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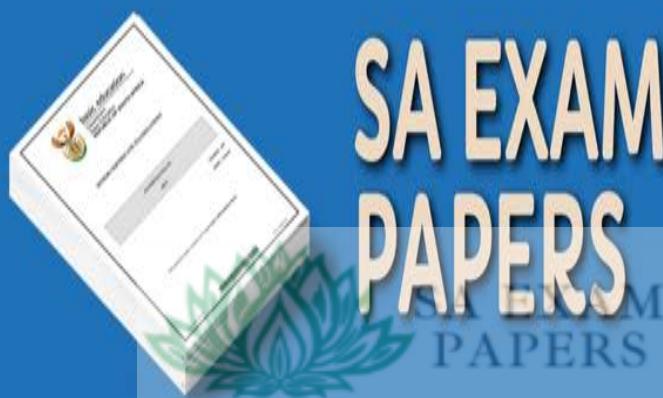
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**NATIONAL
SENIOR CERTIFICATE/
*NASIONALE SENIORSERTIFIKAAT***

GRADE/GRAAD 12

SEPTEMBER 2023

**MATHEMATICS P1/WISKUNDE V1
MARKING GUIDELINE/NASIENRIGLYN**

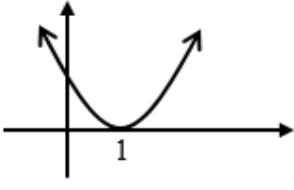
MARKS/PUNTE: 150

This marking guideline consists of 17 pages./
Hierdie nasienriglyn bestaan uit 17 bladsye.

NOTE/LET WEL:

- If a candidate answers a question TWICE, mark the FIRST attempt ONLY.
Indien 'n kandidaat 'n vraag TWEE keer beantwoord, merk SLEGS die EERSTE poging.
- Consistent accuracy applies in ALL aspects of the marking guideline.
Volgehoue akkuraatheid geld deurgaans in ALLE aspekte van die nasienriglyn.
- If a candidate crossed out an attempt of a question and did not redo the question, mark the crossed-out attempt.
Indien 'n kandidaat 'n poging vir 'n vraag deurgetrek het en nie die vraag weer beantwoord het nie, merk die poging wat deurgetrek is.
- The mark for substitution is awarded for substitution into the correct formula.
Die punt vir substitusie word toegeken vir substitusie in die korrekte formule.

QUESTION 1/VRAAG 1

1.1.1	$\begin{aligned}x^2 + x - 30 &= 0 \\(x-5)(x+6) &= 0 \\\therefore x = 5 &\quad \text{or / of} \quad x = -6\end{aligned}$ <p style="text-align: center;">OR/OF</p> $\begin{aligned}x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\&= \frac{-1 \pm \sqrt{(1)^2 - 4(1)(-30)}}{2(1)} \\&= \frac{-1 \pm \sqrt{121}}{2} \\&= 5 \text{ or / of } -6\end{aligned}$	✓ factors / faktore ✓ $x = 5$ ✓ $x = -6$ <p style="text-align: center;">OR/OF</p> ✓ substitution / vervanging ✓ $x = 5$ ✓ $x = -6$	(3)
1.1.2	$\begin{aligned}x(2x-6) &= -3 \\2x^2 - 6x + 3 &= 0 \\x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\&= \frac{-(-6) \pm \sqrt{(-6)^2 - 4(2)(3)}}{2(2)} \\&= \frac{6 \pm \sqrt{12}}{4} \quad \text{OR / OF } \frac{3 \pm \sqrt{3}}{2} \\&= 2,37 \text{ or / of } 0,63\end{aligned}$	✓ standard form / standaardvorm ✓ substitution / vervanging ✓ $x = 2,37$ or / of ✓ $x = 0,63$	(4)
1.1.3	$\begin{aligned}x^2 - 2x + 1 &> 0 \\(x-1)(x-1) &> 0 \\c/v: x &= 1 \\\therefore x &\in \mathbb{R}, x \neq 1\end{aligned}$ 	✓ factors / faktore ✓ $x \in \mathbb{R}, x \neq 1$ (Accuracy/Akkuraatheid)	(3)

1.3	$2x^2 - px + 1 = 0$ <p>For real unequal roots: <i>Vir ongelykereeële wortels:</i></p> $b^2 - 4ac > 0$ $(-p)^2 - 4(2)(1) > 0$ $p^2 - 8 > 0$ $\therefore p < -\sqrt{8} \text{ or } p > \sqrt{8}$	<ul style="list-style-type: none"> ✓ $b^2 - 4ac > 0$ ✓ substitution / <i>vervanging</i> ✓ standard form / <i>standaardvorm</i> ✓ ✓ answer / <i>antwoord</i>
		(5) [25]

