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**NATIONAL
SENIOR CERTIFICATE**

GRADE 12

MATHEMATICS P2

PREPARATORY EXAMINATIONS

SEPTEMBER 2023

MARK 150

TIME: 3 hours

**N.B. This question paper consists of 12 pages and 1 information sheet.
This paper has an Answer Booklet.**

INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

1. This question paper consists of **11** questions.
2. Answer **ALL** the questions.
3. Number the answers correctly according to the numbering system used in this question paper.
4. Clearly show **ALL** calculations, diagrams, graphs, etc. that you have used in determining your answers.
5. Answers only will **NOT** necessarily be awarded full marks.
6. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
7. If necessary, round off answers to **TWO** decimal places, unless stated otherwise.
8. Diagrams are **NOT** necessarily drawn to scale.
9. An information sheet with formulae is included at the end of the question paper.
10. Write neatly and legibly.

QUESTION 1

Mr Siphokazi supplements his pension by mowing lawns for customers. He measures the areas (x) (in m^2) of 12 of his customers' lawns and the time (y) in minutes, it takes him to mow these lawns. He works 8 hours a day. He recorded the data.

Area (x) (m^2)	360	120	845	602	1 190	530	245	486	350	1 005	320	250
Time (y) (minutes)	50	28	130	75	120	95	55	70	48	110	55	60

- 1.1 Determine the equation of the least squares regression line. (3)
- 1.2 Calculate the value of r , the correlation coefficient for the data. (2)
- 1.3 Given that Mr Siphokazi charges a flat call out fee of R150, as well as R50 per half hour (or part thereof), estimate the charge for mowing a customer's lawn that has an area of 560 m^2
(For example: 100 minutes would be taken as 2 hours). (3)
- 1.4 The local high school wants Mr Siphokazi to mow their rugby field which is rectangular, 100 meters long by 70 meters wide.
 - 1.4.1 Use the regression equation found in 1.1 to calculate the time it would take to mow this area. (1)
 - 1.4.2 Is it possible for him to complete this job in a day?
Give a reason for your answer. (1)

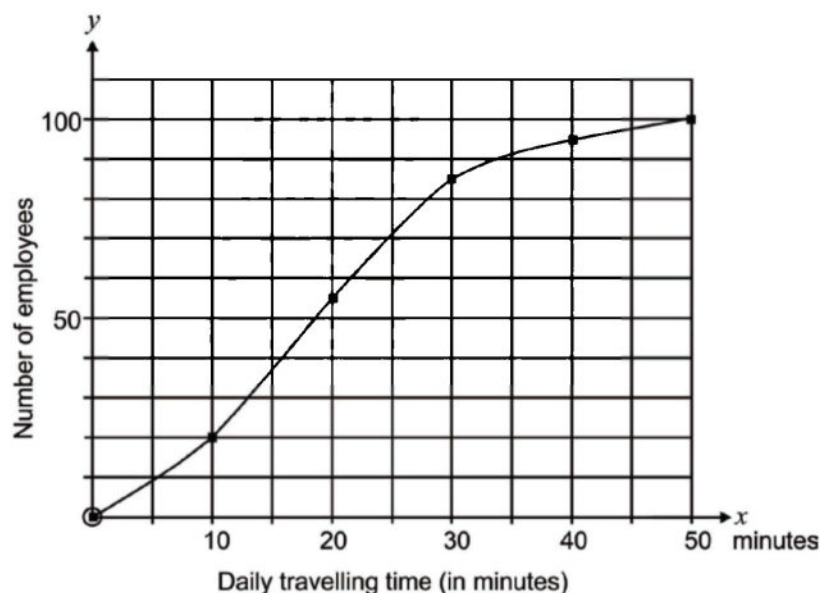
[10]

QUESTION 2

The following table gives the frequency distribution of the daily travelling time (in minutes) from home to work for the employees of a certain company.

Daily travelling time x (in minutes)	Number of employees (f)	Midpoint of Interval	
$0 \leq x < 10$	20		
$10 \leq x < 20$	35		
$20 \leq x < 30$	30		
$30 \leq x < 40$	10		
$40 \leq x < 50$	5		

- 2.1 Calculate the estimated mean travelling time. (3)
- 2.2 Write the modal class of the data. (2)
- 2.3 An ogive was drawn for the given data.
Construct a box-whisker plot for the data in the ANSWER BOOK. (3)

