

SA's Leading Past Year

Exam Paper Portal

S T U D Y

You have Downloaded, yet Another Great
Resource to assist you with your Studies ☺

Thank You for Supporting SA Exam Papers

Your Leading Past Year Exam Paper Resource Portal

Visit us @ www.saexamapers.co.za





Province of the
EASTERN CAPE
EDUCATION



**NATIONAL
SENIOR CERTIFICATE
*NASIONALE
SENIORSERTIFIKAAT***

GRADE/GRAAD 12

SEPTEMBER 2023

**MATHEMATICS P2/WISKUNDE V2
MARKING GUIDELINE/NASIENRIGLYN**

MARKS/PUNTE: 150

This marking guideline consists of 14 pages.
Hierdie nasienriglyn bestaan uit 14 bladsye.

QUESTION 1/VRAAG 1

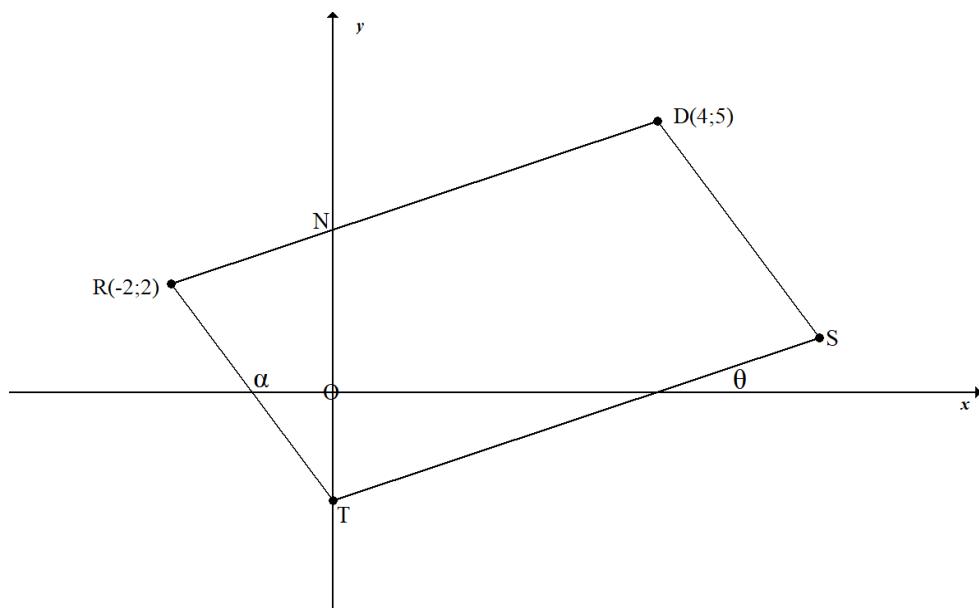
Data Set / Datastel:		29 27 24 31 22 19 30	
1.1.1(a)	Mean / Gemiddelde	$\frac{182}{7} = 26$	✓✓ mean / gemiddelde (2)
1.1.1(b)	Standard deviation / standaardafwyking	$= 4,14$	✓ SD / standaardafwyking (1)
1.1.2	$\{26 - 4,14; 26 + 4,14\} = \{21, 86; 30, 14\}$ 5 players / spelers		✓✓ calculations berekening ✓ answer / antwoord (3)
1.1.3	Rugby team has the same average number of push-ups. The rugby team results were clustered around the mean because of the smaller standard deviation. <i>Rugbyspan het dieselfde gemiddelde aantal opstote. Die rugbyspan se uitslae was rondom die gemiddelde gegroepeer agv die kleiner standaardafwyking.</i>		✓✓ for any two valid comments using SD and the mean <i>Vir enige twee geldige opmerkings in gebruik van standaardafwyking en die gemiddelde</i> (2)
1.2.1	50%		✓ answer / antwoord (1)
1.2.2	Mean / Gemiddelde Distribution skewed to the right. (positively skewed) <i>Verspreiding is skeef na regs (positief skeef)</i>		✓ answer / antwoord ✓ reason / rede (2)
			[11]

QUESTION 2/VRAAG 2

Third Term % Derde Kw. %	71	80	59	38	41	98	80	88	91	94	64	94	70	42	64
Final Term % Finale Kw. %	74	77	58	41	42	98	78	92	85	92	68	96	73	52	71

2.1	$a = 9,035$ $b = 0,895$ $\hat{y} = 9,035 + 0,895x$	✓ for a / vir a ✓ for b / vir b ✓ for equation / vir vergelyking (3)
2.2	$r = 0,98$	✓ answer / antwoord (1)
2.3.1	$y = 9,035 + 0,895(48)$ $y \approx 52$	✓ substitution / vervanging ✓ answer / antwoord (2)
2.3.2	correlation is very strong OR 48 is within domain of regression line. <i>korrelasie is baie sterk OF 48 is binne die gebied van die regressie-lyn.</i>	✓ answer / antwoord (1)
2.4.1	50% is outside the domain of the line (data set) OR (50 ; 80) is an outlier. <i>50% is buite die gebied van die lyn (datastel) OF (50 ; 80) is 'n uitskieter</i>	✓ answer / antwoord (1)
2.4.2	Increase the gradient / Vermeerder die gradiënt	✓ answer / antwoord (1)
		[9]