QUESTION 2/VRAAG 2

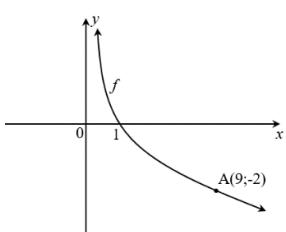
2.1.1	$a + 9d = 21$ $a + 16d = 49$ $\therefore -7d = -28$ $d = 4$	<ul style="list-style-type: none"> ✓ $a + 9d = 21$ ✓ $a + 16d = 49$ ✓ value of d / <i>waarde van d</i> (3)
2.1.2	$a + 9(4) = 21$ $a = -15$ $T_{18} = T_{17} + 4$ $= 49 + 4$ $= 53$ $\therefore T_1 + T_{18}$ $= -15 + 53$ $= 38$	<ul style="list-style-type: none"> ✓ $a = -15$ ✓ $T_{18} = 53$ ✓ answer / <i>antwoord</i> (3)
2.2.1	$T_1 = 4(1) - 19 = -15$ $T_2 = 4(2) - 19 = -11$ $T_3 = 4(3) - 19 = -7$	<ul style="list-style-type: none"> ✓ all three terms / <i>al drie terme</i> (1)
2.2.2	$S_n = \frac{n}{2}[2a + (n-1)d]$ $S_m = \frac{m}{2}[2(-15) + 4(m-1)]$ $1189 = \frac{m}{2}(-30 + 4m - 4)$ $0 = 2m^2 - 17m - 1189$ $(2m+41)(m-29) = 0 \quad \text{or / of}$ $m = \frac{-(-17) \pm \sqrt{(-17)^2 - 4(2)(-1189)}}{2(2)}$ $\therefore m = 29 \quad \text{or / of} \quad m \neq -\frac{41}{2}$	<ul style="list-style-type: none"> ✓ substitution / <i>vervanging</i> and/en = 1 189 ✓ standard form / <i>standaardvorm</i> ✓ method / <i>metode</i> ✓ answer / <i>antwoord</i> (4)

3.2.2	$S_{\infty} = \frac{a}{1-r}$ $\frac{1}{2} = \frac{3^x}{1-3^x}$ $2 \cdot 3^x = 1 - 3^x$ $3 \cdot 3^x = 1$ $3^x = \frac{1}{3}$ $3^x = 3^{-1}$ $\therefore x = -1$	✓ $a = 3^x$ & $r = 3^x$ ✓ substitution / vervanging ✓ answer / antwoord (3) [8]

QUESTION 4/VRAAG 4

4.1	$f(x) = \frac{2}{x-5} + 3$ $x = 5$ $y = 3$	✓ $x = 5$ ✓ $y = 3$ (2)
4.2	$y \in \mathbb{R}$ but/maar $y \neq 3$	✓ $y \neq 3$ (1)
4.3	$f(x) = \frac{2}{x-5} + 3$ <p><i>x</i>-intercept / <i>x</i>-afsnit:</p> $\frac{2}{x-5} + 3 = 0$ $\frac{2}{x-5} = -3$ $-3x + 15 = 2$ $x = \frac{13}{3}$ <p><i>y</i>-intercept / <i>y</i>-afsnit:</p> $y = \frac{2}{0-5} + 3$ $= \frac{13}{5}$ $\therefore \text{Intercepts/Afsnitte: } (\frac{13}{3}; 0) \text{ and } (0; \frac{13}{5})$	✓ substitution / vervanging ✓ $x = \frac{13}{3}$ ✓ $y = \frac{13}{5}$ (3)
4.4		✓ asymptotes / asimptote ✓ <i>y</i> -intercept / <i>y</i> -afsnit ✓ <i>x</i> -intercept / <i>x</i> -afsnit ✓ shape and quadrants vorm en kwadrante (4)
4.5	<p>f is reflected in the <i>x</i>-axis and shifted 2 units downwards. f is gereflekteer in die <i>x</i>-as en 2 eenhede afwaarts geskuif.</p> <p style="text-align: center;">OR/OF</p> <p>f is shifted 2 units upwards and then reflected in the <i>x</i>-axis.</p> <p>f is 2 eenhede opwaarts geskuif en daarna gereflekteer in die <i>x</i>-as.</p>	✓ $f(x)$ reflected / gereflekteer ✓ in the <i>x</i> -axis / in die <i>x</i> -as ✓ shift 2 units / skuif 2 eenhede downwards/upwards afwaarts/opwaarts (3)
	—	[13]