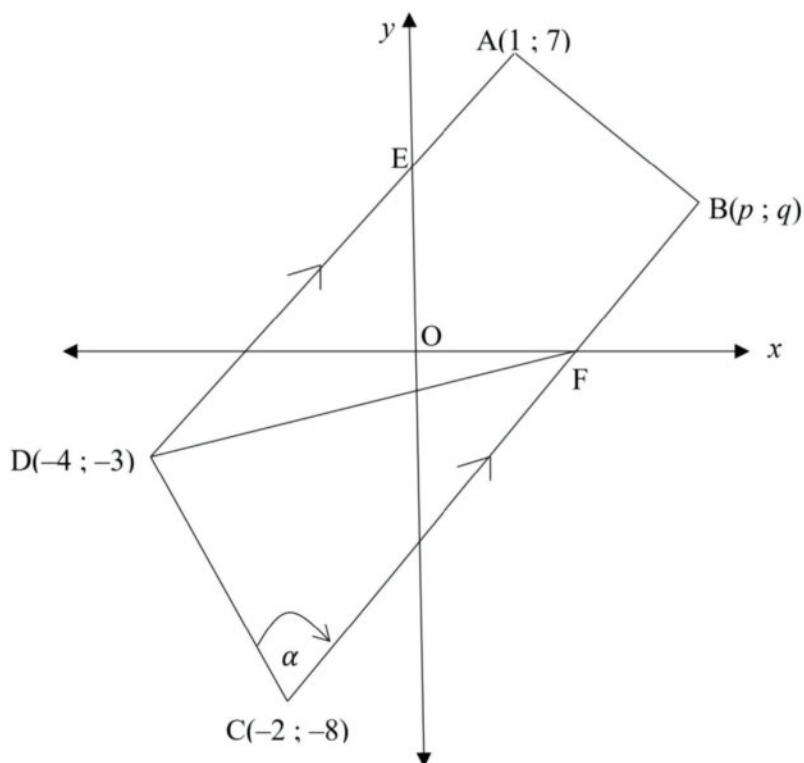


- 2.4 State whether the following statements are TRUE or FALSE.
- 2.4.1 The distribution of these travelling times is positively skewed. (1)
- 2.4.2 The inter-quartile range for the data is 25. (1)
- 2.4.3 35 employees take less than 20 minutes. (1)

[11]

QUESTION 3

Trapezium ABCD is drawn below with $AD \parallel BC$ is drawn. The coordinates of the vertices are $A(1 ; 7)$, $B(p ; q)$, $C(-2 ; -8)$ and $D(-4 ; -3)$. BC intersects the x – axis at F. $\widehat{DCB} = \alpha$. AD intersects the y – axis at E.



- 3.1 Calculate the gradient of AD. (2)
- 3.2 Determine the equation of BC in the form $y = mx + c$. (3)
- 3.3 Determine the coordinates of F. (2)
- 3.4 AMCD is a parallelogram, with M on BC. Determine the coordinates of M. (2)
- 3.5 Show that $\alpha = 48,37^\circ$. (4)
- 3.6 Calculate the area of $\triangle DCF$. (4)

[17]

QUESTION 4

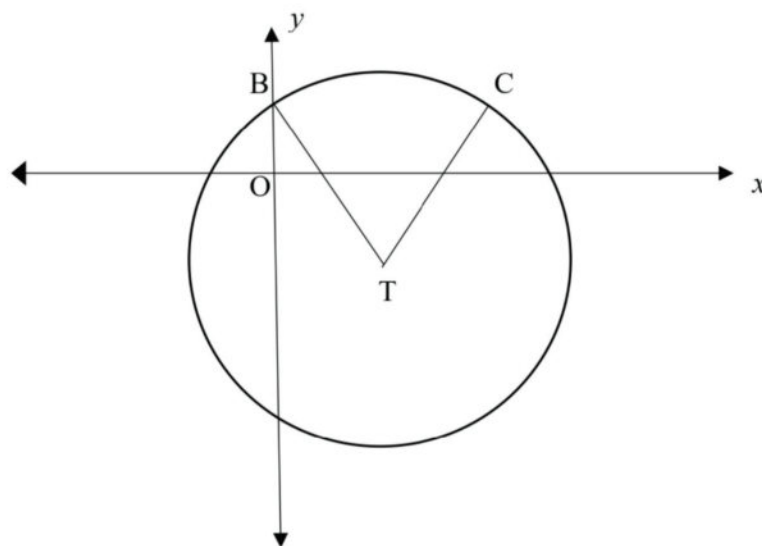
4.1 The equation of a circle is $x^2 + y^2 - 8x + 6y = 15$.

4.1.1 Show that $P(2 ; -9)$ lies on the circle. (2)

4.1.2 Determine the equation of the tangent to the circle at point $P(2 ; -9)$. (6)

4.1.3 A tangent is drawn from $Q(-10 ; 12)$ to the circle. Calculate the length of the tangent. (4)

4.2 The circle, with centre T , and equation $(x - 3)^2 + (y + 2)^2 = 25$ is given below. B is the y -intercept of the circle.