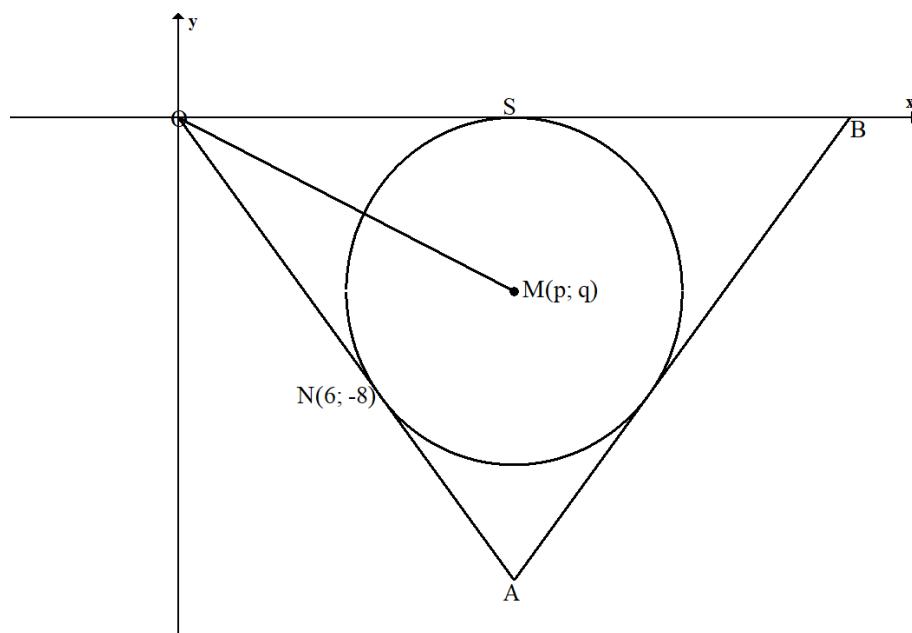
QUESTION 3 / VRAAG 3



3.1	T(0; -2)	✓ answer / antwoord	(1)
3.2.1	$m_{RT} = \frac{2-(-2)}{-2-0} = -\frac{4}{2} = -2$	✓ substitution / vervanging ✓ answer / antwoord	(2)
3.2.2	$\tan \theta = \frac{1}{2}$ $\therefore \theta = 26,57^\circ$ $\tan \alpha = -2$ $\therefore \alpha = 116,57^\circ$ $\therefore R\hat{D}S = 116,57^\circ - 26,57^\circ = 90^\circ$	✓ for / vir $\tan \theta = \frac{1}{2}$ ✓ for / vir $\theta = 26,57^\circ$ ✓ for / vir $\tan \alpha = -2$ ✓ for / vir $\alpha = 116,57^\circ$ ✓ $R\hat{D}S = 90^\circ$	
	OR / OF	OR / OF	
	$m_{TS} = \frac{1}{2}$ $m_{RT} = -2$ $m_{TS} \times m_{RT} = -1$ $R\hat{D}S = 90^\circ$	✓ $m_{TS} = \frac{1}{2}$ ✓ $m_{RT} = -2$ ✓✓ product of gradients <i>produk van gradiënte</i> ✓ $R\hat{D}S = 90^\circ$	(5)
3.3	$y = \frac{1}{2}x + c$ $2 = \frac{1}{2}(-2) + c$ $c = 3$ $\therefore y = \frac{1}{2}x + 3$	✓ gradient / gradiënt ✓ substitution of point R or D <i>vervanging van punt R of D</i> ✓ answer / antwoord	(3)