QUESTION 5/VRAAG 5

		
5.1	$f(x) = \log_b x$ $x = b^y$ $9 = b^{-2}$ $b^2 = \frac{1}{9}$ $b = \frac{1}{3}$	✓ substitution / vervanging ✓ answer / antwoord (2)
5.2	$y = \log_{\frac{1}{3}} x$ $x = \log_{\frac{1}{3}} y$ $y = \left(\frac{1}{3}\right)^x \text{ OR/OF } y = 3^{-x}$	✓ swopping x and y omruil van x en y ✓ answer / antwoord (2)
5.3	$0 < x \leq 1$	✓ ✓ answer (Accuracy) antwoord (Akkuraatheid) (2)
5.4	$y = 0$	✓ ✓ answer (Accuracy) antwoord (Akkuraatheid) (2)
		[8]

QUESTION 6/VRAAG 6

6.1	$\begin{aligned}f(x) &= x^2 - 6x + 11 \\&= x^2 - 6x + 9 - 9 + 11 \\&= (x-3)^2 + 2\end{aligned}$ <p>\therefore At TP : $x = 3$ and / en $y = 2$</p> <p style="text-align: center;">OR/OF</p> $\begin{aligned}f(x) &= x^2 - 6x + 11 \\x &= -\frac{b}{2a} = -\frac{(-6)}{2(1)} \\&= 3 \\ \therefore y &= 3^2 - 6(3) + 11 \\&= 2\end{aligned}$ <p>\therefore At TP : $x = 3$ and / en $y = 2$</p>	<ul style="list-style-type: none"> ✓ completing the square vierkantsvoltooiing ✓ $(x-3)^2 + 2$ ✓✓ values for x and y waardes van x en y
6.2	$\begin{aligned}m_g &= \tan 63,44^\circ \\&= 2 \\y - 2 &= 2(x-3) \\y &= 2x - 4\end{aligned}$	<ul style="list-style-type: none"> ✓ $m_g = 2$ ✓ substitution / vervanging ✓ value of x / waarde van x ✓ substitution / vervanging ✓ value of y / waarde van y
6.3	$\begin{aligned}f(x) &= g(x) \\x^2 - 6x + 11 &= 2x - 4 \\x^2 - 8x + 15 &= 0 \\(x-3)(x-5) &= 0 \\x = 3 \text{ or / of } x &= 5 \\ \therefore y &= 2(5) - 4 \\&= 6 \\ \therefore S(5 ; 6) &\end{aligned}$ <div style="border: 1px solid black; padding: 5px; margin-left: 20px;"> CA only if g is linear VA slegs as g lineêr is </div>	<ul style="list-style-type: none"> ✓ equating / gelyk stel ✓ standard form / standaardvorm ✓ x values / x-waardes ✓ S coordinates / S-koördinate

6.4.1	$1 \leq x \leq 5$	✓✓ answer / antwoord (2)
6.4.2	$k \leq -2$ Accept / Aanvaar $k < -2$ for 1 mark / vir 1 punt	✓✓ answer / antwoord (2)
		[15]

QUESTION 7/VRAAG 7

7.1	$A = P(1+i)^n$ $166\,433 = 97\,000 \left(1 + \frac{0,091}{4}\right)^{4n}$ $\frac{166\,433}{97\,000} = \left(\frac{4\,091}{4\,000}\right)^n$ $\therefore 4n = \log_{\frac{4091}{4000}} \frac{166\,433}{97\,000}$ $= 24$ $\therefore n = 6 \text{ years / jaar}$	✓ $\frac{0,091}{4}$ ✓ substitution into correct formula <i>vervanging in korrekte formule</i> ✓ correct use of logs <i>korrekte gebruik van logs</i> ✓ answer / antwoord (4)
7.2.1	$A = P(1-i)^n$ $= 482\,000(1-0,147)^5$ $= R217\,666,80$	✓ substitution into correct formula <i>vervanging in korrekte formule</i> ✓ answer / antwoord (2)
7.2.2	$A = P(1+i)^n$ $= 482\,000(1+0,081)^5$ $= R711\,500,99$	✓ substitution into correct formula <i>vervanging in korrekte formule</i> ✓ answer / antwoord (2)

