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FINAL



KWAZULU-NATAL PROVINCE

EDUCATION
REPUBLIC OF SOUTH AFRICA

MATHEMATICS

COMMON TEST

MARCH 2025

MARKING GUIDELINES

**NATIONAL
SENIOR CERTIFICATE**

GRADE 12

MARKS: 100

These marking guidelines consist of 11 pages.



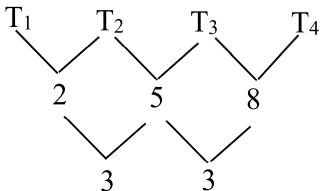
GRADE 12
Marking Guideline

QUESTION 1

1.1.1	$S_{21} = 3(21)^2 - 5(21)$ $= 1218$	✓A substitution ✓A answer (2)
1.1.2	$S_{22} = 3(22)^2 - 5(22)$ $= 1342$ $T_{22} = S_{22} - S_{21}$ $= 1342 - 1218$ $= 124$	✓A value of S_{22} ✓CA answer (2)
1.1.3	$8162 = 3n^2 - 5n$ $3n^2 - 5n - 8162 = 0$ $n = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(3)(-8162)}}{2(3)}$ $n = 53 \quad \text{or} \quad n = -\frac{154}{3}$ N/A 53 terms have to be added	✓A equating ✓A standard form ✓CA substitution ✓CA answer (53 only) (4)
1.2.1	The even-numbered terms form an AS with $a = 7$ and $d = 5$. T_{39} of the AS $= a + (n-1)d$ $= 7 + (39-1)5$ $= 197$	 ✓A substitution ✓CA answer (2)
1.2.2	Sum of the 52 odd-numbered terms $= 52 \times 7 = 364$ Sum of the 51 even-numbered terms $= \frac{n}{2} [2a + (n-1)d]$ $= \frac{51}{2} [2(7) + (51-1) \cdot 5]$ $= 6732$ Sum of first 103 terms $= 364 + 6732$ $= 7096$	✓A 52×7 ✓CA substitution ✓CA sum of AS ✓CA answer (4)
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QUESTION 2

2.1.1	9 ; -27 ; 81	✓A 9 ✓A -27 ; 81 (2)
2.1.2	$r = -3$	✓A answer (1)
2.1.3	No, the series will not converge $r < -1$ OR r does not lie between -1 and 1.	✓CA answer (no) ✓CA motivation (2)
2.1.4	$a = 9x$ $r = -3$ $n = 12$ $S_n = \frac{a(r^n - 1)}{r - 1}$ $= \frac{9x((-3)^{12} - 1)}{-3 - 1}$ $= -1\,195\,740x$	✓A $n = 12$ ✓CA substitution ✓CA answer (3)
2.2	 $2^{\text{nd}} \text{ difference} = 3$ $a = \frac{2^{\text{nd}} \text{ difference}}{2} = \frac{3}{2}$ $3a + b = 2$ $b = 2 - 3\left(\frac{3}{2}\right) = -\frac{5}{2}$ $T_{29} = \frac{3}{2}(29)^2 - \frac{5}{2}(29) + c = 1166$ $c = -23$ $\therefore T_n = \frac{3}{2}n^2 - \frac{5}{2}n - 23$ $T_1 = \frac{3}{2}(1)^2 - \frac{5}{2}(1) - 23 = -24$	✓A $2^{\text{nd}} \text{ difference} = 3$ ✓CA value of a ✓CA value of b ✓CA substitution in T_{29} ✓CA value of c ✓CA answer (6)

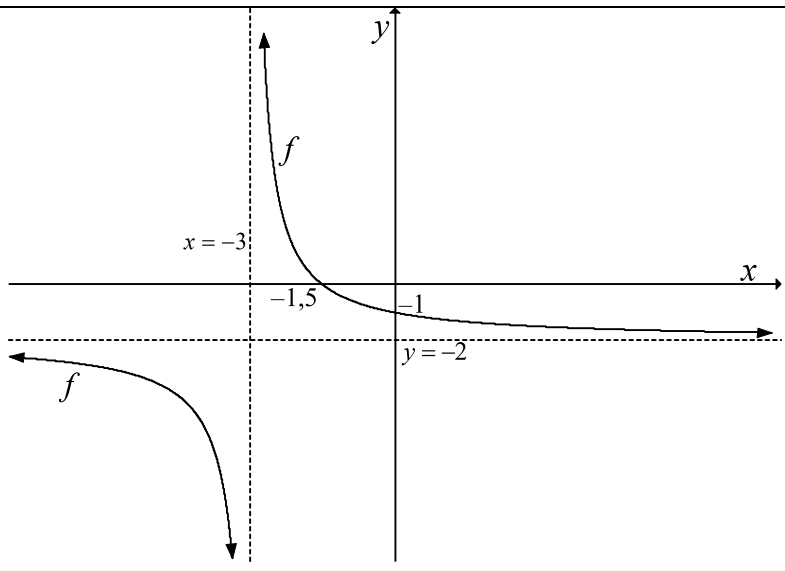
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QUESTION 3