3.4	<p>RDST is a parallelogram (opposite sides parallel) <i>RDST is 'n parallelogram (teenoorst. sye ewewydig)</i> Midpoint of DT / <i>Middelpunt van DT:</i> $\left(\frac{4+0}{2}; \frac{5-2}{2}\right) = \left(2; \frac{3}{2}\right)$ <p>Midpoint of RS is the same as midpoint of DT (diagonals bisect each other.) <i>Middelpunt van RS is dieselfde as die middelpunt van DT (hoeklyne halveer mekaar)</i></p> <p>Midpoint of RS / <i>Middelpunt van RS:</i> $\left(2; \frac{3}{2}\right)$</p> <p style="text-align: center;">OR / OF</p> <p>$S(6; 1)$ Midpoint of RS / <i>Middelpunt van RS:</i> $\left(\frac{6-2}{2}; \frac{1+2}{2}\right) = \left(2; \frac{3}{2}\right)$</p> </p>	<ul style="list-style-type: none"> ✓ substitution in the MP formula <i>vervanging in die MP formule</i> ✓ S/R ✓ answer / <i>antwoord</i> <p style="text-align: center;">OR / OF</p> <ul style="list-style-type: none"> ✓✓ $S(6; 1)$ ✓ answer / <i>antwoord</i> 	
3.5	<p>$N(0; 3)$ $RN = \sqrt{2^2 + 1^2} = \sqrt{5}$ $RT = \sqrt{2^2 + 4^2} = \sqrt{20}$</p> <p>Area / <i>Oppervlakte</i> = $\frac{1}{2} \times \sqrt{20} \times \sqrt{5}$ $= 5$ square units / <i>eenhede</i>²</p> <p style="text-align: center;">OR / OF</p> <p>$TN = 5$ units / <i>eenhede</i> Height / <i>Hoogte</i> = 2 units / <i>eenhede</i> $Area / Oppervlakte = \frac{1}{2} \times 5 \times 2$ Area / <i>Oppervlakte</i> = 5 square units / <i>eenhede</i>²</p>	<ul style="list-style-type: none"> ✓ coordinates of N <i>koördinate van N</i> ✓ for / vir RN ✓ for / vir RT ✓ for the answer / <i>vir die antwoord</i> <p style="text-align: center;">OR / OF</p> <ul style="list-style-type: none"> ✓ TN = 5 units / <i>eenhede</i> ✓ Height/hoogte = 2 units / <i>eenhede</i> ✓ sub. into formula <i>vervanging in formule</i> ✓ answer / <i>antwoord</i> 	(3)
			(4)
			[18]

QUESTION 4 / VRAAG 4



4.1.1	$ON = \sqrt{(6 - 0)^2 + (-8)^2}$ $= \sqrt{100} = 10 \text{ units / eenhede}$	✓ substitution in correct formula <i>vervanging in korrekte formule</i> ✓ answer / antwoord	(2)
4.1.2	$ON = OS$ (tangents from the same point) <i>(raaklyne vanaf dieselfde punt)</i> $\therefore p = 10 \text{ units / eenhede}$	✓ S and/en R ✓ answer / antwoord	(2)
4.1.3	$ON \perp NM$ (tan – radius) / (raaklyn – radius) $m_{ON} = \frac{-8}{6} = \frac{-4}{3}$ $m_{NM} = \frac{3}{4}$	✓ S and/en R ✓ gradient of ON / <i>gradiënt van ON</i> ✓ gradient of NM <i>gradiënt van NM</i>	(3)
4.1.4	$m_{NM} = \frac{q + 8}{10 - 6} = \frac{3}{4}$ $\frac{q + 8}{4} = \frac{3}{4}$ $q = -5$	✓ for subs and equating <i>vir vervanging en gelyk stel</i> ✓ answer / antwoord	(2)
4.2	$MS = r = 5 \text{ units / eenhede}$ $(x - 10)^2 + (y + 5)^2 = 25$	✓ radius / radius ✓ centre sub/ <i>vervang middelpunt</i> ✓ answer / antwoord	(3)
4.3	$k = 5$ OR/OF $k = 15$	✓ $k = 5$ OR/OF ✓ $k = 15$	(2)

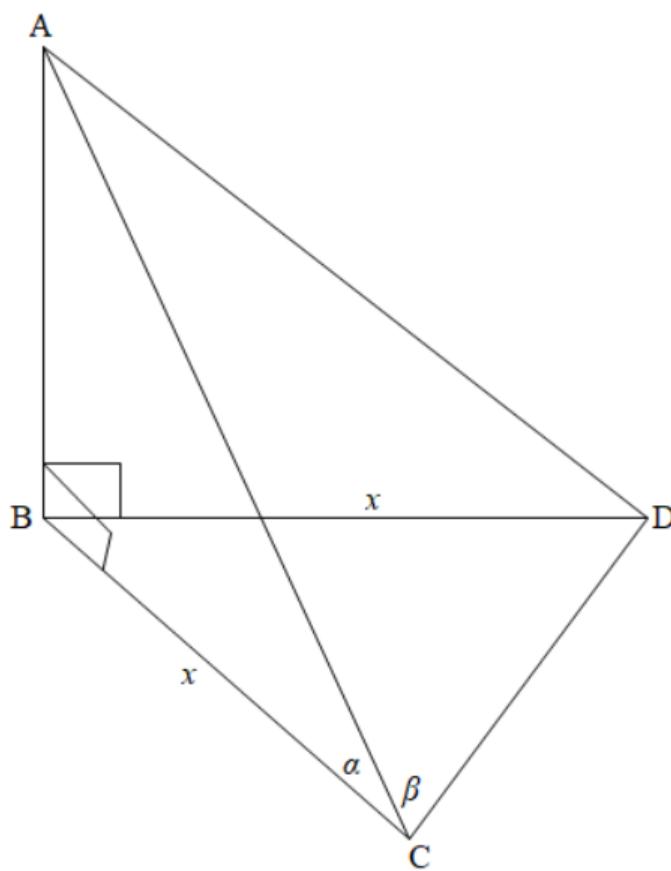
4.4	<p>Coordinates of the point directly opposite N is C. <i>Koördinate van die punt regoor N is C.</i></p> $C\left(\frac{x+6}{2} = 10; \frac{y-8}{2} = -5\right)$ $C(14; -2)$ <p>Equation of the tangent at C: <i>Vergelyking van die raaklyn by C:</i></p> $y + 2 = -\frac{4}{3}(x - 14)$ $y = -\frac{4}{3}x + \frac{50}{3}$ $\therefore 0 < t < \frac{50}{3}$	<ul style="list-style-type: none"> ✓ formula and sub / <i>formule en vervanging</i> ✓ for x-coordinate <i>vir x-koördinaat</i> ✓ for y-coordinate <i>vir y-koördinaat</i> ✓ substitution / vervanging ✓ for the answer / <i>vir die antwoord</i> ✓ for the value of t. <i>vir die waarde van t</i> 	(6)
4.5	<p>They will not touch. The new circle is the old circle shifted up by 11. <i>Hulle sal nie raak nie.</i> <i>Die nuwe sirkel is die ou sirkel 11 eenhede opwaarts geskuif.</i></p>	<ul style="list-style-type: none"> ✓ answer / <i>antwoord</i> ✓ any valid reason / <i>enige geldige antwoord</i> 	(2)
			[22]