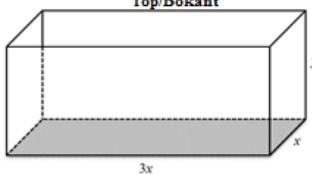
<p>7.2.3 Required amount / <i>Bedrag benodig:</i> $= R\ 711\ 501 - R\ 217\ 666,80$ $= R\ 493\ 834,20$</p> $F = \frac{x[(1+i)^n - 1]}{i}$ $493834,20 = \frac{x \left[\left(1 + \frac{0,073}{12}\right)^{60} - 1 \right]}{\frac{0,073}{12}} \left(1 + \frac{0,073}{12}\right)$ $\therefore x = \frac{493834,20 \times \frac{0,073}{12}}{\left[\left(1 + \frac{0,073}{12}\right)^{60} - 1 \right] \left(1 + \frac{0,073}{12}\right)}$ $= R\ 6803,01$	<p>✓ amount / <i>bedrag</i></p> <p>✓ correct formula / <i>korrekte formule</i></p> <p>✓ $n = 60$ and / en $i = \frac{0,073}{12}$</p> <p>✓ $\frac{x \left[\left(1 + \frac{0,073}{12}\right)^{60} - 1 \right]}{\frac{0,073}{12}}$</p> <p>✓ $\times \left(1 + \frac{0,073}{12}\right)$</p> <p>✓ answer / <i>antwoord</i></p>
	<p>(6)</p> <p>[14]</p>

QUESTION 8/VRAAG 8

8.1	$f(x) = 1 - x^2$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $= \lim_{h \rightarrow 0} \frac{1 - (x+h)^2 - (1 - x^2)}{h}$ $= \lim_{h \rightarrow 0} \frac{1 - x^2 - 2xh - h^2 - 1 + x^2}{h}$ $= \lim_{h \rightarrow 0} \frac{-2xh - h^2}{h}$ $= \lim_{h \rightarrow 0} \frac{h(-2x - h)}{h}$ $= \lim_{h \rightarrow 0} (-2x - h)$ $= -2x$	✓ substitution / vervanging ✓ expansion / uitbreiding ✓ simplification / vereenvoudiging ✓ factorisation / faktorisering ✓ answer / antwoord (5) OR/OF
	$f(x) = 1 - x^2$ $f(x+h) - f(x) = 1 - (x+h)^2 - (1 - x^2)$ $= 1 - x^2 - 2xh - h^2 - 1 + x^2$ $= -2xh - h^2$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $= \lim_{h \rightarrow 0} \frac{-2xh - h^2}{h}$ $= \lim_{h \rightarrow 0} \frac{h(-2x - h)}{h}$ $= \lim_{h \rightarrow 0} (-2x - h)$ $= -2x$	✓ substitution / vervanging ✓ expansion / uitbreiding ✓ simplification / vereenvoudiging ✓ factorisation / faktorisering ✓ answer / antwoord (5)
8.2.1	$D_x \left[\left(x - \frac{1}{x} \right)^2 \right] = D_x \left(x^2 + \frac{1}{x^2} - 2 \right)$ $= D_x \left(x^2 + x^{-2} - 2 \right)$ $= 2x - 2x^{-3}$	✓ $D_x (x^2 + x^{-2} - 2)$ ✓ $2x$ and / en constant/konstante is 0 ✓ $-2x^{-3}$ (3)
8.2.2	$y = \frac{x^5}{10} - \frac{2}{\sqrt{x}}$ $= \frac{1}{10} x^5 - 2x^{-\frac{1}{2}}$ $\therefore \frac{dy}{dx} = \frac{1}{2} x^4 + x^{-\frac{3}{2}}$	✓ $2x^{-\frac{1}{2}}$ ✓ $\frac{1}{2} x^4$ ✓ $x^{-\frac{3}{2}}$ (3)
		[11]

