 \cos 30^\circ$ $AC = 10\sqrt{3} = 17,32 \text{ units}$ <p><b>OR/OF</b></p> $\frac{AC}{\sin 60^\circ} = \frac{20}{\sin 90^\circ}$ $\therefore AC = 20 \sin 60 = 17,32$	✓ trig ratio ✓ answer (2)
7.1.2	$AB^2 = AC^2 + BC^2 - 2AC \cdot BC \cos \hat{ACB}$ $AB^2 = (10\sqrt{3})^2 + 8^2 - 2(10\sqrt{3})(8) \cos 100^\circ$ $AB = 20,30 \text{ units}$	✓ cosine formula ✓ substitution into cosine formula ✓ answer (3)
7.2	$\frac{\sin \hat{ADB}}{AB} = \frac{\sin \hat{ABD}}{AD}$ $\frac{\sin \hat{ADB}}{20,3} = \frac{\sin 73,4^\circ}{20}$ $\sin \hat{ADB} = \frac{20,3 \sin 73,4^\circ}{20}$ $\hat{ADB} = 76,58^\circ$	✓ sine formula in $\triangle ABD$ ✓ substitution into sine formula ✓ answer (3)
		[8]





8.2



8.2.1	$\frac{DC}{CS} = \frac{20}{12} = \frac{5}{3}$ $\therefore \frac{DC}{CS} = \frac{RB}{BS}$ $\therefore BC \parallel DR \quad [\text{converse line } \parallel \text{ one side of } \Delta \text{ OR sides in the same proportion}]$ $\therefore BC \parallel AD$	✓ S ✓ S ✓ R	(3)
8.2.2	$\frac{AR}{AD} = \frac{RB}{BS} \quad [\text{line } \parallel \text{ one side of } \Delta] \text{ OR } [\text{Prop Theorem } AB \parallel DS]$ $\frac{AR}{AD} = \frac{5}{3}$ $\frac{48 - AD}{AD} = \frac{5}{3}$ $\therefore 5AD = 144 - 3AD$ $AD = 18$ $AB = 20 \quad [\text{opp sides of parm}]$ $\therefore AD : AB = 18 : 20 = 9 : 10$	✓ $\frac{AR}{AD} = \frac{5}{3}$ ✓ $AD = 18$ ✓ ratio	(3)

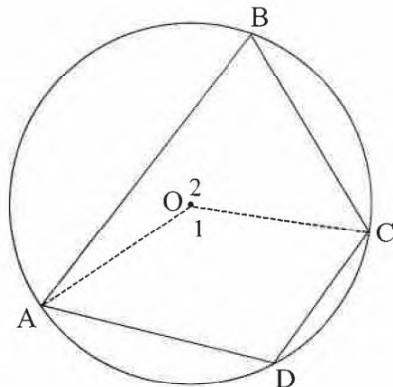






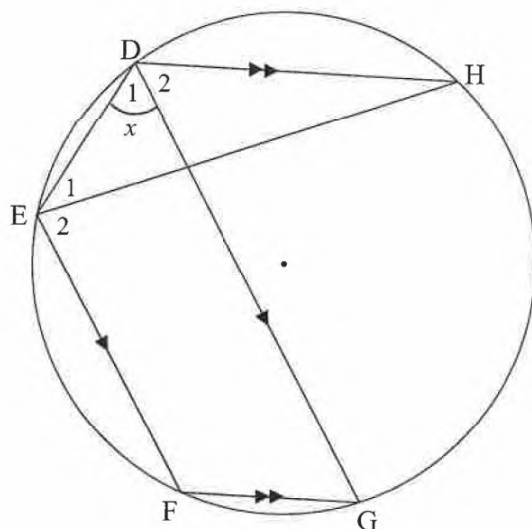
**QUESTION/VRAAG 9**

9.1

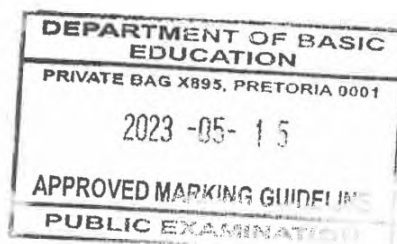


9.1	<p>Constr: Draw radii OA and OC.</p> <p>Proof:</p> <p><math>\hat{O}_1 = 2\hat{B}</math> [<math>\angle</math> at centre = <math>2 \times \angle</math> at circumference]</p> <p><math>\hat{O}_2 = 2\hat{D}</math> [<math>\angle</math> at centre = <math>2 \times \angle</math> at circumference]</p> <p><math>\hat{O}_1 + \hat{O}_2 = 360^\circ</math> [revolution]</p> <p><math>2\hat{B} + 2\hat{D} = 360^\circ</math> [revolution]</p> <p><math>\therefore \hat{B} + \hat{D} = 180^\circ</math></p>	<p>✓ Construction</p> <p>✓ S ✓ R</p> <p>✓ S/R</p> <p>✓ S</p> <p>(5)</p>
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9.2