QUESTION 5/VRAAG 5

5.1.1	$\begin{aligned} & \sin 594^\circ \\ &= \sin 234^\circ \\ &= -\sin 54^\circ \\ &= -p \end{aligned}$	$\checkmark - \sin 54^\circ$ $\checkmark - p$	(2)
5.1.2	$\begin{aligned} & \cos 36^\circ \\ &= p \end{aligned}$	$\checkmark \checkmark$ answer / antwoord	(2)
5.1.3	$\begin{aligned} & \cos 18^\circ \\ &= \sin 72^\circ \\ &= \sin 2(36^\circ) \\ &= 2 \sin 36^\circ \cos 36^\circ \\ &= 2 \left(\frac{\sqrt{1-p^2}}{1} \right) \left(\frac{p}{1} \right) \\ &= 2p \left(\sqrt{1-p^2} \right) \end{aligned}$	\checkmark for / vir $\sin 72^\circ$ \checkmark for / vir $\sin 2(36^\circ)$ \checkmark for / vir $2 \sin 36^\circ \cos 36^\circ$ \checkmark for / vir $2p \left(\sqrt{1-p^2} \right)$	(4)
5.2	$\begin{aligned} & \frac{\cos 140^\circ - \sin(90^\circ - \theta)}{\sin 410^\circ + \cos(-\theta)} \\ &= \frac{\cos(90^\circ + 50^\circ) - \cos \theta}{\sin 50^\circ + \cos \theta} \\ &= \frac{-\sin 50^\circ - \cos \theta}{\sin 50^\circ + \cos \theta} \\ &= \frac{-(\sin 50^\circ + \cos \theta)}{(\sin 50^\circ + \cos \theta)} \\ &= -1 \end{aligned}$	$\checkmark - \sin 50^\circ \checkmark \cos \theta$ $\checkmark \sin 50^\circ \checkmark \cos \theta$ \checkmark for the common factor <i>vir die gemene faktor</i> \checkmark for the answer <i>vir die antwoord</i>	(6)