<p>9.3.2</p> $f''(x) = -12x + 10$ $-12x + 10 = 0$ $x = \frac{5}{6}$ $\therefore x > \frac{5}{6}$ <p style="text-align: center;">OR/OF</p> $x = -\frac{b}{3a}$ $= -\frac{5}{3(-2)}$ $= \frac{5}{6}$ $\therefore x > \frac{5}{6}$	<p>$\checkmark f''(x) = -12x + 10$</p> <p>$\checkmark$ value of x / waarde van x</p> <p>\checkmark answer / antwoord (3)</p> <p style="text-align: center;">OR/OF</p> <p>\checkmark substitution / vervanging</p> <p>\checkmark value of x / waarde van x</p> <p>\checkmark answer / antwoord (3)</p>
<p>9.4</p> $f'(x) = -6x^2 + 10x + 4$ $m = f'(-1) = -6(-1)^2 + 10(-1) + 4$ $= -12$ $\therefore y = -12x + c$ $0 = -12(-1) + c$ $c = -12$ $y = -12x - 12$	<p>$\checkmark f'(x) = -6x^2 + 10x + 4$</p> <p>$\checkmark m$</p> <p>$\checkmark$ substitution / vervanging</p> <p>\checkmark answer / antwoord (4)</p>
	[17]

QUESTION 10/VRAAG 10

10.1	 <p>$3x^2 + 2xy + 6xy = 147$</p> <p>$3x^2 + 8xy = 147$</p> <p>$\therefore y = \frac{147 - 3x^2}{8x}$.</p>	<p>$\checkmark 3x^2 + 2xy + 6xy = 147$</p> <p>$\checkmark$ simplifying / vereenvoudiging (2)</p>
10.2	$\begin{aligned} V &= lwh \\ &= 3x \cdot x \cdot y \\ &= 3x^2 \left(\frac{147 - 3x^2}{8x} \right) \\ &= \frac{441x}{8} - \frac{9x^3}{8} \\ \\ V'(x) &= \frac{441}{8} - \frac{27x^2}{8} \\ \\ \therefore \frac{441}{8} - \frac{27x^2}{8} &= 0 \\ 27x^2 &= 441 \\ x^2 &= \frac{441}{27} \\ x &= \frac{21}{3\sqrt{3}} \quad (= 4,04) \end{aligned}$	<p>$\checkmark 3x \cdot x \cdot y$</p> <p>$\checkmark$ substitution / vervanging</p> <p>$\checkmark V'(x) = 0$</p> <p>\checkmark simplification / vereenvoudiging</p> <p>\checkmark answer / antwoord (5)</p>
		[7]

QUESTION 11/VRAAG 11

		WATCH SOCCER/ KYK SOKKER	WATCH RUGBY/ KYK RUGBY	TOTAL/ TOTAAL						
Female / Vroulik		72	a	120						
Male / Manlik		54	36	90						
Total / Totaal		b	84	210						
11.1.1	$a = 48$ $b = 126$		$\checkmark \ a = 48$ $\checkmark \ b = 126$	(2)						
11.1.2	$P(F \text{ and } en WS) = \frac{72}{210}$		$\checkmark \checkmark \text{ answer / antwoord}$	(2)						
11.1.3	(For independent events) / (Vir onafhanklike gebeurtenisse) $P(M) \times P(R) = P(M \text{ and } en R)$ $P(M) \times P(R) = \frac{90}{210} \times \frac{84}{210}$ $= \frac{6}{35}$ $\square 0,17$ $P(M \text{ and } en R) = \frac{36}{210}$ $= \frac{6}{35}$ ∴ The events are independent $Die \text{ gebeurtenisse is onafhanklik}$		$\checkmark \frac{90}{210} \times \frac{84}{210}$ $\checkmark \text{ answer / antwoord}$ $\checkmark \frac{36}{210}$ $\checkmark \text{ conclusion / gevolgtrekking}$	(4)						
11.2.1	<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>26</td> <td>25</td> <td>24</td> <td>10</td> <td>9</td> <td>8</td> </tr> </table> $26 \times 25 \times 24 \times 10 \times 9 \times 8$ $= 11\ 232\ 000$		26	25	24	10	9	8	$\checkmark \text{ method / metode}$ $\checkmark \text{ answer / antwoord}$	(2)
26	25	24	10	9	8					

<p>11.2.2</p> $\begin{aligned} & 5 \times 25 \times 24 \times 9 \times 8 \times 3 \\ & = 648\ 000 \end{aligned}$ $\begin{aligned} & P(\text{Vowel / Factor of 9}) / P(\text{Vokaal / Faktor van 9}) \\ & = \frac{648\ 000}{11232\ 000} \\ & = \frac{3}{52} \end{aligned}$	<ul style="list-style-type: none"> ✓ $5 \times 25 \times 24$ ✓ $9 \times 8 \times 3$ ✓ 11232 000 as denominator / as noemer ✓ answer / antwoord
(4)	

TOTAL/TOTAAL: 150