3.1.1	$f(x) = \frac{2x+3}{-x-3}$ $= \frac{2x+3}{-(x+3)}$ $= \frac{-(2x+3)}{x+3}$ $= \frac{-(2x+6-3)}{x+3}$ $= \frac{-[2(x+3)-3]}{x+3}$ $= \frac{-2(x+3)}{x+3} + \frac{3}{x+3}$ $\therefore f(x) = \frac{3}{x+3} - 2$ OR $f(x) = \frac{2x+3}{-x-3}$ $= -2 + \frac{-3}{-x-3}$ $= -2 + \frac{-3}{-(x+3)}$ $= -2 + \frac{3}{x+3}$	✓A $-(x+3)$ ✓A $\frac{-[2(x+3)-3]}{x+3}$ (2) OR ✓A $-2 + \frac{-3}{-x-3}$ (through the method of long division) ✓A $-(x+3)$ (2)
3.1.2	For y-intercept, let $x = 0$: $y = \frac{3}{x+3} - 2$ $y = \frac{3}{0+3} - 2 = -1$ For x-intercept, let $y = 0$: $\frac{3}{x+3} - 2 = 0$ $\frac{3}{x+3} = 2$ $x = -\frac{3}{2}$	✓A $y = -1$ ✓A $\frac{3}{x+3} - 2 = 0$ ✓A $x = -\frac{3}{2}$ (3)

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3.1.3		✓CA intercepts ✓A asymptotes ✓A shape (3)
3.1.4	$y = -x + c$ Substitute $(-3 ; -2)$: $-2 = -(-3) + c$ $c = -5$ $y = -x - 5$	✓A equation of straight line with a gradient of -1 ✓CA answer (2)
3.1.5 (a)	$x \in R, x \neq -3$	✓A $x \in R$ ✓CA $x \neq -3$ (2)
3.1.5 (b)	$-3 < x \leq -\frac{3}{2}$	✓CA ✓CA $-3 < x \leq -\frac{3}{2}$ (2)

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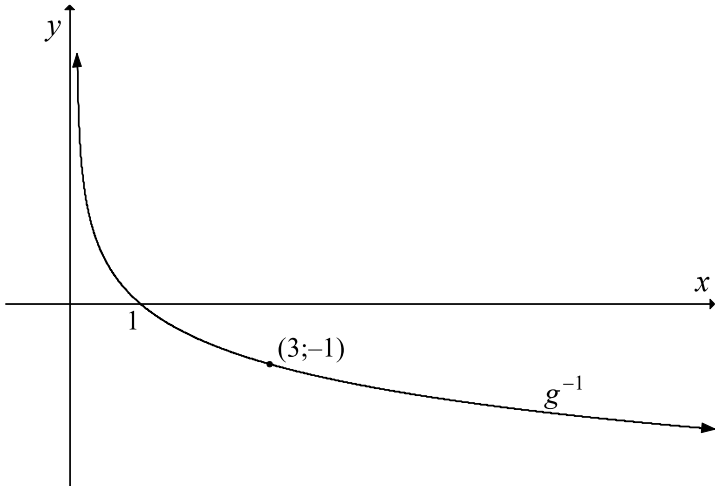
3.2.1	At R: $3x + 6 = 0$ $x = -2$ $R(-2 ; 0)$	✓A x -coordinate ✓A y -coordinate (2)
3.2.2	From symmetry, the x -coordinate at $S = 1$ $y = a(x + 2)(x - 1)$ $y = ax^2 + ax - 2a$ Substitute $\left(-\frac{1}{2}; 9\right)$: $9 = a\left(-\frac{1}{2}\right)^2 + a\left(-\frac{1}{2}\right) - 2a$ $9 = -\frac{9}{4}a$ $\therefore a = -4$ $\therefore y = -4x^2 - 4x + 8$ OR $y = a(x + p)^2 + q$ $y = a\left(x + \frac{1}{2}\right)^2 + 9$ Subst. $S(1 ; 0)$ OR Subst. $R(-2 ; 0)$: $0 = a\left(1 + \frac{1}{2}\right)^2 + 9$ OR $0 = a\left(-2 + \frac{1}{2}\right)^2 + 9$ $\therefore -9 = a\left(\frac{9}{4}\right)$ $a = -4$ $\therefore y = -4\left(x + \frac{1}{2}\right)^2 + 9$	✓CA $y = a(x + 2)(x - 1)$ ✓CA substitution ✓CA value of a ✓CA answer..... OR ✓A $y = a\left(x + \frac{1}{2}\right)^2 + 9$ ✓CA substitution ✓CA value of a ✓CA answer (4)
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QUESTION 4