5.3	$\begin{aligned} & \cos(x + 65^\circ) \cdot \cos(x + 20^\circ) - \sin(x + 245^\circ) \cdot \sin(x + 20^\circ) \\ &= \cos(x + 65^\circ) \cdot \cos(x + 20^\circ) + \sin(x + 65^\circ) \cdot \sin(x + 20^\circ) \\ &= \cos[(x + 65^\circ) - (x + 20^\circ)] \\ &= \cos 45^\circ \\ &= \frac{1}{\sqrt{2}} \end{aligned}$	<ul style="list-style-type: none"> ✓ reduction / reduksie ✓ compound angle saamgestelde hoek ✓ $\cos 45^\circ$ ✓ answer / antwoord 	(4)
5.4	$\begin{aligned} \cos^2 x - \sin^2 x &= \frac{1}{2} \\ \cos 2x &= \frac{1}{2} \\ 2x &= 60^\circ + 360^\circ \cdot k \text{ or/of } 2x = 300^\circ + 360^\circ \cdot k \\ x &= 30^\circ + 180^\circ \cdot k \text{ or/of } x = 150^\circ + 180^\circ \cdot k \quad k \in \mathbb{Z} \end{aligned}$ <p style="text-align: center;">OR / OF</p> $\begin{aligned} 2 \cos^2 x - 2 \sin^2 x &= 1 \\ 2 \cos^2 x - 2 \sin^2 x &= \sin^2 x + \cos^2 x \\ 3 \sin^2 x &= \cos^2 x \\ \tan^2 x &= \frac{1}{3} \\ \tan x &= \frac{1}{\sqrt{3}} \\ x &= 30^\circ \text{ (reference angle / verwysingshoek)} \\ x &= 30^\circ + 180^\circ \cdot k, k \in \mathbb{Z} \end{aligned}$	<ul style="list-style-type: none"> ✓ $\cos 2x = \frac{1}{2}$ ✓ for / vir $2x$ in both quadrants / in beide kwadrante ✓ $x = 30^\circ + 180^\circ \cdot k$ ✓ $x = 150^\circ + 180^\circ \cdot k$ <p style="text-align: center;">OR / OF</p> <ul style="list-style-type: none"> ✓ multiplying by 2 and using identity / vermenigvuldig met 2 en gebruik van identiteit ✓ $3 \sin^2 x = \cos^2 x$ ✓ $\tan x = \frac{1}{\sqrt{3}}$ ✓ answer / antwoord 	(4)
5.5.1	$\begin{aligned} \text{LHS} &= \frac{\sin 2\theta \cdot \tan \theta}{\cos 2\theta + 1} \\ &= \frac{2 \sin \theta \cos \theta \cdot \frac{\sin \theta}{\cos \theta}}{2 \cos^2 \theta - 1 + 1} \\ &= \frac{2 \sin^2 \theta}{2 \cos^2 \theta} \\ &= \tan^2 \theta \end{aligned}$	<ul style="list-style-type: none"> ✓ $2 \sin \theta \cos \theta$ ✓ $\frac{\sin \theta}{\cos \theta}$ ✓ $2 \cos^2 \theta - 1$ ✓ $\frac{2 \sin^2 \theta}{2 \cos^2 \theta}$ 	(4)
5.5.2	$\begin{aligned} \cos 2\theta + 1 &= 0 \\ \cos 2\theta &= -1 \\ 2\theta &= 180^\circ \\ \theta &= 90^\circ \end{aligned}$	<ul style="list-style-type: none"> ✓ $\cos 2\theta + 1 = 0$ ✓ $\cos 2\theta = -1$ ✓ $2\theta = 180^\circ$ ✓ $\theta = 90^\circ$ 	(4)
			[30]

QUESTION 6 / VRAAG 6



6.1	$\Delta ABC \equiv \Delta ABD$ (SAS) / (SHS)	✓ S and/en R	(1)
6.2	$\cos \alpha = \frac{x}{AC}$ $AC = \frac{x}{\cos \alpha}$	✓ S ✓ answer / antwoord	(2)
6.3	$CD^2 = \left(\frac{x}{\cos \alpha}\right)^2 + \left(\frac{x}{\cos \alpha}\right)^2 - 2\left(\frac{x}{\cos \alpha}\right)\left(\frac{x}{\cos \alpha}\right) \cos(180^\circ - 2\beta)$ $CD^2 = \frac{x^2}{\cos^2 \alpha} + \frac{x^2}{\cos^2 \alpha} + 2\left(\frac{x^2}{\cos^2 \alpha}\right) \cos 2\beta$ $CD^2 = \frac{2x^2}{\cos^2 \alpha} (1 + \cos 2\beta)$ $CD^2 = \frac{2x^2}{\cos^2 \alpha} (1 + (1 - 2\sin^2 \beta))$ $CD^2 = \frac{2x^2}{\cos^2 \alpha} \times 2\cos^2 \beta$ $CD^2 = \frac{4x^2 \cos^2 \beta}{\cos^2 \alpha}$ $\therefore CD = \frac{2x \cos \beta}{\cos \alpha}$	✓ cos rule / cos-reël ✓ simplification vereenvoudiging ✓ double angles expansion dubbelhoeke uitbreiding ✓ simplification vereenvoudiging	