4.2.1 Determine the coordinates of B . (4)

4.2.2 Write down the coordinates of C , if C is the reflection of B in the line $x = 3$. (2)

4.2.3 Another circle with centre M and equation $(x - 12)^2 + (y - 10)^2 = 100$ is given.

(a) Calculate the distance, TM , between the centres. (2)

(b) Do these circles touch or intersect each other? Justify your answer. (2)

[22]

QUESTION 5

5.1 If $\sin 38^\circ = p$, determine the value of the following, **without using a calculator**:

5.1.1 $\cos 218^\circ$ (3)

5.1.2 $\cos 14^\circ$ (3)

5.1.3 $\sin 26^\circ \cos 26^\circ$ (2)

5.2 Evaluate the following trigonometric expression **without using a calculator**:

$$\frac{2 \sin 165^\circ \cos 195^\circ}{\cos 45^\circ \sin 15^\circ - \cos 15^\circ \sin 45^\circ} \quad (5)$$

5.3 Given: $K = \sqrt{3} \cos x + \sin x$.

5.3.1 Write K in the form of $t \sin (x + \theta)$. (3)

5.3.2 Hence, calculate the value of t and θ . (1)

5.3.3 Write down the maximum value of K . (1)

5.4 Prove the identity:

$$5.4.1 \quad \frac{2 \tan \theta - \sin 2\theta}{2 \sin^2 \theta} = \tan \theta \quad (6)$$

5.4.2 Hence, determine the values of θ , $\theta \in [180^\circ; 360^\circ]$ which will make the above identity undefined. (2)

[26]

QUESTION 6

6.1 Sketch the graphs of $f(x) = 2 \sin x$ and $g(x) = \cos(x - 30^\circ)$ for $x \in [-180^\circ; 180^\circ]$ on the grid in the ANSWER BOOK. Indicate the intercepts with the axes and also the turning points. (6)

6.2 Use your graphs to answer the following questions:

6.2.1 Write down the period of g . (1)

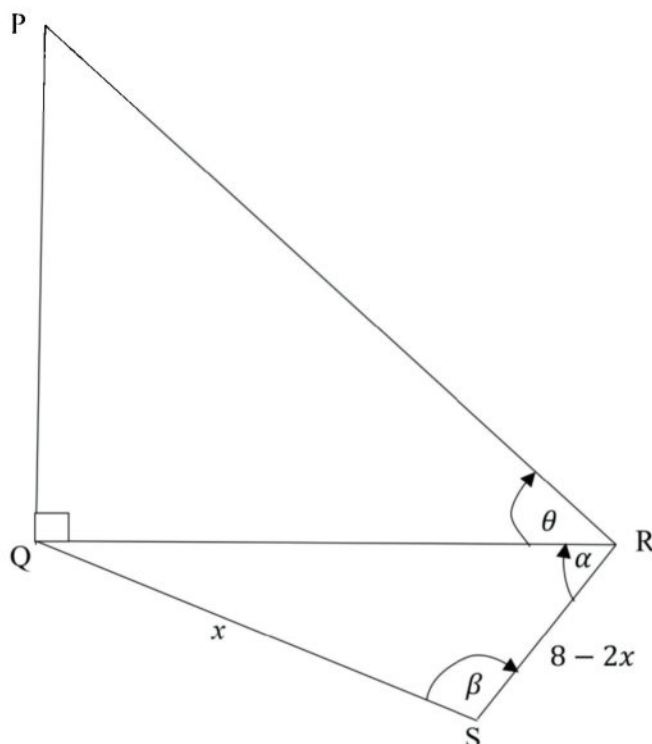
6.2.2 Determine the values of x for which $f(x) > g(x)$. (4)

6.2.3 Write down the values of x for which $f(x) = 1,5 + g(x)$. (2)

[13]

QUESTION 7

In the diagram below, PQ is a vertical mast. R and S are two points in the same horizontal plane as the foot of the mast, Q. $\widehat{QRS} = \alpha$, $\widehat{QSR} = \beta$, $SR = 8 - 2x$ and $SQ = x$. The angle of elevation of P, the top of the mast from R, is θ .