4.1.1	$f^{-1}: y = \sqrt{3x}$ $f: x = \sqrt{3y}$ $x^2 = 3y$ $y = \frac{x^2}{3}; x \geq 0$	✓A swapping x and y ✓A $y = \frac{x^2}{3}$ ✓A $x \geq 0$ (3)
4.1.2	$0 \leq x \leq 3$ OR $x \in [0 ; 3]$	✓A ✓A answer (2)

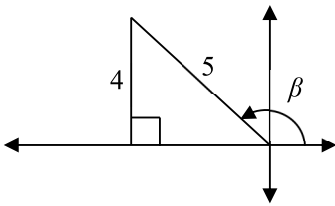


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4.2.1	$g: y = \left(\frac{1}{3}\right)^x$ OR $g: y = 3^{-x}$ $g^{-1}: x = \left(\frac{1}{3}\right)^y$ $g^{-1}: x = 3^{-y}$ $\therefore y = \log_{\frac{1}{3}} x$ $\therefore y = -\log_3 x$	✓A swapping x and y ✓A answer (2)
4.2.2		✓CA shape ✓A x -intercept ✓CA coordinates of one more point (3)
4.2.3	$y = a\left(\frac{1}{3}\right)^x + 7$ Substitute $(-2; 10)$: $10 = a\left(\frac{1}{3}\right)^{-2} + 7$ $9a = 3$ $a = \frac{1}{3}$	✓A substitution ✓CA answer (2)
4.2.4	$h: y = \left(\frac{1}{3}\right) \cdot \left(\frac{1}{3}\right)^x + 7$ From $y = \left(\frac{1}{3}\right)^{x+1} + 7$ to $y = \left(\frac{1}{3}\right)^x$: Translation of 1 unit to the right and 7 units downwards. Answer only: full marks	✓A $y = \left(\frac{1}{3}\right)^{x+1} + 7$ ✓A 1 unit to the right ✓A 7 units downwards (3)
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QUESTION 5

5.1.1	$\sin \beta = \frac{4}{5}$ $x^2 = r^2 - y^2 \quad [\text{Pythagoras}]$ $= 5^2 - 4^2$ $= 9$ $x = -3$ $\therefore \cos \beta = \frac{-3}{5}$ 	✓A $\sin \beta = \frac{4}{5}$ ✓A x - value ✓CA answer (3)
5.1.2	$\cos 2\beta = 2\cos^2 \beta - 1$ $= 2\left(\frac{-3}{5}\right)^2 - 1$ $= 2\left(\frac{9}{25}\right) - 1$ $= \frac{-7}{25}$ OR $\cos 2\beta = \cos^2 \beta - \sin^2 \beta$ $= \left(\frac{-3}{5}\right)^2 - \left(\frac{4}{5}\right)^2$ $= \frac{9}{25} - \frac{16}{25}$ $= \frac{-7}{25}$ OR $\cos 2\beta = 1 - 2\sin^2 \beta$ $= 1 - 2\left(\frac{4}{5}\right)^2$ $= 1 - 2\left(\frac{16}{25}\right)$ $= \frac{-7}{25}$	✓A double $\angle$ expansion ✓CA substitution ✓CA answer (3) OR ✓A double $\angle$ expansion ✓CA substitution ✓CA answer (3) OR ✓A double $\angle$ expansion ✓A substitution ✓CA answer (3)