OR / OF

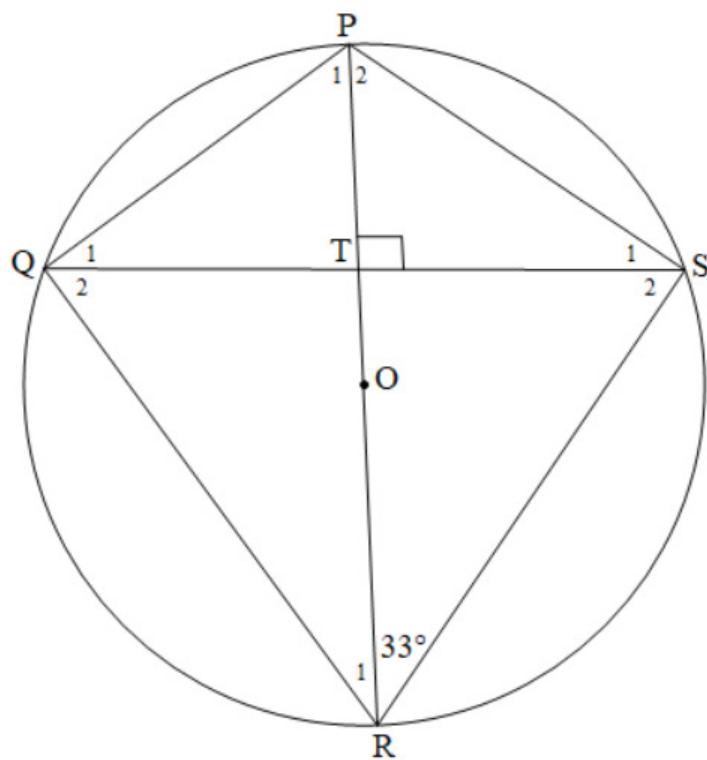
OR / OF

	$\begin{aligned} A\hat{D}B &= \beta \\ C\hat{A}D &= 180^\circ - 2\beta \\ CD &= \frac{AC}{\sin \beta} \\ \sin(180^\circ - 2\beta) &= \frac{AC \sin 2\beta}{\sin \beta} \\ CD &= \frac{AC \sin 2\beta}{2 \sin \beta \cos \beta} \\ CD &= \frac{x \cdot 2 \sin \beta \cos \beta}{\cos \alpha \sin \beta} \\ CD &= \frac{2x \cos \beta}{\cos \alpha} \end{aligned}$	<ul style="list-style-type: none"> ✓ for /vir $A\hat{D}B = \beta$ and/en $C\hat{A}D = 180^\circ - 2\beta$ ✓ use of sin rule <i>gebruik van sinus-reël</i> ✓ substitution of AC <i>vervanging van AC</i> ✓ simplification / <i>vereenvoudiging</i> 	(4)
6.4	$\begin{aligned} CD &= \frac{2x \cos \beta}{\cos \alpha} \\ CD &= \frac{2(25) \cos 65,62^\circ}{\cos 30^\circ} \\ CD &= 23,83 \text{ cm} \end{aligned}$	<ul style="list-style-type: none"> ✓ substitution / <i>vereenvoudiging</i> ✓ answer / <i>antwoord</i> 	(2)
			[9]

QUESTION 7 / VRAAG 7

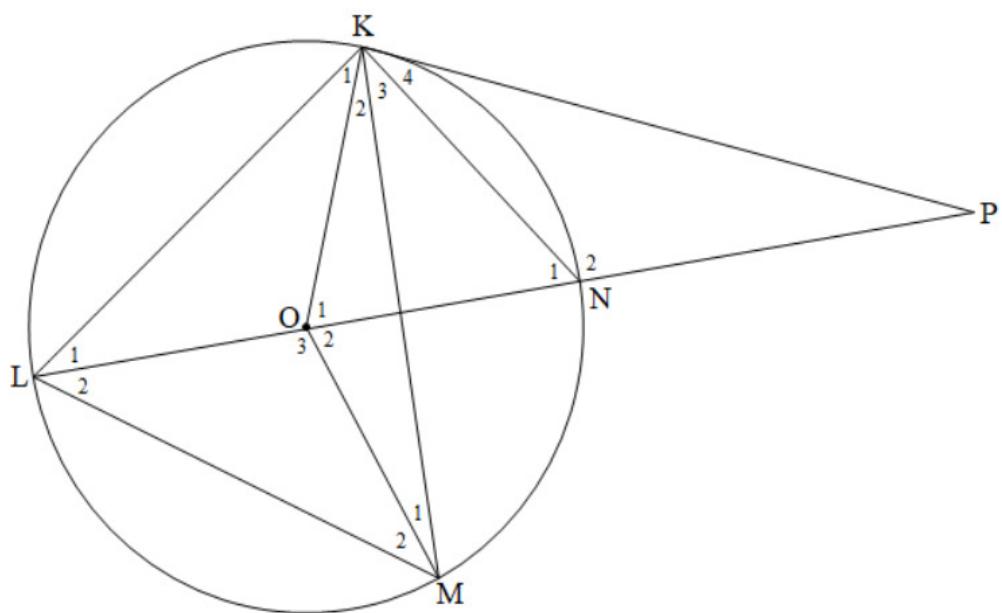
7.1	$f(180^\circ) = -0,71$ $\therefore \text{Range: Terrein: Waardeversameling: } -0,71 \leq y \leq 1$ OR / OF $[-0,71; 1]$	<ul style="list-style-type: none"> ✓ $f(180^\circ)$ ✓ answer / <i>antwoord</i> 	(2)
7.2	<p style="text-align: center;">\checkmark intercepts / <i>afsnitte</i> \checkmark shape / <i>vorm</i> \checkmark turning points / <i>draaipunte</i></p>		(3)
7.3	Period / <i>Periode</i> = 180°	✓ answer / <i>antwoord</i>	(1)
7.4	$-45^\circ < x < 45^\circ$	✓✓ answer / <i>antwoord</i>	(2)
7.5	$x = -45^\circ$ or / of $x = 135^\circ$	<ul style="list-style-type: none"> ✓ $x = -45^\circ$ ✓ $x = 135^\circ$ 	(2)
7.6	$g(x) = \cos(x + 15^\circ)$	✓ answer / <i>antwoord</i>	(1)
			[11]