7.1 Express PQ in terms QR and a trigonometric ratio of θ . (1)

7.2 Show that: $PQ = \frac{x \sin \beta \tan \theta}{\sin \alpha}$ (4)

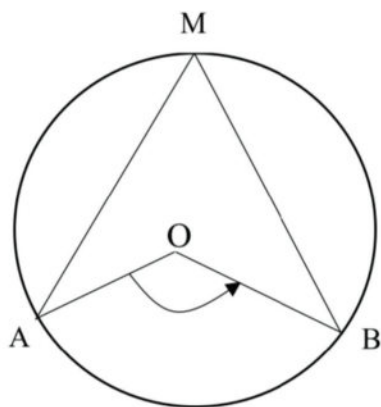
7.3 If $\beta = 60^\circ$, show that the area of $\triangle QSR = 2\sqrt{3}x - \frac{\sqrt{3}}{2}x^2$. (3)

7.4 Determine the value of x for which the area of $\triangle QSR$ will be at a maximum. (3)

[11]

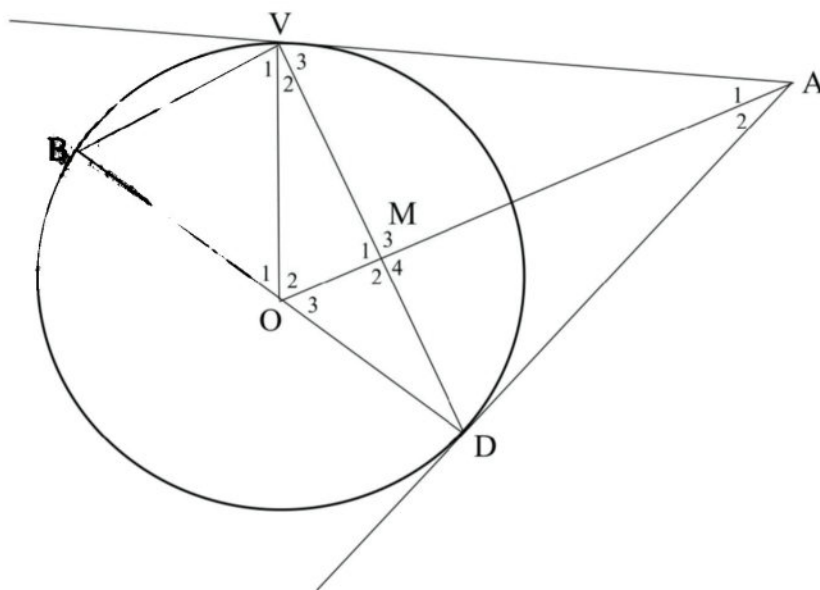
QUESTION 8

- 8.1 In the diagram O is the centre of the circle and M is a point on the circumference of the circle. Arc AB subtends \hat{AOB} at the centre of the circle and \hat{M} at the circumference of the circle.



Use the diagram to prove the theorem that states that $\hat{AOB} = 2\hat{M}$. (5)

- 8.2 From a point A outside the circle, center O, two tangents AD and AV are drawn. AO and VD intersect at M. BOD is a diameter of the circle. BV and VO are drawn. $\hat{VAD} = 40^\circ$



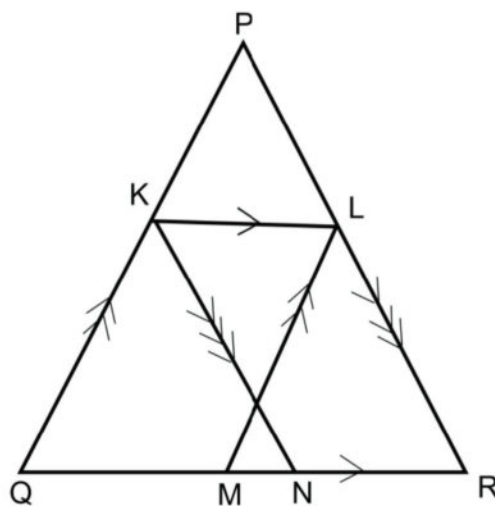
- 8.2.1 Prove that quadrilateral VODA is cyclic. (2)
- 8.2.2 Calculate the magnitude of \hat{O}_1 . (2)
- 8.2.3 Prove that $BV \parallel OA$. (5)

[14]

QUESTION 9

9.1 Complete the following statement: A line drawn parallel to one side of a triangle ... (2)

9.2 In the figure, $KL \parallel QR$. M and N are points on QR such that $KN \parallel PR$ and $LM \parallel PQ$. $PK = 3$ units, $PL = 4$ units, $LR = 6$ units and $MN = 1,8$ units.