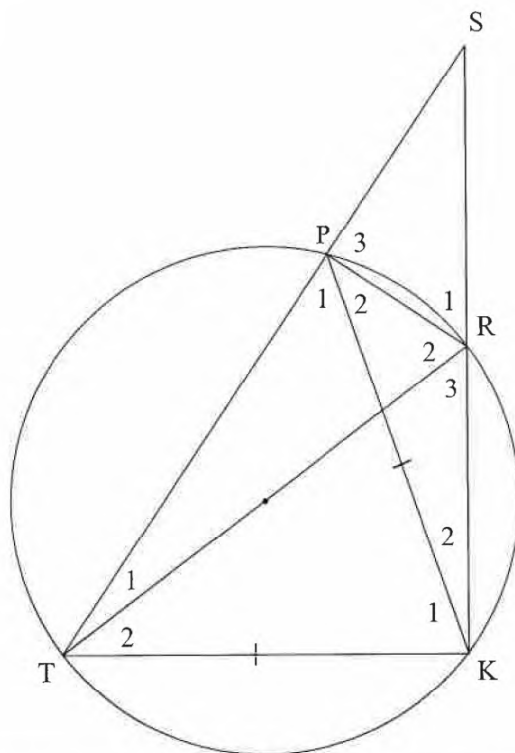


9.2	$\hat{EFG} = 180^\circ - \hat{D}_1$ [opp $\angle$ 's of cyclic quad] $\therefore \hat{EFG} = 180^\circ - x$ $\hat{EFG} = 180^\circ - \hat{G}$ [co-int $\angle$ 's; $EF \parallel DG$ ] $\hat{G} = x$ But $\hat{G} = \hat{D}_2$ [alt $\angle$ 's; $DH \parallel FG$ ] $\therefore \hat{D}_1 = \hat{D}_2 = x$	$\checkmark S \checkmark R$  $\checkmark S / R$  $\checkmark S / R$
		(4)
		[9]



**QUESTION/VRAAG 10**

10.1



10.1.1	$\hat{T}PR = 90^\circ$ [ $\angle$ in semi-circle ] $\hat{S}PR = 90^\circ$ [ $\angle$ 's on a straight line ] $\therefore$ SR is a diameter [ converse $\angle$ in semi-circle ]	$\checkmark$ S $\checkmark$ R $\checkmark$ S $\checkmark$ R	(4)
	<b>OR</b>  $\hat{T}KR = 90^\circ$ [ $\angle$ in semi-circle ] $\hat{S}PR = 90^\circ$ [ ext $\angle$ of cyclic quad ] $\therefore$ SR is a diameter [ converse $\angle$ in semi-circle ] <b>OR</b> [ chord subtends a right angle ]	$\checkmark$ S $\checkmark$ R $\checkmark$ S $\checkmark$ R	(4)





10.1.2	$\hat{R}_1 = \hat{P}\hat{T}K$ [ext $\angle$ of cyclic quad] $\hat{P}_1 = \hat{P}\hat{T}K = \hat{R}_1$ [ $\angle$ s opp equal sides] $\hat{S} + \hat{R}_1 = \hat{P}_1 + \hat{P}_2$ [ext $\angle$ of $\Delta$ ] $\therefore \hat{S} = \hat{P}_2$ [ $\hat{R}_1 = \hat{P}_1$ ]	$\checkmark S \checkmark R$ $\checkmark S / R$ $\checkmark S \checkmark R$	(5)
10.1.3	In $\Delta SPK$ and $\Delta PRK$ $\hat{S} = \hat{P}_2$ [proved] $\hat{K}_2 = \hat{K}_2$ [common] $\Delta SPK \parallel \Delta PRK$ [ $\angle, \angle, \angle$ ] <b>OR/OF</b> In $\Delta SPK$ and $\Delta PRK$ $\hat{S} = \hat{P}_2$ [proved] $\hat{K}_2 = \hat{K}_2$ [common] $\hat{S}\hat{P}K = \hat{P}\hat{R}K$ [sum of $\angle$ s in $\Delta$ ] $\Delta SPK \parallel \Delta PRK$	$\checkmark S$ $\checkmark S$ $\checkmark S/R$ $\checkmark S$ $\checkmark S$ $\checkmark S/R$	(3)
10.2	$\frac{PK}{RK} = \frac{SK}{PK}$ [ $\Delta SPK \parallel \Delta PRK$ ] $PK^2 = SK.RK$ $ST^2 = SK^2 + TK^2$ [Pythagoras] $TK = PK$ [Given] $ST^2 = SK^2 + PK^2$ $ST^2 = SK^2 + SK.RK$ $ST^2 = (2RK)^2 + 2RK.RK$ $ST^2 = 6RK^2$ $ST = \sqrt{6}RK$	$\checkmark S$ $\checkmark S$ $\checkmark PK^2 = SK.RK$ $\checkmark SK = 2RK$ $\checkmark ST^2 = 6RK^2$	(5)
			[17]

TOTAL/TOTAAL: 150