QUESTION 8 / VRAAG 8



8.1.1	$\hat{Q}_1 = 33^\circ$ (\angle s in the same segment) $(\angle e$ in dieselfde segment)	$\checkmark S \checkmark R$	
	$\hat{P}_1 = 57^\circ$ (\angle s of a triangle) / ($\angle e$ van 'n driehoek)	$\checkmark S$ and/en R	(3)
8.1.2	$\hat{Q} = 90^\circ$ (\angle subtended by the diameter) $(\angle onderspan deur middellyn)$	$\checkmark S$ and/en R	
	$\hat{Q}_2 = 57^\circ$ (complementary \angle s / \angle s of a triangle) $(komplementêre \angle e / \angle e$ van 'n driehoek)	$\checkmark S$ and/en R	(2)
8.2	$QT = TS = 8 \text{ cm}$ (line from centre perp to chord) $(lyn vanaf middelpunt loodreg op koord)$	$\checkmark S$ and/en R	
	$OQ = OS = 10 \text{ cm}$ (radii) / (radiusse)	$\checkmark S$ and/en R	
	$OQ^2 = TO^2 + QT^2$ (Pythagoras) / (Pythagoras)	$\checkmark S$ and/en R	
	$10^2 = OT^2 + 8^2$		
	$OT = \sqrt{100 - 64} = 6 \text{ cm}$	\checkmark answer / antwoord	(4)
			[9]

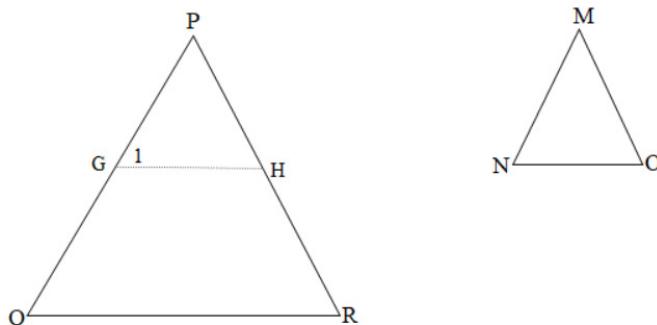
QUESTION 9 / VRAAG 9



9.1	$\hat{L}KN = 90^\circ$ $\hat{O}KP = 90^\circ$	✓ answer / antwoord ✓ answer / antwoord	(2)
9.2.1	$\hat{L}_1 = x$ (tan – chord theorem) / (raaklyn-koord stelling)	✓ S ✓ R	(2)
9.2.2	$\hat{K}_1 = x$ (\angle s opp. = sides) / (\angle e teenoor = sye)	✓ S ✓ R	(2)
9.2.3	In ΔLKP ; $\hat{L}KP = 90^\circ + x$ and/en $\hat{L}_1 = x$ $\therefore \hat{P} = 90^\circ - 2x$ (\angle s of a triangle) (\angle e van 'n driehoek)	✓ S ✓ R OR / OF $\hat{N}_2 = 90^\circ + x$ (ext \angle of Δ) / (buite \angle van Δ) $\therefore \hat{P} = 90^\circ - 2x$ (\angle s of a triangle) (\angle e van 'n driehoek)	 OR / OF ✓ S/R ✓ S/R (2)
9.3	$\hat{OMP} = 90^\circ$ (tan \perp rad) / (raaklyn \perp radius) $\hat{OKP} = 90^\circ$ (proven) / (bewys) $\therefore \text{KOMP is a c.q. (opp. } \angle\text{s suppl.)}$ KOMP is 'n kv (teenoorst. \angle e supplementêr)	✓ S & R ✓ S ✓ R	(3)
			[11]

QUESTION 10 / VRAAG 10

10.1



On PQ , mark $PG = MN$ and on PR , mark off $PH = MO$
Join GH

In ΔPGH and ΔMNO

- (1) $PG = MN$ (construction)
- (2) $\hat{P} = \hat{M}$ (given)
- (3) $PH = MO$ (construction)

$\therefore \Delta PGH \equiv \Delta MNO$ (SAS)

$\therefore \hat{G}_1 = \hat{N}$ (Congruency)

But $\hat{Q} = \hat{N}$ (given)

$\therefore \hat{G}_1 = \hat{Q}$

$\therefore GH \parallel QR$ (corresponding angles formed =)

$\therefore \frac{PG}{PQ} = \frac{PH}{PR}$ (prop.int; $GH \parallel QR$)

But $PG = MN$ and $PH = MO$

$\therefore \frac{MN}{PQ} = \frac{MO}{PR}$

✓ construction

✓ congruency proof

✓ S ✓ R

✓ S and/en R

✓ S

Afrikaans

Op PQ , merk af $PG = MN$ en op PR , merk af $PH = MO$
Verbind GH

In ΔPGH en ΔMNO

- (1) $PG = MN$ (konstruksie)
- (2) $\hat{P} = \hat{M}$ (gegee)
- (3) $PH = MO$ (konstruksie)

$\therefore \Delta PGH \equiv \Delta MNO$ (SHS)

$\therefore \hat{G}_1 = \hat{N}$ (Kongruensie)