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5.1.3	$\sin 3\beta = \sin(2\beta + \beta)$ $= \sin 2\beta \cos \beta + \cos 2\beta \sin \beta$ $= 2 \sin \beta \cos \beta \cos \beta + \cos 2\beta \sin \beta$ $= 2 \left(\frac{4}{5} \right) \left(\frac{-3}{5} \right) \left(\frac{-3}{5} \right) + \left(\frac{-7}{25} \right) \left(\frac{4}{5} \right)$ $= \frac{72}{125} - \frac{28}{125}$ $= \frac{44}{125}$	✓A compound $\angle$ expansion ✓A double $\angle$ expansion ✓CA substitution ✓CA answer (4)
5.2	$\frac{\sin(-180^\circ - \theta) \tan(180^\circ - \theta) \cos(-\theta)}{\cos^2(90^\circ + \theta) + 3 \sin^2 \theta}$ $= \frac{\sin \theta \cdot -\tan \theta \cdot \cos \theta}{(-\sin \theta)^2 + 3 \sin^2 \theta}$ $= \frac{\sin \theta \cdot -\frac{\sin \theta}{\cos \theta} \cdot \cos \theta}{4 \sin^2 \theta}$ $= -\frac{\sin^2 \theta}{4 \sin^2 \theta}$ $= -\frac{1}{4}$	✓A $\sin \theta$ ✓A $-\tan \theta$ ✓A $\cos \theta$ ✓A $-\sin \theta$ ✓A $\tan \theta = \frac{\sin \theta}{\cos \theta}$ ✓CA answer (6)
5.3	$\frac{1}{8}(1 - \cos 4x)$ $= \frac{1}{8}[1 - \cos(2 \times 2x)]$ $= \frac{1}{8}[1 - (1 - 2 \sin^2 2x)]$ $= \frac{1}{8}[2 \sin^2 2x]$ $= \frac{1}{4}[\sin^2 2x]$ $= \frac{1}{4}(2 \sin x \cos x)^2$ $= \frac{1}{4}(4)(\sin^2 x \cdot \cos^2 x)$ $= \sin^2 x \cdot \cos^2 x$ OR	✓A $\frac{1}{8}[1 - \cos(2 \times 2x)]$ ✓A $\frac{1}{8}[1 - (1 - 2 \sin^2 2x)]$ ✓A $\frac{1}{4}[\sin^2 2x]$ ✓A $\frac{1}{4}(2 \sin x \cos x)^2$ ✓A $\frac{1}{4}(4)(\sin^2 x \cdot \cos^2 x)$ OR (5)

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QUESTION 6

6.1	$\cos(x - 45^\circ) = \sin 2x$ $\cos(x - 45^\circ) = \cos(90^\circ - 2x)$ $x - 45^\circ = 90^\circ - 2x + k.360^\circ$ or $x - 45^\circ = 360^\circ - (90^\circ - 2x) + k.360^\circ$ $3x = 135^\circ + k.360^\circ$ $x - 45^\circ = 270^\circ + 2x + k.360^\circ$ $x = 45^\circ + k.120^\circ, k \in \mathbb{Z}$ $-x = 315^\circ + k.360^\circ$ $x = -315^\circ - k.360^\circ$ $x = 45^\circ + k.360^\circ; k \in \mathbb{Z}$ OR $\cos(x - 45^\circ) = \sin 2x$ $\sin[90^\circ - (x - 45^\circ)] = \sin 2x$ $-x + 135^\circ = 2x + k.360^\circ$ or $-x + 135^\circ = 180^\circ - 2x + k.360^\circ$ $3x = 135^\circ + k.360^\circ$ $x = 45^\circ + k.360^\circ$ $x = 45^\circ + k.120^\circ, k \in \mathbb{Z}$ $x = 45^\circ + k.360^\circ, k \in \mathbb{Z}$	✓A co-ratio ✓A both equations ✓CA $45^\circ + k.120^\circ$ ✓A $k \in \mathbb{Z}$ OR ✓A co-ratio ✓A both equations ✓CA $45^\circ + k.120^\circ$ ✓A $k \in \mathbb{Z}$ (4)
6.2.1	360°	✓A answer (1)
6.2.2 (a)	$(-135^\circ; -1)$	✓A x-coordinate ✓A y-coordinate (2)
6.2.2 (b)	$\left(-75^\circ; -\frac{1}{2}\right)$	✓CA x-coordinate ✓CA y-coordinate (2)
6.2.3	$90^\circ < x < 135^\circ$ OR $x \in (90^\circ; 135^\circ)$	✓A ✓A answer (2)
6.2.4	$\frac{1}{\sqrt{2}}(\cos x + \sin x)$ $= \frac{1}{\sqrt{2}}\cos x + \frac{1}{\sqrt{2}}\sin x$ $\cos 45^\circ \cdot \cos x + \sin 45^\circ \sin x$ $= \cos(x - 45^\circ)$ $\therefore$ To solve for x if $\sin 2x \geq \cos(x - 45^\circ)$: $x = 45^\circ$ or $x \in [165^\circ; 180^\circ]$ OR $x = 45^\circ$ or $165^\circ \leq x \leq 180^\circ$	✓A $\cos 45^\circ \cdot \cos x + \sin 45^\circ \sin x$ ✓A compound $\angle$ identity ✓A $x = 45^\circ$ ✓CA ✓CA $x \in [165^\circ; 180^\circ]$ or $165^\circ \leq x \leq 180^\circ$ (5)
[16]		

TOTAL: 100