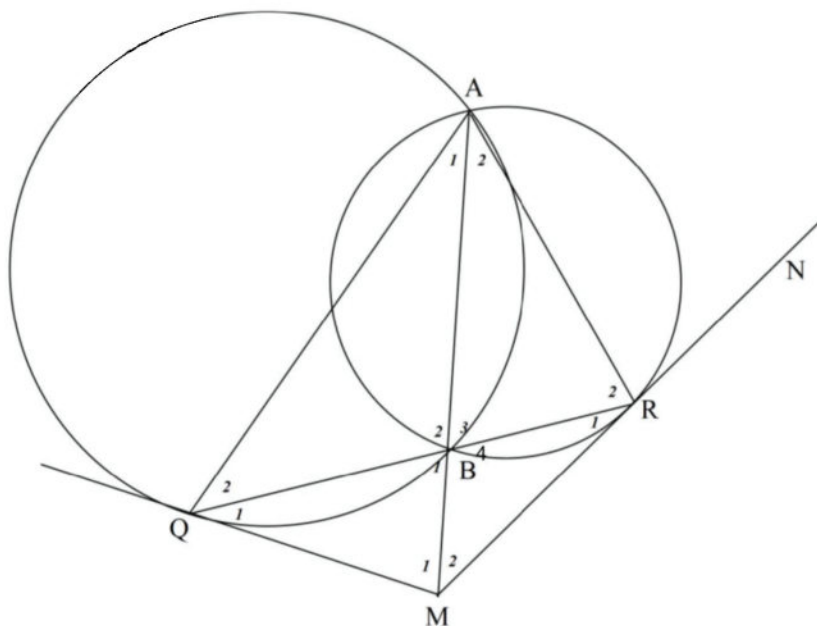


9.2.1 Calculate the length of KQ. (2)

9.2.2 Prove that $QM = NR$. (2)

[6]

In the figure, two circles intersect at A and B. AB produced to M bisects \widehat{QAR} . Tangents MQ and MR meet the circles at Q and R respectively. QBR is a straight line. AQ and AR are drawn.

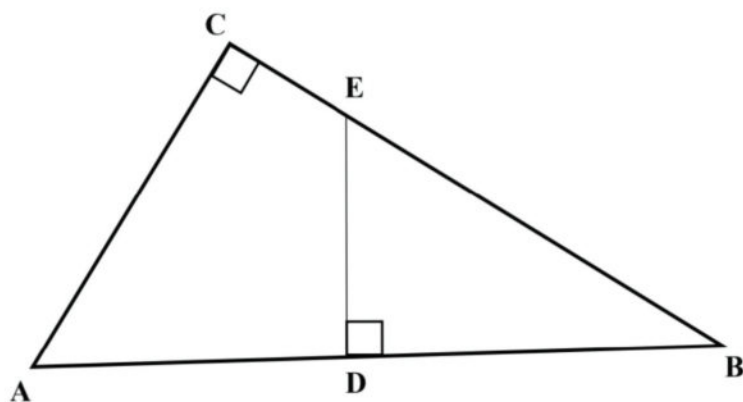

$$10.1 \quad \Delta MQA \parallel \Delta MBQ. \quad (3)$$
$$10..2 \quad MR^2 = AM.MB \quad (5)$$
$$10.3 \quad \frac{MQ^2}{MR^2} = 1 \quad (4)$$

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QUESTION 11

- 11 $\triangle ABC$ is right angled at C. $ED \perp AB$ with E on CB and D on AB.
 $AC = 4,8$ cm and $AB = 8$ cm. $AD = DB$.



- 11.1 Calculate BC, correct to 1 decimal digit. (2)
- 11.2 Complete: $\triangle BAC \sim \dots$ (1)
- 11.3 Hence, or otherwise calculate the area of ADEC. (5)

[8]**GRAND TOTAL: 150**

INFORMATION SHEET: MATHEMATICS
INLIGTING BLADSY

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni)$$

$$A = P(1 - ni)$$

$$A = P(1 - i)^n$$

$$A = P(1 + i)^n$$

$$T_n = a + (n - 1)d$$

$$S_n = \frac{n}{2}(2a + (n - 1)d)$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1}; \quad r \neq 1$$

$$S_\infty = \frac{a}{1 - r}; \quad -1 < r < 1$$

$$F = \frac{x[(1 + i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1 + i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

$$\text{In } \triangle ABC: \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cdot \cos A \quad \text{area } \triangle ABC = \frac{1}{2} ab \cdot \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cdot \cos \beta + \cos \alpha \cdot \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cdot \cos \beta - \cos \alpha \cdot \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cdot \cos \beta - \sin \alpha \cdot \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cdot \cos \beta + \sin \alpha \cdot \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases}$$

$$\sin 2\alpha = 2\sin \alpha \cdot \cos \alpha$$

$$\bar{x} = \frac{\sum f \cdot x}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$