Maar, $\hat{Q} = \hat{N}$ (gegee)

$\therefore \hat{G}_1 = \hat{Q}$

$\therefore GH \parallel QR$ (ooreenkomsige hoeke gevorm =)

$\therefore \frac{PG}{PQ} = \frac{PH}{PR}$ (eweredigheid; $GH \parallel QR$)

Maar, $PG = MN$ en $PH = MO$

$\therefore \frac{MN}{PQ} = \frac{MO}{PR}$

✓ konstruksie

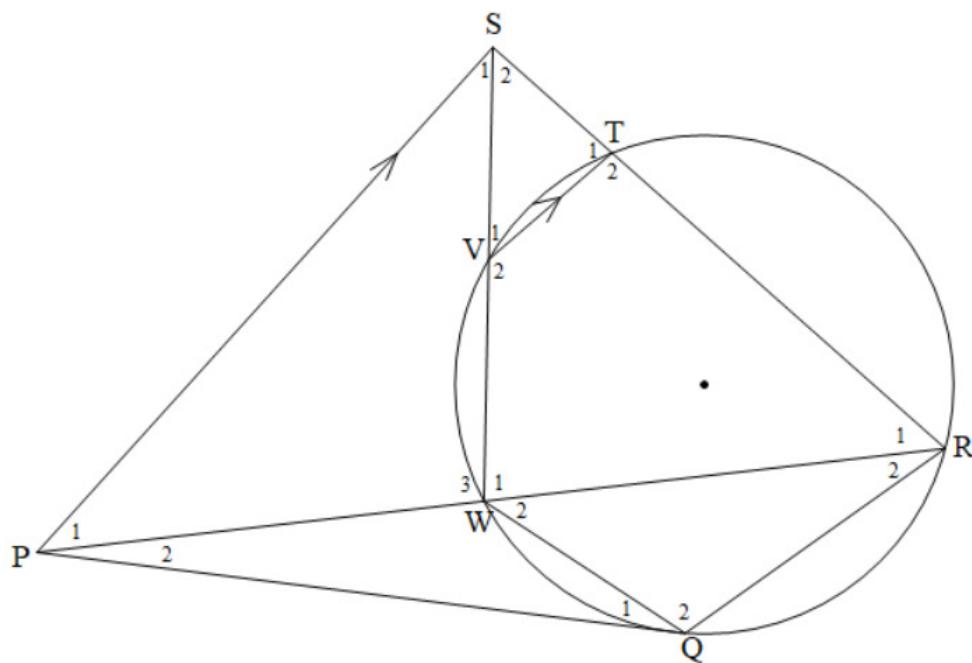
✓ kongruensie bewys

✓ S ✓ R

✓ S and/en R

✓ S

(6)



10.2.1	$\hat{S}_1 = \hat{V}_1$ (alt \angle s; $PS \parallel VT$) / (verw. $\angle e$; $PS \parallel VT$) $\hat{V}_1 = \hat{R}_1$ (ext. \angle of cq $RTVW$) / (buite \angle van kv $RTVW$) $\therefore \hat{S}_1 = \hat{R}_1$	<input checked="" type="checkbox"/> S and/en R <input checked="" type="checkbox"/> S ✓ R	(3)
10.2.2	In ΔPWS and/en ΔPSR (1) \hat{P}_1 is common / is gemeen (2) $\hat{S}_1 = \hat{R}_1$ (proven) / (bewys) (3) 3 rd angle of a triangle / (3 ^{de} hoek van driehoek) $\Delta PWS \parallel \Delta PSR$ (AAA) / (HHH) / ($\angle\angle\angle$)	<input checked="" type="checkbox"/> S <input checked="" type="checkbox"/> R <input checked="" type="checkbox"/> S and/en R	(3)
10.2.3	In ΔPQW and/en ΔPRQ (1) $\hat{Q}_1 = \hat{R}_2$ (tan – chord theorem) / (raaklyn – koord stelling) (2) \hat{P}_2 is common / is gemeen (3) 3 rd angle of a triangle / 3 ^{de} hoek van driehoek $\Delta PQW \parallel \Delta PRQ$ (AAA) $\therefore \frac{PQ}{PR} = \frac{PW}{PQ}$ (similarity) / (gelykvormig) $\therefore PQ^2 = PW \cdot PR$	<input checked="" type="checkbox"/> S and/en R <input checked="" type="checkbox"/> S <input checked="" type="checkbox"/> S and/en R <input checked="" type="checkbox"/> S <input checked="" type="checkbox"/> S	(5)
10.2.4	From / Vanaf 10.2.1 $\frac{PW}{PS} = \frac{PS}{SR}$ ($\Delta PWS \parallel \Delta PSR$) $\therefore PS^2 = PW \cdot PR$ From / Vanaf 10.2.2 $PQ^2 = PW \cdot PR$ $\therefore PQ = PS$	<input checked="" type="checkbox"/> S <input checked="" type="checkbox"/>	(3)
			[20]

TOTAL / TOTAAL: 150